



Model created in COMSOL Multiphysics 6.4

# Shape Optimization of a Shell

## *Introduction*

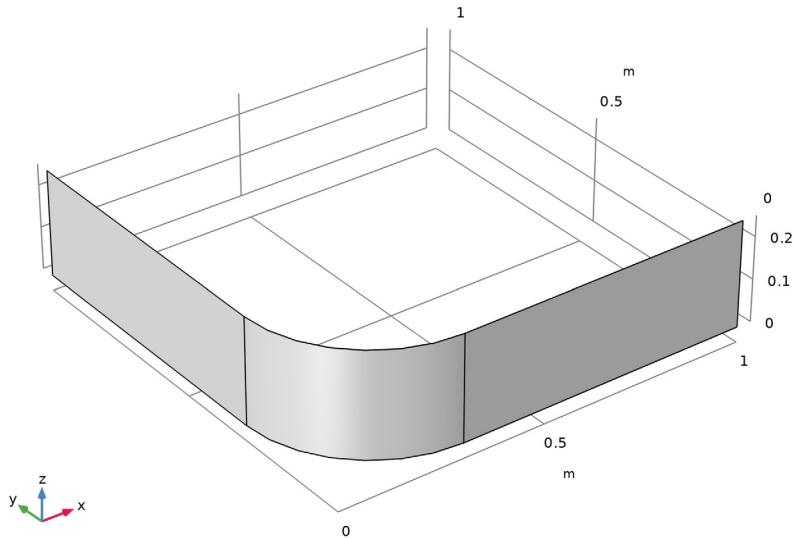
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Shape optimization can be used to alter the geometry of an existing product to improve its performance. You can do that using the **Deformed Geometry** interface, but you have to decide which shape deformations to allow. It is important to impose some restriction to preserve the mesh quality during the optimization. One approach is to use a Helmholtz filter to introduce a length scale, which (in combination with a maximum displacement parameter) limits the slope of the shape variations. This type of regularized shape optimization can be set up using equation based modeling, but it is also built into the **Free Shape Shell** feature. This feature differs from the **Free Shape Boundary** feature in that it can be used on boundaries that are not adjacent to meshed domains.

## *Model Definition*

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Shape optimization is often subject to constraints on the geometry deformation, and this model shows how the **Free Shape Shell** feature can be combined with the **Symmetry/Roller** feature to restrict edges to move along an imaginary boundary defined by a normal vector. The sides as well as the loaded edges are fixed using the **Fixed Edge** feature. The initial geometry of the shell is shown in [Figure 1](#). Note that symmetry is exploited so that only half of the shell has to be modeled.



*Figure 1: The initial geometry is shown. The load is applied in the  $y$  direction on the rightmost edge, while the displacement and rotation is fixed at the leftmost edge of the shell. The shape deformation of this edge is restricted to the  $xz$ -plane.*

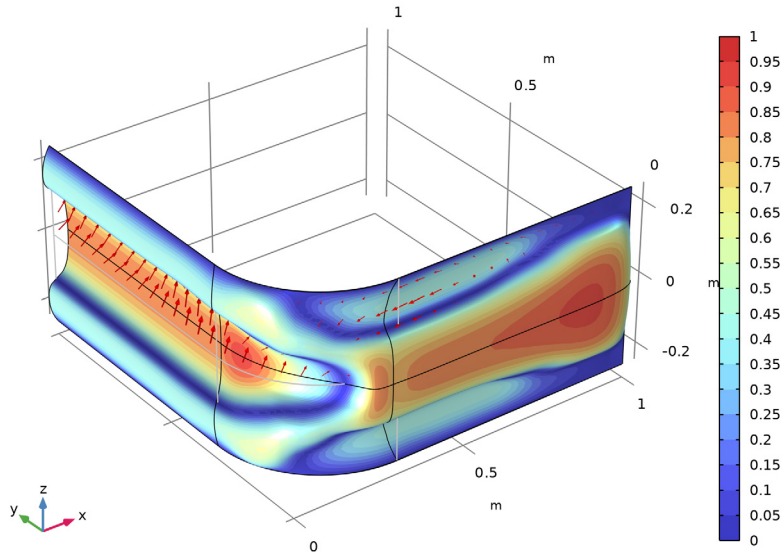
The shell is made of steel and the objective is to maximize its stiffness by deforming it. An initial study is performed to determine a characteristic value for the area and the total elastic strain energy.

The model uses geometric nonlinearity, because the applied load is so large that this is warranted.

## Results and Discussion

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The optimal design is intuitive in the sense that it deforms the shell, so that material is moved away from the midplane, increasing the stiffness of the shell; see [Figure 2](#).



*Figure 2: The default shape optimization plot shows the edges of the old geometry in gray together with a surface plot of the relative normal boundary displacement in colors. The actual displacement is shown with red arrows.*

By deforming the shell, the optimization is able to reduce the elastic strain energy by 89%. This causes a 9% increase in the surface area.

## Notes About the COMSOL Implementation

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This model combines the Optimization and Shell interfaces. The shape optimization features are added before the first study is computed, because this automatically sets the correct scales for the shape optimization variables. It is possible to add the shape optimization features after the first study has been computed, but then the first study will no longer converge (the shape optimization variables cannot be disabled).

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**Application Library path:** Optimization\_Module/Shape\_Optimization/  
shell\_shape\_optimization


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### *Modeling Instructions*




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From the **File** menu, choose **New**.

#### **NEW**

In the **New** window, click  **Model Wizard**.

#### **MODEL WIZARD**

- 1 In the **Model Wizard** window, click  **3D**.
- 2 In the **Select Physics** tree, select **Structural Mechanics > Shell (shell)**.
- 3 Click **Add**.
- 4 Click  **Study**.
- 5 In the **Select Study** tree, select **General Studies > Stationary**.
- 6 Click  **Done**.

#### **GLOBAL DEFINITIONS**


##### *Parameters I*

- 1 In the **Model Builder** window, under **Global Definitions** click **Parameters I**.
- 2 In the **Settings** window for **Parameters**, locate the **Parameters** section.
- 3 In the table, enter the following settings:

<b>Name</b>	<b>Expression</b>	<b>Value</b>	<b>Description</b>
Lmax	5[cm]	0.05 m	Maximum displacement
Fload	10[kN]	10000 N	Load

#### **GEOMETRY I**


##### *Work Plane I (wp1)*

In the **Geometry** toolbar, click  **Work Plane**.


##### *Work Plane I (wp1) > Plane Geometry*

In the **Model Builder** window, click **Plane Geometry**.

*Work Plane 1 (wpl) > Square 1 (sql)*

In the **Work Plane** toolbar, click  **Square**.

*Work Plane 1 (wpl) > Fillet 1 (fill)*

1 In the **Work Plane** toolbar, click  **Fillet**.

2 On the object **sql**, select Point 1 only.

3 In the **Settings** window for **Fillet**, locate the **Radius** section.

4 In the **Radius** text field, type 0.3.

*Work Plane 1 (wpl) > Convert to Curve 1 (ccurl)*

1 In the **Work Plane** toolbar, click  **Conversions** and choose **Convert to Curve**.

2 Select the object **fill** only.

*Edges to Delete*

1 In the **Work Plane** toolbar, click  **Selections** and choose **Box Selection**.

2 In the **Settings** window for **Box Selection**, type Edges to Delete in the **Label** text field.

3 Locate the **Geometric Entity Level** section. From the **Level** list, choose **Boundary**.

4 Locate the **Box Limits** section. In the **xw minimum** text field, type 0.9.

5 In the **yw minimum** text field, type 0.9.

*Work Plane 1 (wpl) > Delete Entities 1 (dell)*

1 Right-click **Plane Geometry** and choose **Delete Entities**.

2 In the **Settings** window for **Delete Entities**, locate the **Entities or Objects to Delete** section.

3 From the **Selection** list, choose **Edges to Delete**.

*Extrude 1 (ext1)*

1 In the **Model Builder** window, right-click **Geometry 1** and choose **Extrude**.


2 In the **Settings** window for **Extrude**, locate the **Distances** section.

3 In the table, enter the following settings:

<b>Distances (m)</b>
0.25



4 Locate the **Selections of Resulting Entities** section. Select the **Resulting objects selection** checkbox.

5 From the **Show in physics** list, choose **Boundary selection**.



6 In the **Geometry** toolbar, click  **Build All**.

The geometry should now look like that in [Figure 1](#).



#### *Exterior Edges*

- 1 In the **Geometry** toolbar, click  **Selections** and choose **Adjacent Selection**.
- 2 In the **Settings** window for **Adjacent Selection**, type Exterior Edges in the **Label** text field.
- 3 Locate the **Input Entities** section. From the **Geometric entity level** list, choose **Boundary**.
- 4 Locate the **Output Entities** section. From the **Geometric entity level** list, choose **Adjacent edges**.
- 5 Locate the **Input Entities** section. Click  **Add**.
- 6 In the **Add** dialog, select **Extrude I** in the **Input selections** list.
- 7 Click **OK**.

#### *Symmetry Edge*

- 1 In the **Geometry** toolbar, click  **Selections** and choose **Box Selection**.
  - 2 In the **Settings** window for **Box Selection**, locate the **Geometric Entity Level** section.
  - 3 From the **Level** list, choose **Edge**.
  - 4 In the **Label** text field, type Symmetry Edge.
  - 5 Locate the **Box Limits** section. In the **z maximum** text field, type eps.
  - 6 Locate the **Output Entities** section. From the **Include entity if** list, choose **Entity inside box**.
  - 7 In the **Geometry** toolbar, click  **Build All**.
- The model geometry is now complete.

### **ADD MATERIAL**

- 1 In the **Materials** toolbar, click  **Add Material** to open the **Add Material** window.
- 2 Go to the **Add Material** window.
- 3 In the tree, select **Built-in > Structural steel**.
- 4 Click the **Add to Component** button in the window toolbar.
- 5 In the **Materials** toolbar, click  **Add Material** to close the **Add Material** window.


### **MESH I**

#### *Mapped I*

- 1 In the **Mesh** toolbar, click  **More Generators** and choose **Mapped**.


- 2 In the **Settings** window for **Mapped**, locate the **Boundary Selection** section.
- 3 From the **Selection** list, choose **All boundaries**.

#### *Size*


- 1 In the **Model Builder** window, click **Size**.
- 2 In the **Settings** window for **Size**, locate the **Element Size** section.
- 3 From the **Predefined** list, choose **Finer**.
- 4 Click to expand the **Element Size Parameters** section. In the **Maximum element size** text field, type  $L_{max}$ .
- 5 In the **Minimum element size** text field, type  $L_{max}/2$ .
- 6 Click  **Build All**.

#### **SHELL (SHELL)**


Enable weak slit and normal constraints to get the correct gradient from the sensitivity analysis performed during the optimization.

- 1 In the **Model Builder** window, under **Component 1 (comp1)** click **Shell (shell)**.
- 2 In the **Settings** window for **Shell**, click to expand the **Fold-Line Settings** section.
- 3 From the **Fold-line constraint** list, choose **Weak constraint**.
- 4 Click the  **Show More Options** button in the **Model Builder** toolbar.
- 5 In the **Show More Options** dialog, select **Physics > Advanced Physics Options** in the tree.
- 6 In the tree, select the checkbox for the node **Physics > Advanced Physics Options**.
- 7 Click **OK**.
- 8 In the **Settings** window for **Shell**, click to expand the **Advanced Settings** section.
- 9 From the **Normal constraint** list, choose **Weak constraint**.

#### *Fixed Constraint 1*

- 1 In the **Physics** toolbar, click  **Edges** and choose **Fixed Constraint**.
- 2 Select Edge 6 only.
- 3 In the **Settings** window for **Fixed Constraint**, click to expand the **Constraint Settings** section.
- 4 From the **Constraint** list, choose **Weak constraints**.


#### *Edge Load 1*

- 1 In the **Physics** toolbar, click  **Edges** and choose **Edge Load**.
- 2 Select Edge 10 only.

- 3 In the **Settings** window for **Edge Load**, locate the **Force** section.
- 4 From the **Load type** list, choose **Total force**.
- 5 Specify the  $\mathbf{F}_{\text{tot}}$  vector as

0	x
-Fload/2	y
0	z


#### *Symmetry I*

- 1 In the **Physics** toolbar, click  **Edges** and choose **Symmetry**.
- 2 In the **Settings** window for **Symmetry**, locate the **Edge Selection** section.
- 3 From the **Selection** list, choose **Symmetry Edge**.
- 4 Locate the **Coordinate System Selection** section. From the **Coordinate system** list, choose **Global coordinate system**.
- 5 Locate the **Symmetry** section. From the **Symmetry plane normal** list, choose **Third axis**.
- 6 Click to expand the **Constraint Settings** section. From the **Constraint** list, choose **Weak constraints**.

### **COMPONENT I (COMPI)**

Define the shape optimization problem using the **Free Shape Shell**, **Symmetry/Roller** and **Fixed Edge** features.

#### *Free Shape Shell I*


- 1 In the **Physics** toolbar, click  **Optimization** and choose **Shape Optimization, Shell**.
- 2 In the **Settings** window for **Free Shape Shell**, click to expand the **Continuity** section.
- 3 From the **Preserve continuity of normals over symmetry boundaries** list, choose **User defined**.
- 4 Click to expand the **Preserve Continuity of Normals over Symmetry Boundaries** section. From the **Selection** list, choose **Symmetry Edge**.
- 5 Locate the **Control Variable Settings** section. From the  $d_{\text{max}}$  list, choose **Box**.
- 6 In the text field, type Lmax.
- 7 Locate the **Filtering** section. From the  $R_{\text{min}}$  list, choose **Small**.

The optimization can sometimes find a bad local minimum when started with zeros for the initial controls. In this case the problem can be avoided by setting nonzero initial values.


8 Click to expand the **Control Variable Initial Value** section. Specify the  $\mathbf{d}_0$  vector as

$\sin((Yg-Xg)/1[m]) * \cos(2*Zg/0.25[m]) * Lmax$	X
$\sin((Yg-Xg)/1[m]) * \cos(2*Zg/0.25[m]) * Lmax$	Y
0	Z

#### *Fixed Edge 1*

- 1 In the **Shape Optimization** toolbar, click  **Fixed Edge**.
- 2 In the **Settings** window for **Fixed Edge**, locate the **Edge Selection** section.
- 3 From the **Selection** list, choose **Exterior Edges**.

#### *Symmetry/Roller 1*

- 1 In the **Shape Optimization** toolbar, click  **Symmetry/Roller**.
- 2 In the **Settings** window for **Symmetry/Roller**, locate the **Geometric Entity Selection** section.
- 3 From the **Geometric entity level** list, choose **Edge**.
- 4 Select Edge 6 only.
- 5 Locate the **Prescribed Normal Vector** section. Specify the  $\mathbf{n}$  vector as

0	X
1	Y
0	Z



#### *Symmetry/Roller 2*


- 1 Right-click **Symmetry/Roller 1** and choose **Duplicate**.
- 2 In the **Settings** window for **Symmetry/Roller**, locate the **Geometric Entity Selection** section.
- 3 From the **Selection** list, choose **Symmetry Edge**.
- 4 In the **Model Builder** window, click **Symmetry/Roller 2**.
- 5 Locate the **Prescribed Normal Vector** section. Specify the  $\mathbf{n}$  vector as

0	X
0	Y
1	Z


## STUDY I

### Step 1: Stationary

- 1 In the **Model Builder** window, under **Study I** click **Step 1: Stationary**.
- 2 In the **Settings** window for **Stationary**, locate the **Study Settings** section.
- 3 Select the **Include geometric nonlinearity** checkbox.
- 4 Locate the **Physics and Variables Selection** section. Select the **Modify model configuration for study step** checkbox.
- 5 In the tree, select **Component 1 (comp1) > Shape Optimization, Controls material frame**.
- 6 Click  **Disable in Solvers**.
- 7 Click  **Control Frame Deformation**.

The initial design has low stiffness, so the problem becomes highly nonlinear. Use continuation in the load to make a continuous transition from the linear regime.
- 8 Click to expand the **Study Extensions** section. Select the **Auxiliary sweep** checkbox.
- 9 Click  **Add**.
- 10 In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
Fload (Load)	0.1 10	kN


- 11 In the **Model Builder** window, click **Study I**.
- 12 In the **Settings** window for **Study**, type Study 1: Initial Design in the **Label** text field.
- 13 In the **Study** toolbar, click  **Compute**.

## RESULTS

### Shape Optimization

In the **Model Builder** window, under **Results** right-click **Shape Optimization** and choose **Delete**.


## ADD STUDY

- 1 In the **Home** toolbar, click  **Add Study** to open the **Add Study** window.
- 2 Go to the **Add Study** window.
- 3 Find the **Studies** subsection. In the **Select Study** tree, select **General Studies > Stationary**.
- 4 Click the **Add Study** button in the window toolbar.

5 In the **Home** toolbar, click  **Add Study** to close the **Add Study** window.

## STUDY 2



### Step 1: Stationary

- 1 In the **Settings** window for **Stationary**, locate the **Study Settings** section.
- 2 Select the **Include geometric nonlinearity** checkbox.
- 3 Click to expand the **Study Extensions** section. Select the **Auxiliary sweep** checkbox.
- 4 Click  **Add**.
- 5 In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
Fload (Load)	0.1 10	kN

- 6 In the **Model Builder** window, click **Study 2**.
- 7 In the **Settings** window for **Study**, type Study 2: Shape Optimization in the **Label** text field.

### Shape Optimization

- 1 In the **Study** toolbar, click  **Optimization** and choose **Shape Optimization**.
- 2 In the **Settings** window for **Shape Optimization**, locate the **Optimization Solver** section.
- 3 Clear the **Move limits** checkbox.
- 4 In the **Maximum number of iterations** text field, type 25.
- 5 Click **Add Expression** in the upper-right corner of the **Objective Function** section. From the menu, choose **Component 1 (comp1) > Shell > Global > comp1.shell.Ws\_tot - Total elastic strain energy - J**.  
Scale the objective with the initial value.
- 6 Locate the **Objective Function** section. From the **Solution** list, choose **Use last**.
- 7 Find the **Objective settings** subsection. From the **Objective scaling** list, choose **Initial solution based**.
- 8 In the **Study** toolbar, click  **Get Initial Value**.

## RESULTS

### Mirror 3D 1

- 1 In the **Model Builder** window, expand the **Results > Datasets** node.
- 2 Right-click **Results > Datasets** and choose **More 3D Datasets > Mirror 3D**.

- 3 In the **Settings** window for **Mirror 3D**, locate the **Plane Data** section.
- 4 From the **Plane** list, choose **XY-planes**.
- 5 Locate the **Data** section. From the **Dataset** list, choose **Study 2: Shape Optimization/ Solution 2 (sol2)**.

#### *Shape Optimization*

- 1 In the **Model Builder** window, under **Results** click **Shape Optimization**.
- 2 In the **Settings** window for **3D Plot Group**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Mirror 3D 1**.

### **STUDY 2: SHAPE OPTIMIZATION**


#### *Solver Configurations*

In the **Model Builder** window, expand the **Study 2: Shape Optimization > Solver Configurations** node.

#### *Solution 2 (sol2)*

- 1 In the **Model Builder** window, expand the **Study 2: Shape Optimization > Solver Configurations > Solution 2 (sol2) > Optimization Solver 1 > Stationary Solver 1 > Segregated 1** node, then click **Shell**.
- 2 In the **Settings** window for **Segregated Step**, click to expand the **Method and Termination** section.
- 3 From the **Termination technique** list, choose **Tolerance** to reduce the computational time further.

#### *Shape Optimization*

- 1 In the **Model Builder** window, under **Study 2: Shape Optimization** click **Shape Optimization**.
- 2 In the **Settings** window for **Shape Optimization**, click to expand the **Output** section.
- 3 Select the **Plot** checkbox.
- 4 From the **Plot group** list, choose **Shape Optimization**.
- 5 In the **Study** toolbar, click  **Compute**.

### **RESULTS**

#### *Stress, Initial Design*

- 1 In the **Model Builder** window, under **Results** click **Stress (shell)**.

- 2 In the **Settings** window for **3D Plot Group**, type Stress, Initial Design in the **Label** text field.

*Stress, Optimized Design*

- 1 In the **Model Builder** window, under **Results** click **Stress (shell) 1**.
- 2 In the **Settings** window for **3D Plot Group**, type Stress, Optimized Design in the **Label** text field.

*Shape Optimization*

- 1 In the **Model Builder** window, click **Shape Optimization**.
- 2 In the **Settings** window for **3D Plot Group**, type Shape Optimization in the **Label** text field.