



Model created in COMSOL Multiphysics 6.4

# Plastic Deformation During the Expansion of a Biomedical Stent

## Introduction

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Percutaneous transluminal angioplasty with stenting is a widely spread method for the treatment of atherosclerosis. During the procedure, a stent is deployed into the artery by using a balloon as an expander. Once the balloon-stent package is in place, the balloon is inflated to expand the stent. The balloon is then deflated and removed, but the stent remains expanded to act as a scaffold, keeping the blood vessel open.

Stent design is of significance for this procedure, since serious damage can be inflicted to the artery during the expansion procedure. One of the most common defect is the nonuniform deformation of the stent, where the ends expand more than the middle section, phenomenon which is also called *dogboning*. Foreshortening of the stent can also damage the artery, and it could make the positioning difficult.

The dogboning is defined according to

$$\text{dogboning} = \frac{r_{\text{distal}} - r_{\text{central}}}{r_{\text{distal}}}$$

where  $r_{\text{distal}}$  and  $r_{\text{central}}$  are the radii at the end and middle of the stent, respectively.

The foreshortening is defined as

$$\text{foreshortening} = \frac{L_0 - L_{\text{load}}}{L_0}$$

here,  $L_0$  is the original length of the stent and  $L_{\text{load}}$  is the deformed length of the stent.

Other common parameters in stent design are the longitudinal and radial recoil. These parameters give information on the stent behavior when removing the inflated balloon.

The longitudinal recoil is defined as

$$L_{\text{recoil}} = \frac{L_{\text{load}} - L_{\text{unload}}}{L_{\text{load}}}$$

here,  $L_{\text{unload}}$  is the length of the stent once the balloon is removed, and  $L_{\text{load}}$  is the length of the stent when the balloon is fully inflated.

The radial recoil can be defined as follow

$$R_{\text{recoil}} = \frac{R_{\text{load}} - R_{\text{unload}}}{R_{\text{load}}}$$

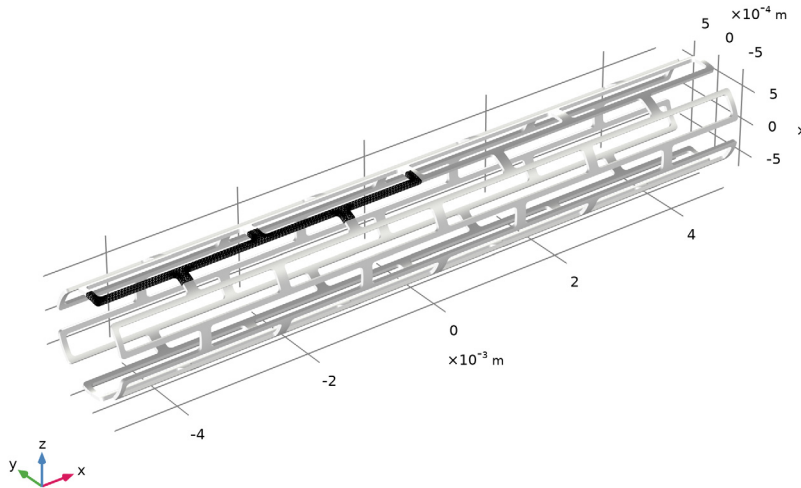
here,  $R_{\text{unload}}$  is the radius of the stent once the balloon is removed, and  $R_{\text{load}}$  is the radius of the stent when the balloon is fully inflated.

To check the viability of a stent design, you can study the deformation process under the influence of the radial pressure that expands the stent. With this example you can both monitor the dogboning and foreshortening effects, and draw conclusions on how to change the geometry design parameters for optimum performance.

### *Model Definition*

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The model studies the Palmaz–Schatz stent model. Due to the stent’s circumferential and longitudinal symmetry, it is possible to model only one twenty-fourth of the geometry. [Figure 1](#) shows the geometry used in the study, represented with the meshed domain.



*Figure 1: The reduced geometry used in the study (meshed) and the full stent geometry.*

The main focus of the study consists in the stress evaluation in the stent. The angioplasty balloon is assumed to stretch with a maximum expansion radius of 2 mm.

## MATERIAL

The stent is made of stainless steel. The material parameters are given in the following table.

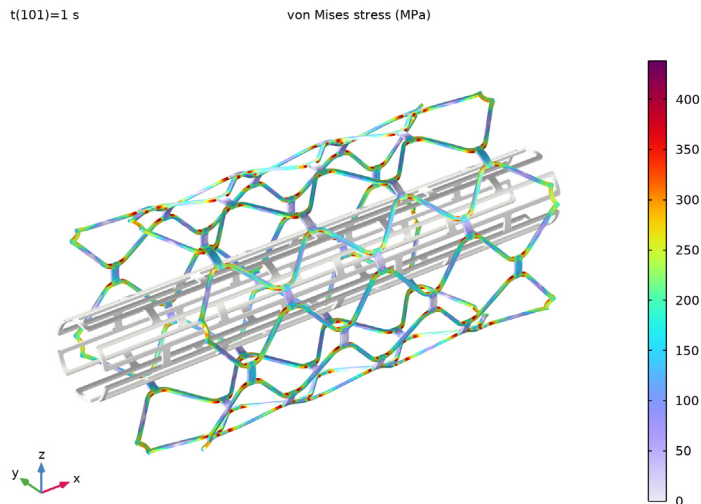
MATERIAL PROPERTY	VALUE
Young's modulus	193 [GPa]
Poisson's ratio	0.27
Initial yield stress	207 [MPa]
Isotropic tangent modulus	692 [MPa]

## LOADS

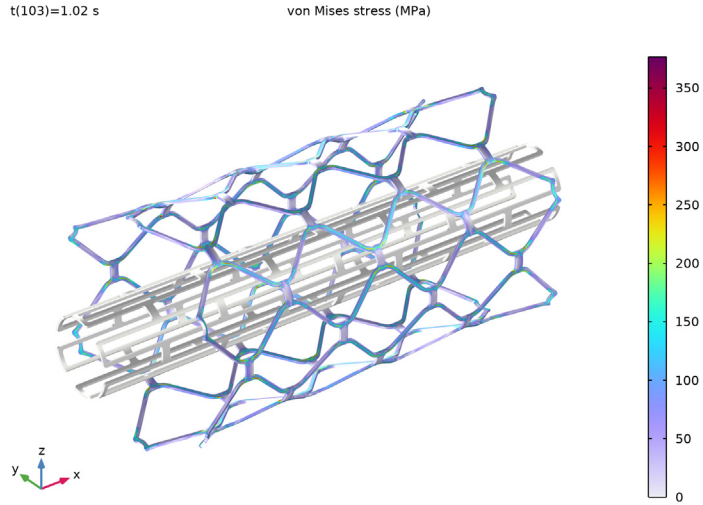
Apply a radial outward pressure on the inner surface of the stent to represent the balloon expansion.

## Results and Discussion

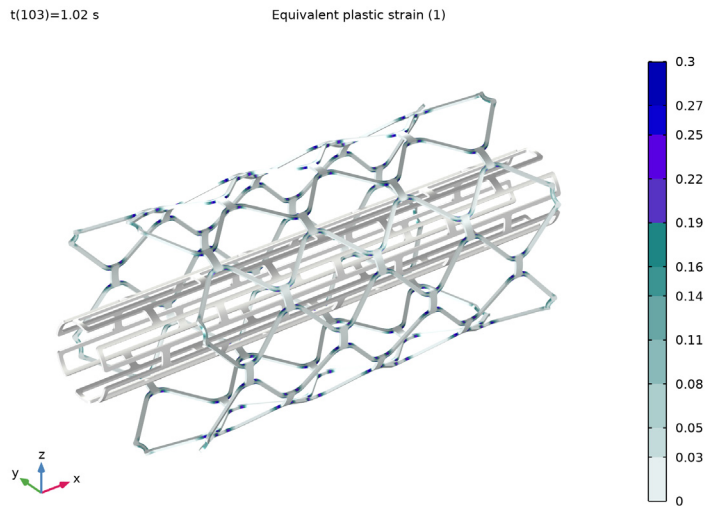
The stent is expanded from an original diameter of 0.74 mm to a diameter of 2 mm in the middle section. [Figure 2](#) shows the stress distribution at maximum balloon inflation, and [Figure 3](#) shows the residual stress after the balloon deflation. After the deflation, irreversible deformation can be observed as shown in [Figure 4](#).



*Figure 2: Maximum stress in the stent during the balloon inflation.*

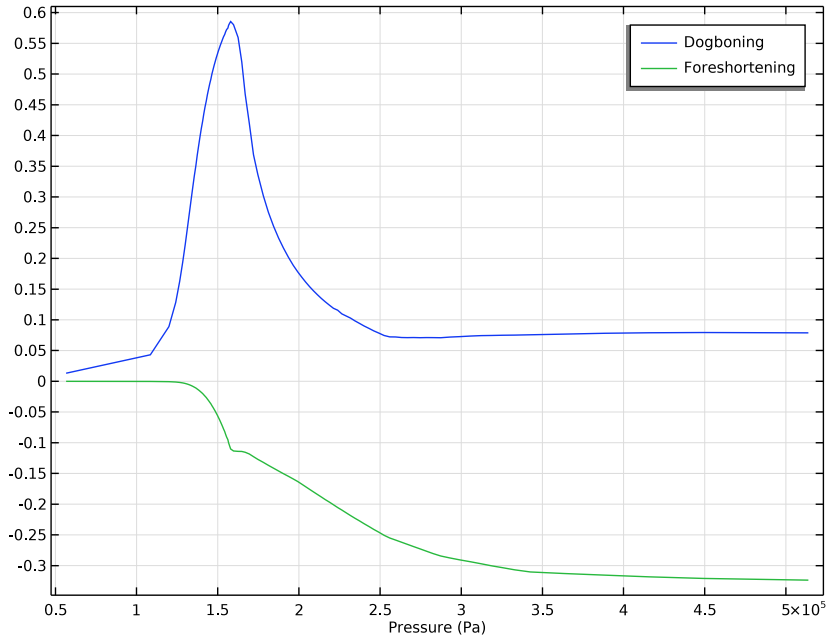


*Figure 3: Residual stress in the stent after deflation of the balloon.*



*Figure 4: Equivalent plastic strain in the stent after deflation of the balloon.*

In [Figure 5](#), you can see the evolution of the dogboning and foreshortening effects with respect to the pressure during the inflation of the balloon. The longitudinal recoil is about  $-0.9\%$ , the distal radial recoil is about  $0.4\%$ , and the central radial recoil is about  $0.7\%$ .



*Figure 5: Stent dogboning (blue) and foreshortening (green) versus pressure inside the angioplasty balloon.*

### *Notes About the COMSOL Implementation*

The maximum radius of the angioplasty balloon is represented with a step function, the pressure is applied as long as the inner radius of the stent is smaller than the maximum balloon radius. Above this limit the pressure is set to zero.

For a highly nonlinear problem like this, the choice of the continuation parameter can improve the convergence during the computation of the solution. A displacement control parameter is usually better than a load parameter. In this example, the average displacement of the stent's inner radius is prescribed, and a **Global Equation** is used to compute the corresponding applied pressure load.

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**Application Library path:** Nonlinear\_Structural\_Materials\_Module/  
Plasticity/biomedical\_stent


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### *Modeling Instructions*




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From the **File** menu, choose **New**.

#### **NEW**





In the **New** window, click  **Model Wizard**.

#### **MODEL WIZARD**

- 1 In the **Model Wizard** window, click  **3D**.
- 2 In the **Select Physics** tree, select **Structural Mechanics > Solid Mechanics (solid)**.
- 3 Click **Add**.
- 4 Click  **Study**.
- 5 In the **Select Study** tree, select **General Studies > Stationary**.
- 6 Click  **Done**.

#### **GEOMETRY 1**

##### *Import 1 (impl)*

- 1 In the **Geometry** toolbar, click  **Import**.
- 2 In the **Settings** window for **Import**, locate the **Source** section.
- 3 From the **Source** list, choose **COMSOL Multiphysics file**.
- 4 Click  **Browse**.
- 5 Browse to the model's Application Libraries folder and double-click the file `biomedical_stent.mphbin`.
- 6 Click  **Import**.
- 7 Click the  **Zoom Extents** button in the **Graphics** toolbar.

#### **SOLID MECHANICS (SOLID)**

##### *Linear Elastic Material 1*

Use a large strain formulation and add **Plasticity** to consider the nonlinear material behavior of the stent.

- 1 In the **Model Builder** window, under **Component 1 (comp1) > Solid Mechanics (solid)** click **Linear Elastic Material 1**.
- 2 In the **Settings** window for **Linear Elastic Material**, locate the **Geometric Nonlinearity** section.
- 3 From the **Formulation** list, choose **Total Lagrangian**.

#### *Plasticity 1*

In the **Physics** toolbar, click  **Attributes** and choose **Plasticity**.

### **MATERIALS**

#### *Material 1 (mat1)*

- 1 In the **Model Builder** window, under **Component 1 (comp1)** right-click **Materials** and choose **Blank Material**.
- 2 In the **Settings** window for **Material**, locate the **Material Contents** section.
- 3 In the table, enter the following settings:


Property	Variable	Value	Unit	Property group
Young's modulus	E	193 [GPa]	Pa	Young's modulus and Poisson's ratio
Poisson's ratio	nu	0.27	l	Young's modulus and Poisson's ratio
Density	rho	7050	kg/m <sup>3</sup>	Basic
Initial yield stress	sigmags	207 [MPa]	Pa	Elastoplastic material model
Isotropic tangent modulus	Et	692 [MPa]	Pa	Elastoplastic material model

Choose the steel material type to improve the visualization of the stent during postprocessing.

- 4 Click to expand the **Appearance** section. From the **Material type** list, choose **Steel**.


### **DEFINITIONS**

#### *Step 1 (step1)*

- 1 In the **Definitions** toolbar, click  **More Functions** and choose **Step**.
- 2 In the **Settings** window for **Step**, locate the **Parameters** section.
- 3 In the **Location** text field, type 2[mm].


- 4 In the **From** text field, type 1.
- 5 In the **To** text field, type 0.
- 6 Click to expand the **Smoothing** section. In the **Size of transition zone** text field, type 1e-5.

*Variables 1*


- 1 In the **Definitions** toolbar, click  **Local Variables**.
- 2 In the **Settings** window for **Variables**, locate the **Variables** section.
- 3 In the table, enter the following settings:

Name	Expression	Unit	Description
r	$\sqrt{y^2+z^2}$	m	Radial distance from x-axis


*Average 1 (aveop1)*

- 1 In the **Definitions** toolbar, click  **Nonlocal Couplings** and choose **Average**.
- 2 In the **Settings** window for **Average**, locate the **Source Selection** section.
- 3 From the **Geometric entity level** list, choose **Edge**.
- 4 Select Edge 28 only.
- 5 Locate the **Advanced** section. From the **Frame** list, choose **Material (X, Y, Z)**.

*Piecewise 1 (pw1)*

- 1 In the **Definitions** toolbar, click  **Piecewise**.
- 2 In the **Settings** window for **Piecewise**, type r0 in the **Function name** text field.
- 3 Locate the **Definition** section. In the **Argument** text field, type t.
- 4 Find the **Intervals** subsection. In the table, enter the following settings:

Start	End	Function
0	1	$(2e-3-7.1e-4)*t+7.1e-4$
1	2	$(2e-3-7.1e-4)*(1-t)+2e-3$

- 5 Locate the **Units** section. In the **Arguments** text field, type s.
- 6 In the **Function** text field, type m.
- 7 Click  **Plot**.



**SOLID MECHANICS (SOLID)**

*Symmetry 1*


- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Symmetry**.

2 Select Boundaries 5, 12, 18, 24, 30, and 31 only.



#### Boundary Load I

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Boundary Load**.
- 2 Select Boundary 4 only.
- 3 In the **Settings** window for **Boundary Load**, locate the **Force** section.
- 4 From the **Load type** list, choose **Pressure**.
- 5 In the  $p$  text field, type  $p \cdot \text{step1}(r)$ .
- 6 Click the  **Show More Options** button in the **Model Builder** toolbar.
- 7 In the **Show More Options** dialog, in the tree, select the checkbox for the node **Physics > Equation Contributions**.
- 8 Click **OK**.

#### Global Equations I (ODEI)

- 1 In the **Physics** toolbar, click  **Global** and choose **Global Equations**.
- 2 In the **Settings** window for **Global Equations**, locate the **Global Equations** section.
- 3 In the table, enter the following settings:

Name	$f(u, ut, utt, t)$ (I)	Initial value ( $u_0$ ) (I)	Initial value ( $ut_0$ ) (I/s)	Description
$p$	$\text{aveop1}(r) - r0(t)$	0	0	Pressure

- 4 Locate the **Units** section. Click  **Select Dependent Variable Quantity**.
- 5 In the **Physical Quantity** dialog, type **pressure** in the text field.
- 6 In the tree, select **General > Pressure (Pa)**.
- 7 Click **OK**.
- 8 In the **Settings** window for **Global Equations**, locate the **Units** section.
- 9 Click  **Select Source Term Quantity**.
- 10 In the **Physical Quantity** dialog, type **length** in the text field.
- 11 In the tree, select **General > Length (m)**.
- 12 Click **OK**.

#### MESH I

##### Free Triangular I


- 1 In the **Mesh** toolbar, click  **More Generators** and choose **Free Triangular**.

2 Select Boundary 3 only.


#### *Size 1*

- 1 Right-click **Free Triangular 1** and choose **Size**.
- 2 In the **Settings** window for **Size**, locate the **Element Size** section.
- 3 Click the **Custom** button.
- 4 Locate the **Element Size Parameters** section.
- 5 Select the **Maximum element size** checkbox. In the associated text field, type  $4.5e-5$ .
- 6 Select the **Minimum element size** checkbox. In the associated text field, type  $4e-6$ .
- 7 Select the **Maximum element growth rate** checkbox. In the associated text field, type 1.4.
- 8 Select the **Curvature factor** checkbox. In the associated text field, type 0.3.

#### *Swept 1*

In the **Mesh** toolbar, click  **Swept**.


#### *Distribution 1*

- 1 Right-click **Swept 1** and choose **Distribution**.
- 2 In the **Settings** window for **Distribution**, locate the **Distribution** section.
- 3 In the **Number of elements** text field, type 2.
- 4 Click  **Build All**.


### **DEFINITIONS**

Create variables for the results processing.

#### *Integration 1 (intop1)*

- 1 In the **Definitions** toolbar, click  **Nonlocal Couplings** and choose **Integration**.
- 2 In the **Settings** window for **Integration**, locate the **Source Selection** section.
- 3 From the **Geometric entity level** list, choose **Point**.
- 4 Select Point 57 only.
- 5 In the **Operator name** text field, type central.
- 6 Locate the **Advanced** section. From the **Frame** list, choose **Material (X, Y, Z)**.

#### *Integration 2 (intop2)*

- 1 In the **Definitions** toolbar, click  **Nonlocal Couplings** and choose **Integration**.
- 2 In the **Settings** window for **Integration**, locate the **Source Selection** section.
- 3 From the **Geometric entity level** list, choose **Point**.

- 4 Select Point 3 only.
- 5 In the **Operator name** text field, type `distal`.
- 6 Locate the **Advanced** section. From the **Frame** list, choose **Material (X, Y, Z)**.

#### *Variables I*

- 1 In the **Model Builder** window, click **Variables I**.
- 2 In the **Settings** window for **Variables**, locate the **Variables** section.
- 3 In the table, enter the following settings:

Name	Expression	Unit	Description
dogboning	$(\text{distal}(r) - \text{central}(r)) / \text{distal}(r)$		Dogboning
length	$2 * \text{abs}(\text{distal}(x) - \text{central}(x))$	m	Length of the deformed stent
L0	$2 * \text{abs}(\text{distal}(X) - \text{central}(X))$	m	Length of the undeformed stent
foreshortening	$(\text{length} - L0) / \text{length}$		Foreshortening

### **GLOBAL DEFINITIONS**

#### *Parameters I*

- 1 In the **Model Builder** window, under **Global Definitions** click **Parameters I**.
- 2 In the **Settings** window for **Parameters**, locate the **Parameters** section.
- 3 In the table, enter the following settings:

Name	Expression	Value	Description
t	0[s]	0 s	Time

### **STUDY I**

#### *Step 1: Stationary*



Set up an auxiliary continuation sweep for the t parameter.

- 1 In the **Model Builder** window, under **Study I** click **Step 1: Stationary**.
- 2 In the **Settings** window for **Stationary**, click to expand the **Study Extensions** section.
- 3 Select the **Auxiliary sweep** checkbox.
- 4 Click **+ Add**.

5 In the table, enter the following settings:


Parameter name	Parameter value list	Parameter unit
t (Time)	range(0, 1e-2, 1.5)	s

#### *Solution 1 (sol1)*


- 1 In the **Study** toolbar, click  **Show Default Solver**.
- 2 In the **Model Builder** window, expand the **Solution 1 (sol1)** node.
- 3 In the **Model Builder** window, expand the **Study 1 > Solver Configurations > Solution 1 (sol1) > Dependent Variables 1** node, then click **Global Equations 1 (comp1.ODE1)**.
- 4 In the **Settings** window for **State**, locate the **Scaling** section.
- 5 From the **Method** list, choose **Manual**.
- 6 In the **Scale** text field, type 1e6.  
Add a stop condition to prevent the computed pressure from becoming negative.
- 7 In the **Model Builder** window, expand the **Study 1 > Solver Configurations > Solution 1 (sol1) > Stationary Solver 1** node.
- 8 Right-click **Study 1 > Solver Configurations > Solution 1 (sol1) > Stationary Solver 1 > Parametric 1** and choose **Stop Condition**.
- 9 In the **Settings** window for **Stop Condition**, locate the **Stop Expressions** section.
- 10 Click  **Add**.
- 11 In the table, enter the following settings:

Stop expression	Stop if	Active	Description
comp1.p<0	True (>=1)	<input checked="" type="checkbox"/>	Stop expression 1

Specify that the solution is to be stored just before the stop condition is reached.

- 12 Locate the **Output at Stop** section. From the **Add solution** list, choose **Step before stop**.
- 13 In the **Study** toolbar, click  **Compute**.

#### **RESULT TEMPLATES**

- 1 In the **Results** toolbar, click  **Result Templates** to open the **Result Templates** window.
- 2 Go to the **Result Templates** window.
- 3 In the tree, select **Study 1/Solution 1 (sol1) > Solid Mechanics > Equivalent Plastic Strain (solid)**.
- 4 Click the **Add Result Template** button in the window toolbar.

5 In the **Results** toolbar, click  **Result Templates** to close the **Result Templates** window.


## RESULTS

Use mirror 3D and sector 3D datasets to display the solution on the full geometry.


### *Mirror 3D 1*

- 1 In the **Model Builder** window, expand the **Results > Datasets** node.
- 2 Right-click **Results > Datasets** and choose **More 3D Datasets > Mirror 3D**.

### *Mirror 3D 2*

- 1 In the **Results** toolbar, click  **More Datasets** and choose **Mirror 3D**.
- 2 In the **Settings** window for **Mirror 3D**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Mirror 3D 1**.
- 4 Locate the **Plane Data** section. From the **Plane** list, choose **zx-planes**.

### *Sector 3D 1*

- 1 In the **Results** toolbar, click  **More Datasets** and choose **Sector 3D**.
- 2 In the **Settings** window for **Sector 3D**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Mirror 3D 2**.
- 4 Locate the **Axis Data** section. In row **Point 2**, set **x** to 1 and **z** to 0.
- 5 Locate the **Symmetry** section. In the **Number of sectors** text field, type 6.

### *Stress (solid)*

- 1 In the **Model Builder** window, under **Results** click **Stress (solid)**.
- 2 In the **Settings** window for **3D Plot Group**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Sector 3D 1**.
- 4 Locate the **Plot Settings** section. Clear the **Plot dataset edges** checkbox.

### *Volume 1*

- 1 In the **Model Builder** window, expand the **Stress (solid)** node, then click **Volume 1**.
- 2 In the **Settings** window for **Volume**, locate the **Expression** section.
- 3 From the **Unit** list, choose **MPa**.


Use a **Surface Plot** with a **Material Appearance** subnode to visualize the stent in its original state.

### *Surface 1*



- 1 In the **Model Builder** window, right-click **Stress (solid)** and choose **Surface**.

- 2 In the **Settings** window for **Surface**, click to expand the **Title** section.
- 3 From the **Title type** list, choose **None**.

#### *Material Appearance 1*

- 1 Right-click **Surface 1** and choose **Material Appearance**.
- 2 In the **Stress (solid)** toolbar, click  **Plot**.

#### *Stress (solid)*

- 1 In the **Model Builder** window, under **Results** click **Stress (solid)**.
- 2 In the **Settings** window for **3D Plot Group**, click  **Plot Previous** twice to plot the maximum stress.
- 3 In the **Stress (solid)** toolbar, click  **Plot**.

#### *Equivalent Plastic Strain (solid)*

- 1 In the **Model Builder** window, click **Equivalent Plastic Strain (solid)**.
- 2 In the **Settings** window for **3D Plot Group**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Sector 3D 1**.
- 4 Locate the **Plot Settings** section. Clear the **Plot dataset edges** checkbox.

#### *Surface 2*

- 1 In the **Model Builder** window, expand the **Equivalent Plastic Strain (solid)** node.
- 2 Right-click **Results > Equivalent Plastic Strain (solid) > Surface 1** and choose **Duplicate**.


#### *Deformation 1*

- 1 Right-click **Surface 1** and choose **Deformation**.
- 2 In the **Settings** window for **Deformation**, locate the **Scale** section.
- 3 Select the **Scale factor** checkbox. In the associated text field, type 1.


#### *Surface 2*

- 1 In the **Model Builder** window, under **Results > Equivalent Plastic Strain (solid)** click **Surface 2**.
- 2 In the **Settings** window for **Surface**, locate the **Title** section.
- 3 From the **Title type** list, choose **None**.


#### *Material Appearance 1*

- 1 Right-click **Surface 2** and choose **Material Appearance**.
- 2 In the **Equivalent Plastic Strain (solid)** toolbar, click  **Plot**.


### *Dogboning and Foreshortening*

- 1 In the **Results** toolbar, click  **ID Plot Group**.
- 2 In the **Settings** window for **ID Plot Group**, type Dogboning and Foreshortening in the **Label** text field.
- 3 Locate the **Data** section. From the **Time selection** list, choose **From list**.
- 4 In the parameter values list, select all solution steps between 0 and 1.

### *Global I*

- 1 Right-click **Dogboning and Foreshortening** and choose **Global**.
- 2 In the **Settings** window for **Global**, click **Replace Expression** in the upper-right corner of the **y-Axis Data** section. From the menu, choose **Component I (comp1) > Definitions > Variables > dogboning - Dogboning - I**.
- 3 Click **Add Expression** in the upper-right corner of the **y-Axis Data** section. From the menu, choose **Component I (comp1) > Definitions > Variables > foreshortening - Foreshortening - I**.
- 4 Click **Replace Expression** in the upper-right corner of the **x-Axis Data** section. From the menu, choose **Component I (comp1) > Solid Mechanics > p - Pressure - Pa**.
- 5 In the **Dogboning and Foreshortening** toolbar, click  **Plot**.  
Evaluate the longitudinal recoil, the distal radial recoil, and the central radial recoil using the **Evaluation Group**.  
Click on the checkbox in the Results node to enable automatic reevaluation of evaluation groups when the model is resolved.
- 6 In the **Model Builder** window, click **Results**.
- 7 In the **Settings** window for **Results**, locate the **Update of Results** section.
- 8 Select the **Reevaluate all evaluation groups after solving** checkbox.

### *Recoil Evaluation*


- 1 In the **Results** toolbar, click  **Evaluation Group**.
- 2 In the **Settings** window for **Evaluation Group**, type Recoil Evaluation in the **Label** text field.
- 3 Locate the **Data** section. From the **Time selection** list, choose **From list**.
- 4 In the **Parameter values (t (s))** list box, select **I**.

### *Global Evaluation I*

- 1 Right-click **Recoil Evaluation** and choose **Global Evaluation**.
- 2 In the **Settings** window for **Global Evaluation**, locate the **Expressions** section.


3 In the table, enter the following settings:

Expression	Unit	Description
$(\text{length-with}(103, \text{length})) / \text{length}$	1	Longitudinal recoil
$(\text{distal}(r) - \text{with}(103, \text{distal}(r))) / \text{distal}(r)$	1	Distal radial recoil
$(\text{central}(r) - \text{with}(103, \text{central}(r))) / \text{central}(r)$	1	Central radial recoil

4 In the **Recoil Evaluation** toolbar, click  **Evaluate**.

The steps below illustrate how to display the geometry as in [Figure 1](#).

#### *Full Geometry and Mesh*

- 1 In the **Results** toolbar, click  **3D Plot Group**.
- 2 In the **Settings** window for **3D Plot Group**, type Full Geometry and Mesh in the **Label** text field.
- 3 Click to expand the **Title** section. From the **Title type** list, choose **None**.


#### *Surface I*

- 1 Right-click **Full Geometry and Mesh** and choose **Surface**.
- 2 In the **Settings** window for **Surface**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Sector 3D I**.

#### *Material Appearance I*

Right-click **Surface I** and choose **Material Appearance**.

#### *Mesh I*

- 1 In the **Model Builder** window, right-click **Full Geometry and Mesh** and choose **Mesh**.
- 2 In the **Settings** window for **Mesh**, locate the **Coloring and Style** section.
- 3 From the **Element color** list, choose **None**.
- 4 In the **Full Geometry and Mesh** toolbar, click  **Plot**.