



Model created in COMSOL Multiphysics 6.4

# Water and Carbon Dioxide Co-Electrolysis in a Solid Oxide Electrolyzer Cell

## *Introduction*

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In this tutorial, a solid oxide electrolyzer cell model for co-electrolysis of H<sub>2</sub>O and CO<sub>2</sub> is presented. The model includes the full coupling between the mass balances and gas flow in the H<sub>2</sub> and O<sub>2</sub> gas diffusion electrodes, the momentum balances in the H<sub>2</sub> and O<sub>2</sub> gas-flow channels, the energy balance across the cell, the balance of the ionic current carried by the oxide ion, and an electronic-current balance. A reversible water–gas shift reaction is included in the H<sub>2</sub> gas-diffusion electrode and the H<sub>2</sub> gas-flow channel.

The model computes the spatial distributions of the various species across the gas-diffusion electrodes and gas-flow channels. The spatial distribution of the total current density along the electrode length is also evaluated using a general projection operator.

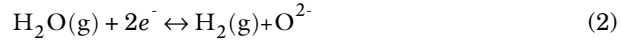
## *Model Definition*

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On the anode, oxygen ions are oxidized to form oxygen gas,



whereas on the cathode, water vapor is reduced to form hydrogen gas and oxygen ions:



A CO<sub>2</sub> electrolysis reaction also occurs on the cathode, where CO<sub>2</sub> gas is reduced to form CO gas and oxygen ions:

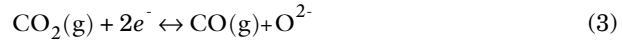


Figure 1 shows the model geometry. Seven computational domains are used in the model: the two interconnects, H<sub>2</sub> and O<sub>2</sub> gas-flow channels, H<sub>2</sub> and O<sub>2</sub> gas-diffusion electrodes, and the membrane.

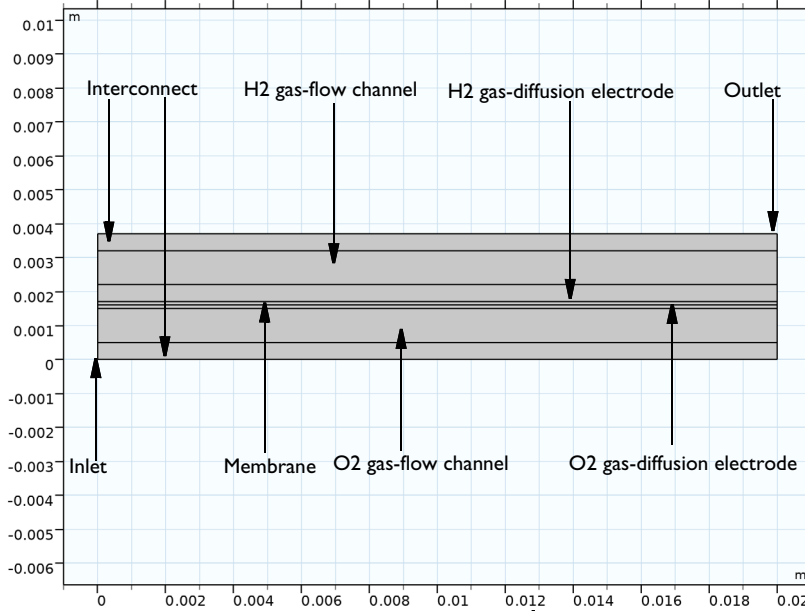


Figure 1: Model geometry. From top: Interconnect, H<sub>2</sub> gas channel, H<sub>2</sub> gas-diffusion electrode, solid oxide electrolyte layer, O<sub>2</sub> gas-diffusion electrode, O<sub>2</sub> gas-flow channel, and interconnect. The inlet and outlet positions are indicated in the figure.

The gas mixture at the cathode consists of H<sub>2</sub>, H<sub>2</sub>O, CO<sub>2</sub>, and CO, whereas that at the anode consists of O<sub>2</sub> and N<sub>2</sub>. The composition of the gas mixture will change as a result of the electrochemical reactions and the water–gas shift reaction. The mass transport of the gaseous species is modeled in the gas-flow channels and the gas-diffusion electrodes coupled to the resulting (laminar) flow of the gas mixture.

The current distribution is defined assuming a temperature-dependent electrolyte conductivity of the solid electrolyte. The Water Electrolyzer interface is used to define the electrode reactions and the electrolyte charge transport in the porous gas-diffusion electrodes and the electrolyte layer, as well as the mass transport of the gas mixture. The momentum flow is defined using Darcy’s Law in the gas-flow channels and the gas-diffusion electrodes.

On the cathode side, the electrode kinetics depends on the local concentrations of H<sub>2</sub>O and H<sub>2</sub> for the H<sub>2</sub>O electrolysis reaction and on the local concentrations of CO<sub>2</sub> and CO

for the  $\text{CO}_2$  electrolysis reaction according to the law of mass action (and the Nernst equation). On the anode side, the electrode kinetics depends on the local concentrations of  $\text{O}_2$  for the  $\text{O}_2$  evolution reaction according to the law of mass action (and the Nernst equation).

The properties of the gas mixtures at both anode and cathode, as well as the equilibrium potentials of the electrode reactions are automatically defined by the default built-in options of the Water Electrolyzer interface.

## Results and Discussion

Figure 2 shows the  $\text{H}_2$  concentration distribution in the  $\text{H}_2$  gas-flow channel and the  $\text{H}_2$  gas-diffusion electrode for an applied potential of 1.5 V. The  $\text{H}_2$  concentration is found to increase along the electrode length due to the  $\text{H}_2\text{O}$  electrolysis reaction occurring at the  $\text{H}_2$  gas diffusion electrode.

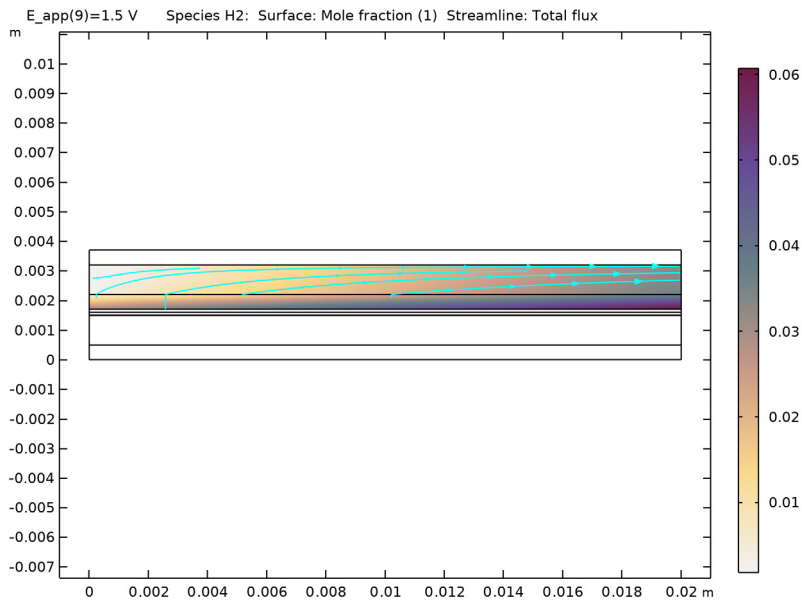
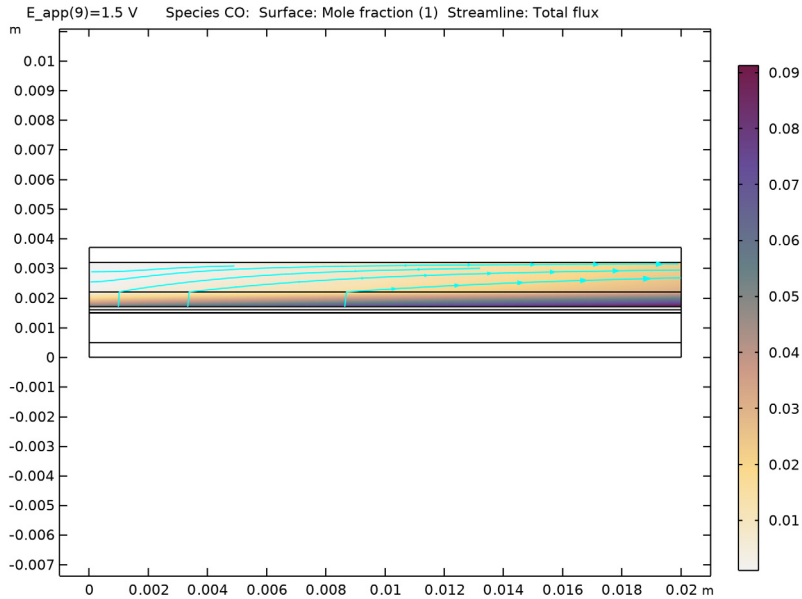


Figure 2:  $\text{H}_2$  concentration distribution in the  $\text{H}_2$  gas-flow channel and  $\text{H}_2$  gas-diffusion electrode for an applied potential of 1.5 V.

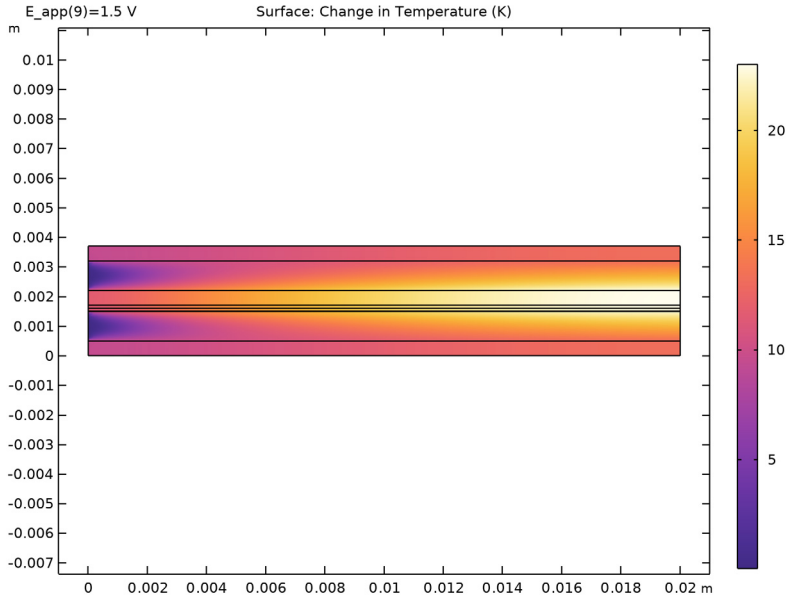
Figure 3 shows the  $\text{CO}$  concentration distribution in the  $\text{H}_2$  gas-flow channel and  $\text{H}_2$  gas diffusion electrode for applied potential of 1.5 V.  $\text{CO}$  concentration is found to increase along the electrode length due to the  $\text{CO}_2$  electrolysis reaction occurring at the  $\text{H}_2$  gas-

diffusion electrode. The difference in the CO concentration between the H<sub>2</sub> gas-diffusion electrode and the H<sub>2</sub> gas-flow channel is considerably higher for CO in the downstream when compared to H<sub>2</sub>. This can be attributed to slower diffusion of CO than H<sub>2</sub>.



*Figure 3: CO concentration distribution in the H<sub>2</sub> gas-flow channel and the H<sub>2</sub> gas-diffusion electrode for an applied potential of 1.5 V.*

Figure 4 shows the change in temperature across a solid oxide electrolyzer cell for an applied potential of 1.5 V. Although both the H<sub>2</sub>O and CO<sub>2</sub> electrolysis reactions are endothermic, the cell temperature is increased by about 25 K from the inlet to the outlet for an applied potential of 1.5 V. As this applied potential is higher than the cell thermoneutral potential, the heat generated from overpotential losses is more than the heat required for electrolysis reactions.



*Figure 4: Change in temperature across a solid oxide electrolyzer cell for an applied potential of 1.5 V.*

Figure 5 shows the distribution of the water-gas shift reaction rate in the  $H_2$  gas-flow channel and the  $H_2$  gas-diffusion electrode for an applied potential of 1.5 V. The water-gas shift reaction rate is found to be higher closer to the  $H_2$  gas-diffusion electrode-

membrane interface for an applied potential of 1.5 V, which is attributed to the high CO concentration in the region.

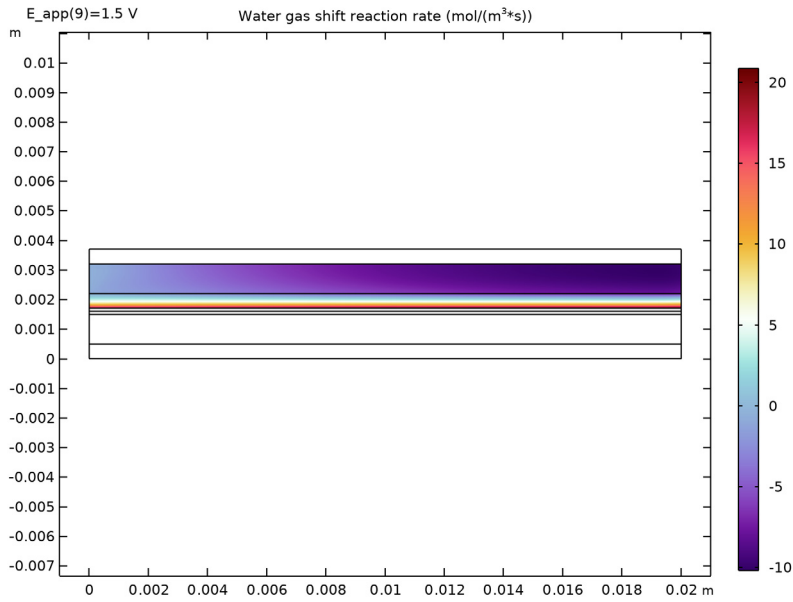


Figure 5: Water-gas shift reaction rate in the  $H_2$  gas-flow channel and the  $H_2$  gas-diffusion electrode for an applied potential of 1.5 V.

Figure 6 shows that the total cathodic (negative) current density, which is integrated along the  $y$  direction for each grid point along the  $x$  direction using a general projection operator, decreases for  $H_2O$  electrolysis and increases for  $CO_2$  electrolysis along the electrode length.

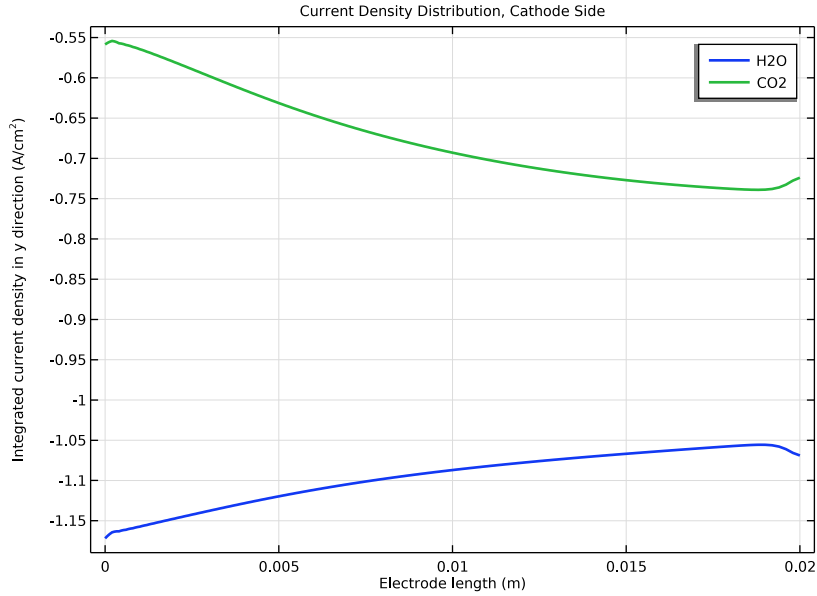


Figure 6: The total cathodic current density for H<sub>2</sub>O and CO<sub>2</sub> electrolysis along the electrode length for an applied potential of 1.5 V.

Finally, Figure 7 shows the average current density as a function of the applied potential (polarization curve).

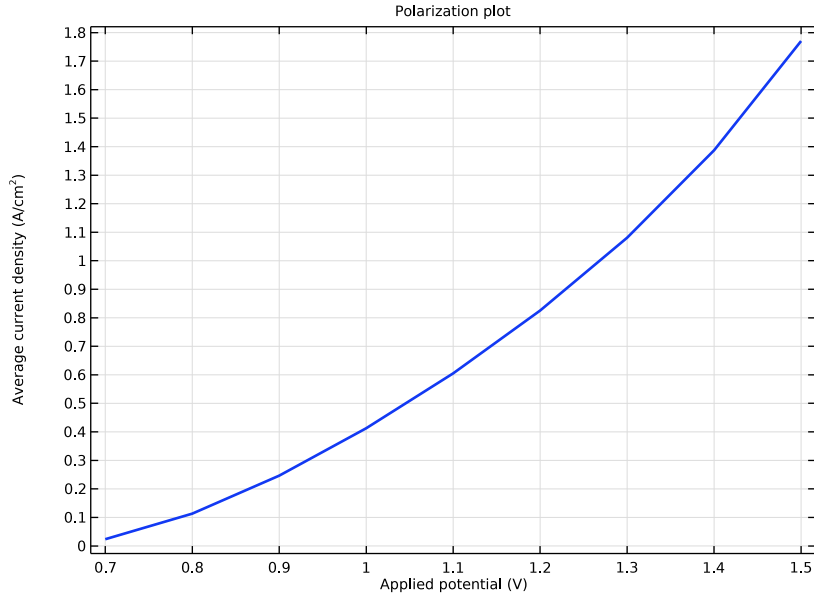


Figure 7: Polarization curve.

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**Application Library path:** Fuel\_Cell\_and\_Electrolyzer\_Module/Electrolyzers/soec\_co2


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### *Modeling Instructions*

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From the **File** menu, choose **New**.

#### **NEW**

In the **New** window, click  **Model Wizard**.

#### **MODEL WIZARD**


- 1** In the **Model Wizard** window, click  **2D**.
- 2** In the **Select Physics** tree, select **Electrochemistry** > **Water Electrolyzers** > **Solid Oxide (we)**.
- 3** Click **Add**.

- 4 In the **Select Physics** tree, select **Heat Transfer > Heat Transfer in Solids and Fluids (ht)**.
- 5 Click **Add**.
- 6 Click  **Study**.
- 7 In the **Select Study** tree, select **Preset Studies for Selected Physics Interfaces > Water Electrolyzer > Stationary with Initialization**.
- 8 Click  **Done**.

## GLOBAL DEFINITIONS

### *Parameters 1*

First load the model parameters.

- 1 In the **Model Builder** window, under **Global Definitions** click **Parameters 1**.
- 2 In the **Settings** window for **Parameters**, locate the **Parameters** section.
- 3 Click  **Load from File**.
- 4 Browse to the model's Application Libraries folder and double-click the file `soec_co2_parameters.txt`.

## GEOMETRY 1

Draw the model geometry using a rectangle and six layers.

- 1 In the **Sketch** toolbar, click **Rectangle** and choose **Rectangle**.

### *Rectangle 1 (r1)*

- 1 In the **Model Builder** window, expand the **Geometry 1** node.
- 2 Right-click **Component 1 (comp1) > Geometry 1** and choose **Rectangle**.
- 3 In the **Settings** window for **Rectangle**, locate the **Size and Shape** section.
- 4 In the **Width** text field, type L.
- 5 In the **Height** text field, type W.
- 6 Click to expand the **Layers** section. In the table, enter the following settings:

Layer name	Thickness (m)
Layer 1	di
Layer 2	dg
Layer 3	da
Layer 4	dm



Layer name	Thickness (m)
Layer 5	dc
Layer 6	dg

7 Click  **Build All Objects**.

## DEFINITIONS

### *Variables 1*

Next, add variables.

- 1 In the **Definitions** toolbar, click  **Local Variables**.
- 2 In the **Settings** window for **Variables**, locate the **Variables** section.
- 3 Click  **Load from File**.
- 4 Browse to the model's Application Libraries folder and double-click the file `soec_co2_variables.txt`.


### *General Projection 1 (genproj1)*

Next, add a **General Projection** coupling.

- 1 In the **Definitions** toolbar, click  **Nonlocal Couplings** and choose **General Projection**.
- 2 Select Domain 5 only.

### *Average 1 (aveop1)*

Add an average operator which will be used later while plotting the polarization plot.

- 1 In the **Definitions** toolbar, click  **Nonlocal Couplings** and choose **Average**.
- 2 In the **Settings** window for **Average**, type `aveop_an` in the **Operator name** text field.
- 3 Locate the **Source Selection** section. From the **Geometric entity level** list, choose **Boundary**.
- 4 Select Boundary 12 only.

## WATER ELECTROLYZER (WE)

Start setting up the electrochemistry part of the model.


- 1 In the **Model Builder** window, under **Component 1 (comp1)** click **Water Electrolyzer (we)**.
- 2 Select Domains 2–6 only.
- 3 In the **Settings** window for **Water Electrolyzer**, locate the **H2 Gas Mixture** section.
- 4 Select the **CO2** checkbox.
- 5 Select the **CO** checkbox.

- 6 Find the **Transport mechanisms** subsection. Select the **Use Darcy's Law for momentum transport** checkbox.
- 7 Locate the **O2 Gas Mixture** section. Select the **N2** checkbox.
- 8 Select the **Include gas phase diffusion** checkbox.
- 9 Select the **Use Darcy's Law for momentum transport** checkbox.

#### *Membrane 1*

- 1 In the **Physics** toolbar, click  **Domains** and choose **Membrane**.
- 2 Select Domain 4 only.

#### *H2 Gas Diffusion Electrode 1*

- 1 In the **Physics** toolbar, click  **Domains** and choose **H2 Gas Diffusion Electrode**.
- 2 Select Domain 5 only.
- 3 In the **Settings** window for **H2 Gas Diffusion Electrode**, locate the **Effective Electrolyte Charge Transport** section.
- 4 In the  $\epsilon_1$  text field, type eps1.
- 5 Locate the **Gas Transport** section. From the **Effective diffusivity correction** list, choose **Tortuosity**.
- 6 In the  $\epsilon_g$  text field, type epsg.
- 7 In the  $\tau_g$  text field, type taug.
- 8 In the  $\kappa_g$  text field, type kappag\_GDE.

#### *H2 Gas Diffusion Electrode Reaction: Water Electrolysis*

- 1 In the **Model Builder** window, under **Component 1 (comp1) > Water Electrolyzer (we) > H2 Gas Diffusion Electrode 1** click **H2 Gas Diffusion Electrode Reaction 1**.
- 2 In the **Settings** window for **H2 Gas Diffusion Electrode Reaction**, type H2 Gas Diffusion Electrode Reaction: Water Electrolysis in the **Label** text field.
- 3 Locate the **Electrode Kinetics** section. In the  $i_{0,\text{ref}}(T)$  text field, type i0\_ref\_HER.
- 4 In the  $\alpha_a$  text field, type 0.5.
- 5 Locate the **Active Specific Surface Area** section. In the  $a_v$  text field, type S.

#### *H2 Gas Diffusion Electrode 1*


In the **Model Builder** window, click **H2 Gas Diffusion Electrode 1**.

#### *H2 Gas Diffusion Electrode Reaction: CO2 Electrolysis*

- 1 In the **Physics** toolbar, click  **Attributes** and choose **H2 Gas Diffusion Electrode Reaction**.

- 2 In the **Settings** window for **H2 Gas Diffusion Electrode Reaction**, type H2 Gas Diffusion Electrode Reaction: CO2 Electrolysis in the **Label** text field.
- 3 Locate the **Stoichiometric Coefficients** section. In the  $v_{\text{CO}_2}$  text field, type -1.
- 4 In the  $v_{\text{CO}}$  text field, type 1.
- 5 Locate the **Electrode Kinetics** section. In the  $i_{0,\text{ref}}(T)$  text field, type  $i_{0,\text{ref\_COER}}$ .
- 6 Locate the **Active Specific Surface Area** section. In the  $a_v$  text field, type S.

#### *O2 Gas Diffusion Electrode I*


- 1 In the **Physics** toolbar, click  **Domains** and choose **O2 Gas Diffusion Electrode**.
- 2 Select Domain 3 only.
- 3 In the **Settings** window for **O2 Gas Diffusion Electrode**, locate the **Effective Electrolyte Charge Transport** section.
- 4 In the  $\epsilon_l$  text field, type eps1.
- 5 Locate the **Gas Transport** section. From the **Effective diffusivity correction** list, choose **Tortuosity**.
- 6 In the  $\epsilon_g$  text field, type epsg.
- 7 In the  $\tau_g$  text field, type taug.
- 8 In the  $\kappa_g$  text field, type kappag\_GDE.

#### *O2 Gas Diffusion Electrode Reaction I*

- 1 In the **Model Builder** window, click **O2 Gas Diffusion Electrode Reaction I**.
- 2 In the **Settings** window for **O2 Gas Diffusion Electrode Reaction**, locate the **Electrode Kinetics** section.
- 3 In the  $i_{0,\text{ref}}(T)$  text field, type  $i_{0,\text{ref\_OER}}$ .
- 4 Locate the **Active Specific Surface Area** section. In the  $a_v$  text field, type S.


#### *H2 Gas Flow Channel I*

Next, add the **H2 Gas Flow Channel**.

- 1 In the **Physics** toolbar, click  **Domains** and choose **H2 Gas Flow Channel**.
- 2 Select Domain 6 only.
- 3 In the **Settings** window for **H2 Gas Flow Channel**, locate the **Gas Transport** section.
- 4 From the list, choose **Straight channels**.
- 5 In the  $H$  text field, type dg.
- 6 In the  $W$  text field, type dg.

### *O<sub>2</sub> Gas Flow Channel 1*

Next, add the **O<sub>2</sub> Gas Flow Channel**.


- 1 In the **Physics** toolbar, click  **Domains** and choose **O<sub>2</sub> Gas Flow Channel**.
- 2 Select Domain 2 only.
- 3 In the **Settings** window for **O<sub>2</sub> Gas Flow Channel**, locate the **Gas Transport** section.
- 4 From the list, choose **Straight channels**.
- 5 In the  $H$  text field, type dg.
- 6 In the  $W$  text field, type dg.

### *Electronic Conducting Phase 1*

Next, specify the initial values for the oxygen domain to enhance convergence and set the boundary conditions.

- 1 In the **Model Builder** window, click **Electronic Conducting Phase 1**.

### *Initial Values, O<sub>2</sub> Domains 1*

- 1 In the **Physics** toolbar, click  **Attributes** and choose **Initial Values, O<sub>2</sub> Domains**.
- 2 Select Domain 3 only.
- 3 In the **Settings** window for **Initial Values, O<sub>2</sub> Domains**, locate the **Initial Values** section.
- 4 In the  $\phi_s$  text field, type E\_app.

### *Electronic Conducting Phase 1*

In the **Model Builder** window, click **Electronic Conducting Phase 1**.


### *Electric Ground 1*

- 1 In the **Physics** toolbar, click  **Attributes** and choose **Electric Ground**.
- 2 Select Boundary 12 only.

### *Electronic Conducting Phase 1*

In the **Model Builder** window, click **Electronic Conducting Phase 1**.

### *Electric Potential 1*

- 1 In the **Physics** toolbar, click  **Attributes** and choose **Electric Potential**.
- 2 Select Boundary 6 only.
- 3 In the **Settings** window for **Electric Potential**, locate the **Electric Potential** section.
- 4 In the  $\phi_{s,bnd}$  text field, type E\_app.

### *H2 Gas Phase I*

Next, specify initial values, add the water gas shift reaction, and set the hydrogen inlet and outlet boundary conditions.


### *Initial Values I*

- 1 In the **Model Builder** window, click **Initial Values I**.
- 2 In the **Settings** window for **Initial Values**, locate the **Initial Composition** section.
- 3 In the  $x_{0,H_2O}$  text field, type  $x0\_H2O$ .
- 4 In the  $x_{0,CO_2}$  text field, type  $x0\_CO2$ .
- 5 In the  $x_{0,CO}$  text field, type  $x0\_CO$ .

### *H2 Gas Phase I*

In the **Model Builder** window, click **H2 Gas Phase I**.


### *Water Gas Shift Reaction I*

- 1 In the **Physics** toolbar, click  **Attributes** and choose **Water Gas Shift Reaction**.
- 2 In the **Settings** window for **Water Gas Shift Reaction**, locate the **Water Gas Shift Reaction Rate** section.
- 3 In the  $k_{WGSR}$  text field, type  $k\_wgsr$ .
- 4 In the  $p_{ref}$  text field, type  $1 [Pa]$ .

### *H2 Gas Phase I*

In the **Model Builder** window, click **H2 Gas Phase I**.

### *H2 Inlet I*

- 1 In the **Physics** toolbar, click  **Attributes** and choose **H2 Inlet**.
- 2 Select Boundary I1 only.
- 3 In the **Settings** window for **H2 Inlet**, locate the **Inlet Flow Type** section.
- 4 Clear the **Stoichiometric feed** checkbox.
- 5 Locate the **Mass Flow Rates** section. In the  $J_{0,H_2O}$  text field, type  $Mflux\_in*w0\_H2O$ .
- 6 In the  $J_{0,CO_2}$  text field, type  $Mflux\_in*w0\_CO2$ .
- 7 In the  $J_{0,CO}$  text field, type  $Mflux\_in*w0\_CO$ .
- 8 Locate the **Flow Boundary Condition** section. From the list, choose **Total mass flow rate**.
- 9 In the  $J_0$  text field, type  $Mflux\_in$ .

### *H2 Gas Phase I*

In the **Model Builder** window, click **H2 Gas Phase I**.

### *H2 Outlet 1*

- 1 In the **Physics** toolbar, click  **Attributes** and choose **H2 Outlet**.
- 2 Select Boundary 21 only.

### *O2 Gas Phase 1*

Next, set the initial values and the oxygen inlet and outlet boundary conditions.


### *Initial Values 1*

- 1 In the **Model Builder** window, click **Initial Values 1**.
- 2 In the **Settings** window for **Initial Values**, locate the **Initial Composition** section.
- 3 In the  $x_{0,N_2}$  text field, type  $x_{0,N_2}$ .

### *O2 Gas Phase 1*

In the **Model Builder** window, click **O2 Gas Phase 1**.

### *O2 Inlet 1*

- 1 In the **Physics** toolbar, click  **Attributes** and choose **O2 Inlet**.
- 2 Select Boundary 3 only.
- 3 In the **Settings** window for **O2 Inlet**, locate the **Inlet Flow Type** section.
- 4 From the **Inlet flow type** list, choose **Mass flow rates**.
- 5 Locate the **Mass Flow Rates** section. In the  $J_{0,N_2}$  text field, type  $Mflux\_in*w_{0,N_2}$ .
- 6 Locate the **Flow Boundary Condition** section. From the list, choose **Total mass flow rate**.
- 7 In the  $J_0$  text field, type  $Mflux\_in$ .

### *O2 Gas Phase 1*

In the **Model Builder** window, click **O2 Gas Phase 1**.

### *O2 Outlet 1*

- 1 In the **Physics** toolbar, click  **Attributes** and choose **O2 Outlet**.
- 2 Select Boundary 17 only.

## **HEAT TRANSFER IN SOLIDS AND FLUIDS (HT)**

Next, set the heat transfer physics.

- 1 In the **Model Builder** window, under **Component 1 (comp1)** click **Heat Transfer in Solids and Fluids (ht)**.
- 2 In the **Settings** window for **Heat Transfer in Solids and Fluids**, locate the **Physical Model** section.
- 3 In the  $T_{ref}$  text field, type  $T\_in$ .

*Solid: Interconnects*

- 1 In the **Model Builder** window, under **Component 1 (comp1) > Heat Transfer in Solids and Fluids (ht)** click **Solid 1**.
- 2 In the **Settings** window for **Solid**, type Solid: Interconnects in the **Label** text field.

*Fluid: Flow Channels*

- 1 In the **Model Builder** window, under **Component 1 (comp1) > Heat Transfer in Solids and Fluids (ht)** click **Fluid 1**.
- 2 In the **Settings** window for **Fluid**, type Fluid: Flow Channels in the **Label** text field.
- 3 Select Domains 2 and 6 only.
- 4 Locate the **Model Input** section. From the  $p_A$  list, choose **User defined**. In the associated text field, type  $w_e.pA$ .
- 5 Locate the **Heat Convection** section. Specify the **u** vector as

$w_e.u$	$x$
$w_e.v$	$y$


- 6 Locate the **Heat Conduction, Fluid** section. From the  $k$  list, choose **Thermal conductivity, gas phase (we)**.
- 7 Locate the **Thermodynamics, Fluid** section. From the **Fluid type** list, choose **Gas/Liquid**.
- 8 From the  $p$  list, choose **Density of gas phase (we)**.
- 9 From the  $C_p$  list, choose **Heat capacity at constant pressure, gas phase (we)**.

*Initial Values 1*

- 1 In the **Model Builder** window, click **Initial Values 1**.
- 2 In the **Settings** window for **Initial Values**, locate the **Initial Values** section.
- 3 In the  $T$  text field, type  $T_{in}$ .

*Porous Medium: Cathode GDE*

Next, add thermal conductivities for the gas diffusion electrode domains.

- 1 In the **Physics** toolbar, click  **Domains** and choose **Porous Medium**.
- 2 In the **Settings** window for **Porous Medium**, type Porous Medium: Cathode GDE in the **Label** text field.
- 3 Select Domain 5 only.

*Fluid 1*

- 1 In the **Model Builder** window, click **Fluid 1**.

- 2 In the **Settings** window for **Fluid**, locate the **Model Input** section.
- 3 From the  $p_A$  list, choose **User defined**. In the associated text field, type  $we.pA$ .
- 4 Locate the **Heat Convection** section. Specify the **u** vector as


$we.u$	$x$
$we.v$	$y$

- 5 Locate the **Heat Conduction, Fluid** section. From the  $k_f$  list, choose **Thermal conductivity, gas phase (we)**.
- 6 Locate the **Thermodynamics, Fluid** section. From the  $\rho_f$  list, choose **Density of gas phase (we)**.
- 7 From the  $C_{p,f}$  list, choose **Heat capacity at constant pressure, gas phase (we)**.

#### *Porous Matrix 1*

- 1 In the **Model Builder** window, click **Porous Matrix 1**.
- 2 In the **Settings** window for **Porous Matrix**, locate the **Matrix Properties** section.
- 3 From the  $\varepsilon_p$  list, choose **User defined**. In the associated text field, type  $eps_g$ .
- 4 Locate the **Heat Conduction, Porous Matrix** section. From the  $k_b$  list, choose **User defined**. In the associated text field, type  $kc$ .
- 5 Locate the **Thermodynamics, Porous Matrix** section. From the  $\rho_b$  list, choose **User defined**. From the  $C_{p,b}$  list, choose **User defined**.

#### *Porous Medium: Anode GDE*

- 1 In the **Physics** toolbar, click  **Domains** and choose **Porous Medium**.
- 2 In the **Settings** window for **Porous Medium**, type Porous Medium: Anode GDE in the **Label** text field.
- 3 Select Domain 3 only.

#### *Fluid 1*

- 1 In the **Model Builder** window, click **Fluid 1**.
- 2 In the **Settings** window for **Fluid**, locate the **Model Input** section.
- 3 From the  $p_A$  list, choose **User defined**. In the associated text field, type  $we.pA$ .
- 4 Locate the **Heat Convection** section. Specify the **u** vector as

$we.u$	$x$
$we.v$	$y$


- 5 Locate the **Heat Conduction, Fluid** section. From the  $k_f$  list, choose **Thermal conductivity, gas phase (we)**.
- 6 Locate the **Thermodynamics, Fluid** section. From the  $\rho_f$  list, choose **Density of gas phase (we)**.
- 7 From the  $C_{p,f}$  list, choose **Heat capacity at constant pressure, gas phase (we)**.

#### *Porous Matrix 1*

- 1 In the **Model Builder** window, click **Porous Matrix 1**.
- 2 In the **Settings** window for **Porous Matrix**, locate the **Matrix Properties** section.
- 3 From the  $\epsilon_p$  list, choose **User defined**. In the associated text field, type epsg.
- 4 Locate the **Heat Conduction, Porous Matrix** section. From the  $k_b$  list, choose **User defined**. In the associated text field, type ka.
- 5 Locate the **Thermodynamics, Porous Matrix** section. From the  $\rho_b$  list, choose **User defined**. From the  $C_{p,b}$  list, choose **User defined**.


#### *Solid: Membrane*

Next, add thermal conductivity for the membrane domains.


- 1 In the **Physics** toolbar, click  **Domains** and choose **Solid**.
- 2 In the **Settings** window for **Solid**, type Solid: Membrane in the **Label** text field.
- 3 Select Domain 4 only.
- 4 Locate the **Heat Conduction, Solid** section. From the  $k$  list, choose **User defined**. In the associated text field, type km.
- 5 Locate the **Thermodynamics, Solid** section. From the  $\rho$  list, choose **User defined**. From the  $C_p$  list, choose **User defined**.

#### *Inflow 1*


Next, add the inflow, outflow, and periodic condition boundary conditions.

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Inflow**.
- 2 Select Boundaries 3 and 11 only.
- 3 In the **Settings** window for **Inflow**, locate the **Upstream Properties** section.
- 4 In the  $T_{ustr}$  text field, type T\_in.

#### *Outflow 1*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Outflow**.
- 2 Select Boundaries 17 and 21 only.

### *Periodic Condition 1*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Periodic Condition**.
- 2 Select Boundaries 2 and 15 only.

### **MULTIPHYSICS**

Next, add an electrochemical heating multiphysics coupling.


### *Electrochemical Heating 1 (ech1)*

- In the **Physics** toolbar, click  **Multiphysics Couplings** and choose **Domain** > **Electrochemical Heating**.

### **MATERIALS**


Now, add materials from the Material Library.

### **ADD MATERIAL**


- 1 In the **Materials** toolbar, click  **Add Material** to open the **Add Material** window.
- 2 Go to the **Add Material** window.
- 3 In the tree, select **Fuel Cell and Electrolyzer** > **Solid Oxides** > **Yttria-Stabilized Zirconia, 8YSZ, (ZrO2)0.92-(Y2O3)0.08**.
- 4 Click the **Add to Component** button in the window toolbar.

### **MATERIALS**

### *Yttria-Stabilized Zirconia, 8YSZ, (ZrO2)0.92-(Y2O3)0.08 (mat1)*

- 1 In the **Settings** window for **Material**, locate the **Geometric Entity Selection** section.
- 2 Click  **Clear Selection**.
- 3 Select Domains 3–5 only.

### **ADD MATERIAL**

- 1 Go to the **Add Material** window.
- 2 In the tree, select **Built-in** > **Steel AISI 4340**.
- 3 Click the **Add to Component** button in the window toolbar.
- 4 In the **Materials** toolbar, click  **Add Material** to close the **Add Material** window.

### **MATERIALS**

### *Steel AISI 4340 (mat2)*

Select Domains 1 and 7 only.

## MESH 1

Next, set up a user-controlled mesh.

### *Distribution 1*

- 1 In the **Model Builder** window, under **Component 1 (comp1)** right-click **Mesh 1** and choose **Distribution**.
- 2 Select Boundaries 2, 4, 6, 8, 10, 12, 14, and 15 only.
- 3 In the **Settings** window for **Distribution**, locate the **Distribution** section.
- 4 In the **Number of elements** text field, type 100.

### *Distribution 2*

- 1 In the **Model Builder** window, right-click **Mesh 1** and choose **Distribution**.
- 2 Select Boundaries 1, 13, 16, and 22 only.
- 3 In the **Settings** window for **Distribution**, locate the **Distribution** section.
- 4 In the **Number of elements** text field, type 2.

### *Distribution 3*

- 1 Right-click **Mesh 1** and choose **Distribution**.
- 2 Select Boundaries 3, 11, 17, and 21 only.
- 3 In the **Settings** window for **Distribution**, locate the **Distribution** section.
- 4 In the **Number of elements** text field, type 10.

### *Distribution 4*

- 1 Right-click **Mesh 1** and choose **Distribution**.
- 2 Select Boundaries 7 and 19 only.
- 3 In the **Settings** window for **Distribution**, locate the **Distribution** section.
- 4 In the **Number of elements** text field, type 2.

### *Distribution 5*

- 1 Right-click **Mesh 1** and choose **Distribution**.
- 2 Select Boundaries 9 and 20 only.
- 3 In the **Settings** window for **Distribution**, locate the **Distribution** section.
- 4 From the **Distribution type** list, choose **Predefined**.
- 5 In the **Number of elements** text field, type 20.
- 6 In the **Element ratio** text field, type 10.
- 7 From the **Growth rate** list, choose **Exponential**.

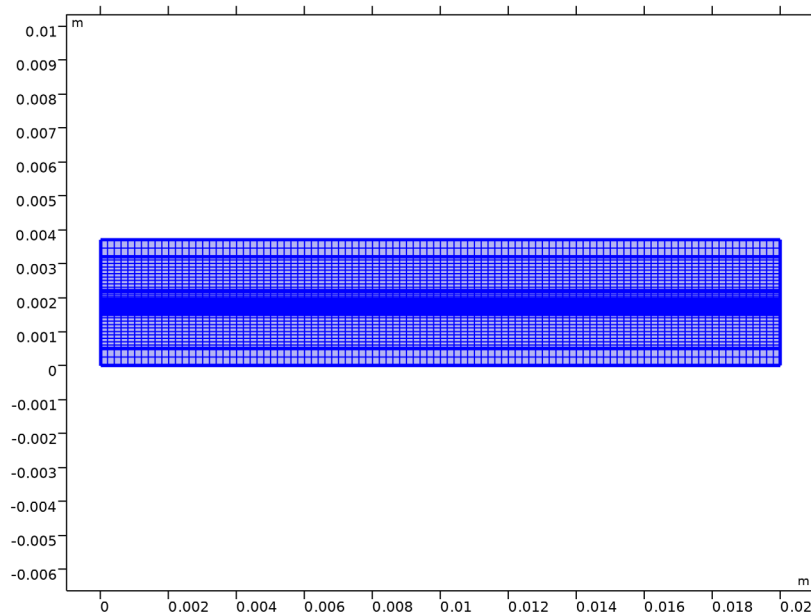
### *Distribution 6*

- 1 Right-click **Mesh 1** and choose **Distribution**.
- 2 Select Boundaries 5 and 18 only.
- 3 In the **Settings** window for **Distribution**, locate the **Distribution** section.
- 4 From the **Distribution type** list, choose **Predefined**.
- 5 In the **Number of elements** text field, type 10.
- 6 In the **Element ratio** text field, type 5.
- 7 From the **Growth rate** list, choose **Exponential**.
- 8 Select the **Reverse direction** checkbox.

### *Mapped 1*

- 1 In the **Mesh** toolbar, click  **Mapped**.
- 2 In the **Settings** window for **Mapped**, click  **Build All**.
- 3 Click the  **Zoom Extents** button in the **Graphics** toolbar.

The mesh should look like this:



### **STUDY 1**

Finally, set the study settings using an auxiliary sweep for the applied potential to complete the model setup.

### Step 1: Current Distribution Initialization

- 1 In the **Model Builder** window, under **Study 1** click **Step 1: Current Distribution Initialization**.
- 2 In the **Settings** window for **Current Distribution Initialization**, locate the **Study Settings** section.
- 3 From the **Current distribution type** list, choose **Secondary**.

### Step 2: Stationary

- 1 In the **Model Builder** window, click **Step 2: Stationary**.
- 2 In the **Settings** window for **Stationary**, click to expand the **Study Extensions** section.
- 3 Select the **Auxiliary sweep** checkbox.
- 4 Click **+ Add**.
- 5 In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
E_app (SOEC operating potential)	range (0.7, 0.1, 1.5)	V

- 6 In the **Study** toolbar, click **= Compute**.

## RESULTS


Some plots are added by default. Follow the instructions below to reproduce the figures in the [Results and Discussion](#) section.

### Surface 1

- 1 In the **Model Builder** window, expand the **Mole Fraction, H2 (we)** node, then click **Surface 1**.
- 2 In the **Settings** window for **Surface**, locate the **Coloring and Style** section.
- 3 From the **Color table** list, choose **ConopiformisZero**.

### Streamline 1

- 1 In the **Model Builder** window, click **Streamline 1**.
- 2 In the **Settings** window for **Streamline**, locate the **Streamline Positioning** section.
- 3 In the **Density level** text field, type 7.
- 4 Locate the **Coloring and Style** section. Find the **Point style** subsection. From the **Arrow length** list, choose **Proportional**.
- 5 From the **Color** list, choose **Cyan**.


- 6 In the **Mole Fraction, H<sub>2</sub> (we)** toolbar, click  **Plot**.

The plot should look like [Figure 2](#).

#### *Surface 1*

- 1 In the **Model Builder** window, expand the **Mole Fraction, CO (we)** node, then click **Surface 1**.
- 2 In the **Settings** window for **Surface**, locate the **Coloring and Style** section.
- 3 From the **Color table** list, choose **ConopiformisZero**.

#### *Streamline 1*


- 1 In the **Model Builder** window, click **Streamline 1**.
- 2 In the **Settings** window for **Streamline**, locate the **Streamline Positioning** section.
- 3 In the **Density level** text field, type 7.5.
- 4 Locate the **Coloring and Style** section. Find the **Point style** subsection. From the **Arrow length** list, choose **Proportional**.
- 5 From the **Color** list, choose **Cyan**.
- 6 In the **Mole Fraction, CO (we)** toolbar, click  **Plot**.

The plot should look like [Figure 3](#).

#### *Surface 1*

- 1 In the **Model Builder** window, expand the **Temperature (ht)** node, then click **Surface 1**.
- 2 In the **Settings** window for **Surface**, locate the **Expression** section.
- 3 In the **Expression** text field, type  $T - T_{in}$ .


#### *Temperature (ht)*

- 1 In the **Model Builder** window, click **Temperature (ht)**.
- 2 In the **Settings** window for **2D Plot Group**, click to expand the **Title** section.
- 3 From the **Title type** list, choose **Manual**.
- 4 In the **Title** text area, type Surface: Change in Temperature (K).
- 5 In the **Temperature (ht)** toolbar, click  **Plot**.

The plot should look like [Figure 4](#).



#### *Water Gas Shift Reaction Rate*

Next, plot the water gas shift reaction rate over the hydrogen gas diffusion electrode and flow channel domains.

- 1 In the **Results** toolbar, click  **2D Plot Group**.


- 2 In the **Settings** window for **2D Plot Group**, type Water Gas Shift Reaction Rate in the **Label** text field.

#### *Surface I*


- 1 In the **Water Gas Shift Reaction Rate** toolbar, click  **Surface**.
- 2 In the **Settings** window for **Surface**, locate the **Expression** section.
- 3 In the **Expression** text field, type `we.r_wgsr`.
- 4 Locate the **Coloring and Style** section. From the **Color table** list, choose **Ctenophora**.
- 5 In the **Water Gas Shift Reaction Rate** toolbar, click  **Plot**.  
The plot should look like [Figure 5](#).

#### *Current Density Distribution*

Add a plot for the total integrated current density across the electrode length.

- 1 In the **Results** toolbar, click  **ID Plot Group**.
- 2 In the **Settings** window for **ID Plot Group**, type Current Density Distribution in the **Label** text field.
- 3 Locate the **Data** section. From the **Parameter selection (E\_app)** list, choose **Last**.
- 4 Click to expand the **Title** section. From the **Title type** list, choose **Manual**.
- 5 In the **Title** text area, type Current Density Distribution, Cathode Side.
- 6 Locate the **Plot Settings** section.
- 7 Select the **x-axis label** checkbox. In the associated text field, type Electrode length (m).
- 8 Select the **y-axis label** checkbox. In the associated text field, type Integrated current density in y direction ( $A/cm^{2}$ ).

#### *Line Graph I*

- 1 In the **Current Density Distribution** toolbar, click  **Line Graph**.
- 2 Select Boundary 10 only.
- 3 In the **Settings** window for **Line Graph**, locate the **y-Axis Data** section.
- 4 In the **Expression** text field, type `genproj1(we.iv_h2gder1)`.
- 5 In the **Unit** field, type  $A/cm^2$ .
- 6 Click to expand the **Coloring and Style** section. From the **Width** list, choose **2**.
- 7 Click to expand the **Legends** section. Select the **Show legends** checkbox.
- 8 From the **Legends** list, choose **Manual**.

9 In the table, enter the following settings:

---

**Legends**

---


H2O

---

*Current Density Distribution*

In the **Model Builder** window, click **Current Density Distribution**.

*Line Graph 2*

- 1 In the **Current Density Distribution** toolbar, click  **Line Graph**.
- 2 Select Boundary 10 only.
- 3 In the **Settings** window for **Line Graph**, locate the **y-Axis Data** section.
- 4 In the **Expression** text field, type `genproj1 (we.iv_h2gder2)`.
- 5 In the **Unit** field, type `A/cm^2`.
- 6 Locate the **Coloring and Style** section. From the **Width** list, choose **2**.
- 7 Locate the **Legends** section. Select the **Show legends** checkbox.
- 8 From the **Legends** list, choose **Manual**.
- 9 In the table, enter the following settings:

---


**Legends**

---

CO2


---

*Current Density Distribution*

- 1 In the **Model Builder** window, click **Current Density Distribution**.
- 2 In the **Current Density Distribution** toolbar, click  **Plot**.  
The plot should look like [Figure 6](#).


*Polarization Plot*

Finally, add the Polarization Plot.

- 1 In the **Home** toolbar, click  **Add Plot Group** and choose **ID Plot Group**.
- 2 In the **Settings** window for **ID Plot Group**, type Polarization Plot in the **Label** text field.
- 3 Click to expand the **Title** section. From the **Title type** list, choose **Manual**.
- 4 In the **Title** text area, type Polarization plot.
- 5 Locate the **Plot Settings** section. Select the **x-axis label** checkbox.
- 6 Select the **y-axis label** checkbox.

- 7 In the **x-axis label** text field, type Applied potential (V).
- 8 In the **y-axis label** text field, type Average current density ( $A/cm^{2}$ ).

#### *Point Graph 1*

- 1 Right-click **Polarization Plot** and choose **Point Graph**.
- 2 Select Point 6 only.
- 3 In the **Settings** window for **Point Graph**, locate the **y-Axis Data** section.
- 4 In the **Expression** text field, type  $aveop\_an(we.nIs)$ .
- 5 In the **Unit** field, type  $A/cm^2$ .
- 6 Click to expand the **Coloring and Style** section. From the **Width** list, choose 2.
- 7 Click to expand the **Legends** section. Clear the **Show legends** checkbox.
- 8 In the **Polarization Plot** toolbar, click  **Plot**.

The plot should look like [Figure 7](#).

Follow the commands below to improve the appearance of the other plots.

#### *Surface 1*

- 1 In the **Model Builder** window, expand the **Electrode Potential with Respect to Ground (we)** node, then click **Surface 1**.
- 2 In the **Settings** window for **Surface**, locate the **Coloring and Style** section.
- 3 From the **Color table** list, choose **MetasepiaBlue**.

#### *Arrow Surface 1*

In the **Model Builder** window, right-click **Arrow Surface 1** and choose **Disable**.

#### *Surface 1*

- 1 In the **Model Builder** window, expand the **Electrolyte Potential (we)** node, then click **Surface 1**.
- 2 In the **Settings** window for **Surface**, locate the **Coloring and Style** section.
- 3 From the **Color table** list, choose **MetasepiaBlue**.

#### *Arrow Surface 1*

- 1 In the **Model Builder** window, click **Arrow Surface 1**.
- 2 In the **Settings** window for **Arrow Surface**, locate the **Coloring and Style** section.
- 3 From the **Color** list, choose **Yellow**.

#### *Surface 1*

- 1 In the **Model Builder** window, expand the **Mole Fraction, O<sub>2</sub> (we)** node, then click **Surface 1**.
- 2 In the **Settings** window for **Surface**, locate the **Coloring and Style** section.
- 3 From the **Color table** list, choose **ConopiformisZero**.

#### *Streamline 1*

- 1 In the **Model Builder** window, click **Streamline 1**.
- 2 In the **Settings** window for **Streamline**, locate the **Streamline Positioning** section.
- 3 In the **Density level** text field, type 8.
- 4 Locate the **Coloring and Style** section. Find the **Point style** subsection. From the **Arrow length** list, choose **Proportional**.
- 5 From the **Color** list, choose **Cyan**.

#### *Surface 1*

- 1 In the **Model Builder** window, expand the **Mole Fraction, H<sub>2</sub>O (we)** node, then click **Surface 1**.
- 2 In the **Settings** window for **Surface**, locate the **Coloring and Style** section.
- 3 From the **Color table** list, choose **ConopiformisZero**.

#### *Streamline 1*

- 1 In the **Model Builder** window, click **Streamline 1**.
- 2 In the **Settings** window for **Streamline**, locate the **Streamline Positioning** section.
- 3 In the **Density level** text field, type 9.
- 4 Locate the **Coloring and Style** section. Find the **Point style** subsection. From the **Arrow length** list, choose **Proportional**.
- 5 From the **Color** list, choose **Cyan**.

#### *Surface 1*

- 1 In the **Model Builder** window, expand the **Mole Fraction, N<sub>2</sub> (we)** node, then click **Surface 1**.
- 2 In the **Settings** window for **Surface**, locate the **Coloring and Style** section.
- 3 From the **Color table** list, choose **ConopiformisZero**.

#### *Streamline 1*

- 1 In the **Model Builder** window, click **Streamline 1**.
- 2 In the **Settings** window for **Streamline**, locate the **Streamline Positioning** section.

- 3 In the **Density level** text field, type 8.
- 4 Locate the **Coloring and Style** section. Find the **Point style** subsection. From the **Arrow length** list, choose **Proportional**.
- 5 From the **Color** list, choose **Cyan**.

#### *Surface 1*

- 1 In the **Model Builder** window, expand the **Mole Fraction, CO2 (we)** node, then click **Surface 1**.
- 2 In the **Settings** window for **Surface**, locate the **Coloring and Style** section.
- 3 From the **Color table** list, choose **ConopiformisZero**.

#### *Streamline 1*

- 1 In the **Model Builder** window, click **Streamline 1**.
- 2 In the **Settings** window for **Streamline**, locate the **Streamline Positioning** section.
- 3 In the **Density level** text field, type 8.
- 4 Locate the **Coloring and Style** section. Find the **Point style** subsection. From the **Arrow length** list, choose **Proportional**.
- 5 From the **Color** list, choose **Cyan**.

#### *Surface 1*

- 1 In the **Model Builder** window, expand the **Pressure (we)** node, then click **Surface 1**.
- 2 In the **Settings** window for **Surface**, locate the **Coloring and Style** section.
- 3 From the **Color table** list, choose **HelfrichiZero**.
- 4 From the **Color table type** list, choose **Discrete**.

#### *Streamline 1*

- 1 In the **Model Builder** window, click **Streamline 1**.
- 2 In the **Settings** window for **Streamline**, locate the **Streamline Positioning** section.
- 3 In the **Density level** text field, type 9.
- 4 Locate the **Coloring and Style** section. Find the **Point style** subsection. From the **Arrow length** list, choose **Proportional**.
- 5 From the **Color** list, choose **Gray**.