



# Thermal Fatigue of a Surface Mount Resistor

## Introduction

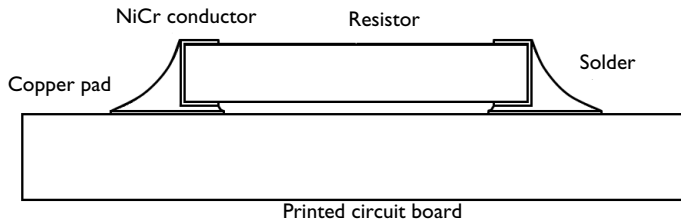
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A surface mount resistor is subjected to thermal cycling. The difference in the thermal expansion between the materials introduces thermal stresses in the structure. The solder, connecting the resistor to the printed circuit board, is seen as the weakest link in the assembly. Because the operating temperature is high when compared to the melting point of the solder, creep deformation occurs. In order to ensure the structural integrity of the component, a fatigue analysis is performed where the life predictions from two different fatigue models are compared.

## Model Definition

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A resistor is fastened on a printed circuit board (PCB) with SnAgCu solder. The solder is connected to the printed circuit board through two copper pads and to the resistor through a NiCr conductor. In reality there are additional thin films around the resistor but they are disregarded in current analysis. A sketch of the surface mount assembly is shown in [Figure 1](#).



*Figure 1: Schematic description of the surface mount resistor.*

The resistor is made out of alumina and has dimensions 3.2 mm x 0.55 mm. It is covered on both edges with a 0.025 mm layer of NiCr conductor. The thin layer continues 0.325 mm along the lower and the upper side of the resistor. The printed circuit board is large in comparison with the resistor and is here modeled 0.8 mm thick. It has two copper pads on the top side that are 0.025 mm thick and 1.05 mm wide. The thickness of the solder fillet between the copper pads and the NiCr conductor is 0.05 mm. The remaining shape of the solder joint varies greatly between each examined solder joint and is here modeled with two representative roundings.

Because the out-of-plane dimension is 1.55 mm, which is significant in comparison with the size of the resistor, the model is simulated in 2D, assuming plane strain conditions.

The elastic properties of the materials are summarized in [Table 1](#).

TABLE 1: ELASTIC AND THERMAL MATERIAL PROPERTIES.

MATERIAL	YOUNG'S MODULUS (GPA)	POISSON'S RATIO	COEFFICIENT OF THERMAL EXPANSION (PPM/°C)
PCB laminate	22	0.4	21
Copper	141	0.35	17
SnAgCu	50	0.4	21
NiCr	170	0.31	13
Alumina	300	0.22	8

The SnAgCu solder material exhibits creep behavior, which can be modeled by a Garofalo model where creep rate is described with

$$\frac{d\varepsilon_{ij}^c}{dT} = 2.62 \cdot 10^5 \left[ \sinh\left(\frac{\sigma_e}{39.1 \cdot 10^6}\right) \right]^{6.19} e^{-\left(\frac{5.32 \cdot 10^4}{RT}\right)} \cdot \frac{3s_{ij}}{2\sigma_e} \quad (1)$$

where  $\varepsilon_{ij}^c$  is the creep strain tensor,  $T$  is the temperature,  $\sigma_e$  is the equivalent stress,  $R$  is the universal gas constant, and  $s_{ij}$  is the deviatoric stress tensor.

The thermal load during an operating cycle is prescribed as a temperature which varies between 20 °C and 70 °C. Each temperature change takes 2 minutes and is followed by a 3 minutes dwell. This means that one fatigue cycle requires 10 minutes, see [Figure 2](#).

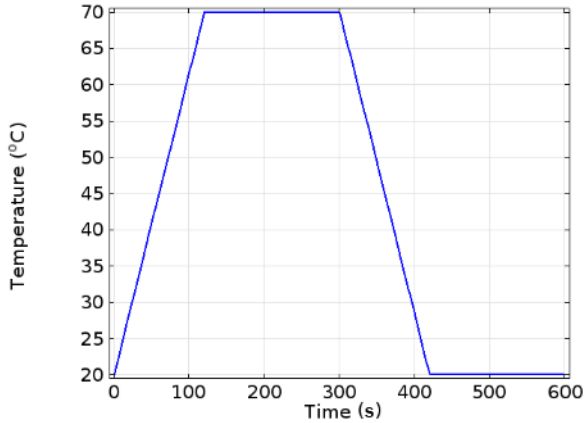


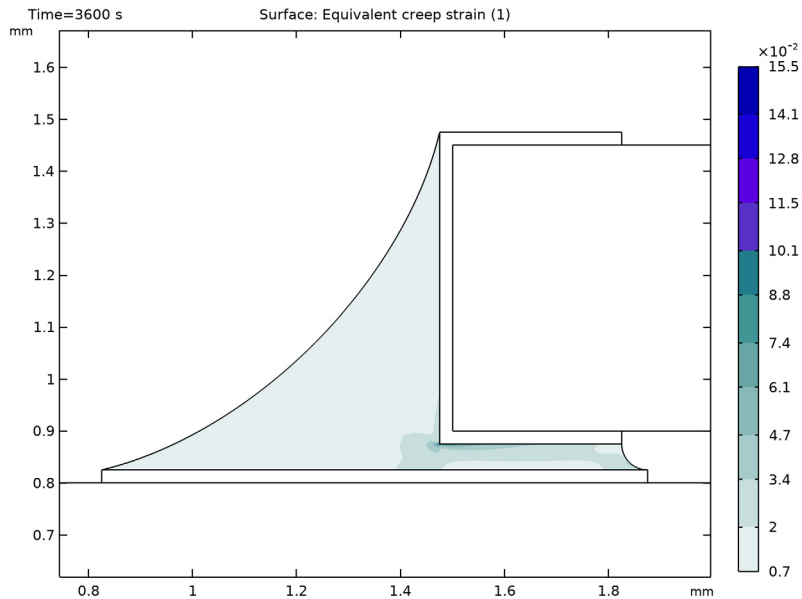
Figure 2: Temperature load.

Since the solder material is nonlinear, see [Equation 1](#), simulation of several cycles may be required before a stable cycle is obtained.

Two fatigue models are evaluated. The first is a strain-based Coffin–Manson-type model with the equivalent creep strain as the damage controlling mechanism, and the second is an energy-based Morrow-type model with the dissipated creep energy as the damage controlling mechanism. The material constants for the Coffin–Manson model are  $\epsilon_f^1 = 0.281$  and  $c = -0.51$ . The material constants for the Morrow-type model are  $W_f' = 55.0 \text{ J/m}^3$  and  $m = -0.69$ .

### Results and Discussion

The difference in the elastic and thermal properties introduces thermal stresses in the device. Although they are not very high, the solder experiences significant inelastic strains. In [Figure 3](#) accumulated equivalent creep strain after six cycles is shown.



*Figure 3: Creep strains in the solder joint.*

The highest strains occur in the thin solder layer just below the resistor. It is mainly the shear strain component which contributes to the equivalent creep strain in that layer. The slightly higher values around the edge are also affected by modeling of a sharp corner. With a fillet instead, the strains will be somewhat lower. Nevertheless, the location of highest strain agrees well with the crack path in real applications.

In order to evaluate fatigue, it is important to obtain a stable load cycle. In applications involving solder joints, either inelastic strain or dissipated energy are typically used to predict fatigue. The change of creep strain during the first six cycles is therefore evaluated at a point just below the resistor, slightly shifted to the right from the sharp corner. The position of this point can be debated. It is however located in the area where the largest strains occur, and is therefore seen as the critical point. In Figure 4, the equivalent creep strain and the shear creep strain components are shown.

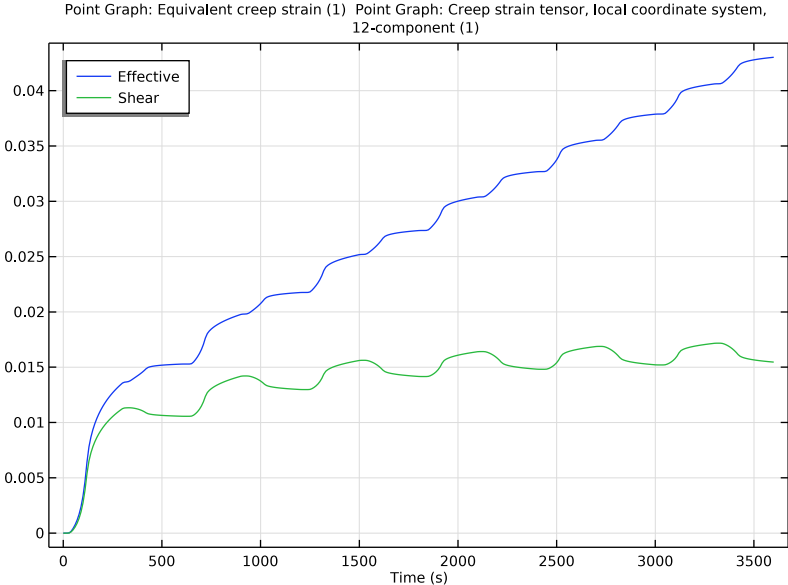
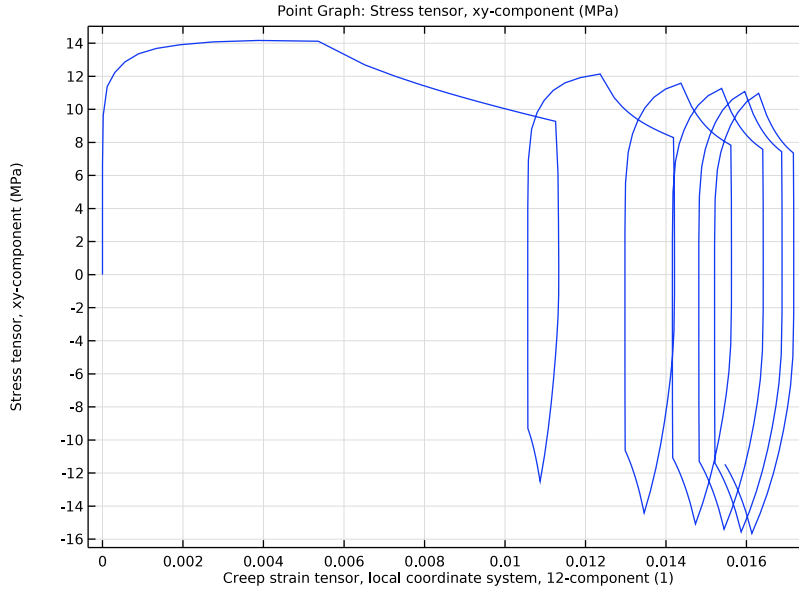


Figure 4: Creep strain development in a critical point below the resistor.

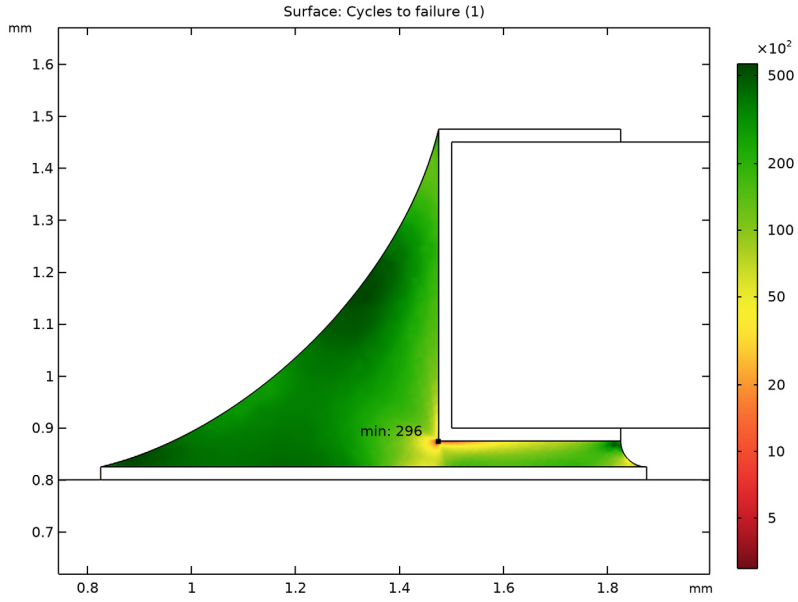
The dissipated energy represents a combined contribution of changes in stresses and strains during a cycle and is in Figure 5 shown with a shear hysteresis. The shear component has been chosen since it gives the dominating contribution to the equivalent creep strain in the critical point.



*Figure 5: Shear hysteresis evaluated in a critical point just below the resistor.*

It is clear from the two last figures that the first cycle is not representative for fatigue analysis, since its response differs significantly from the one experienced in the following cycles. Even after six cycles, the stress-strain loop has not stabilized. The temperature cycling can be extended with additional cycles to evaluate whether the state stabilizes further or not. Under some conditions, it may happen that the hysteresis loop is moving in stress-strain space. In this example additional cycles are not simulated since the difference in the creep strain and the dissipated energy between cycle five and six is small. Assuming that the consecutive cycles follow the trend and deform less as, well as dissipate less energy, the fatigue analysis based on the results of the sixth cycle gives a conservative fatigue prediction.

The fatigue life based on the Coffin–Manson model is shown in [Figure 6](#), and the fatigue life based on the Morrow model is shown in [Figure 7](#).



*Figure 6: Fatigue life based on the creep strain.*

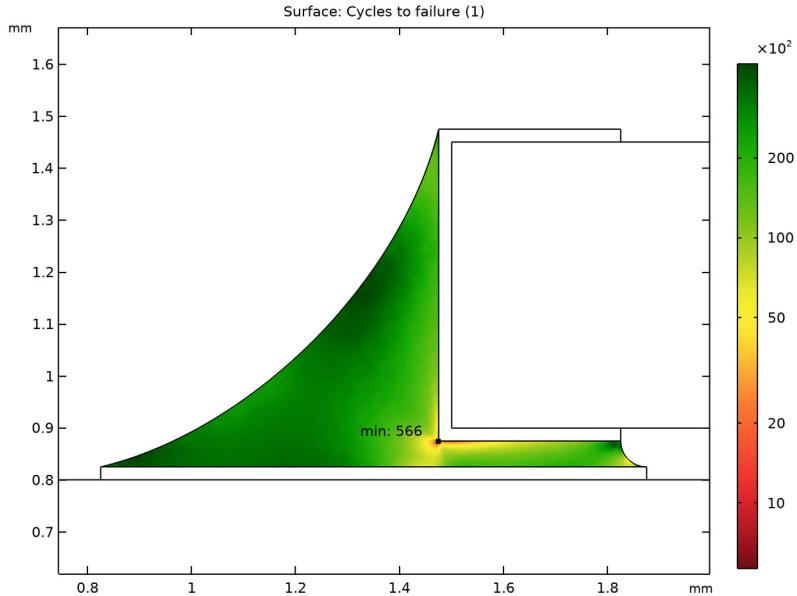


Figure 7: Fatigue life based on the dissipated energy.

Fatigue based on strain gives lifetime of about 300 cycles, while the energy prediction gives about 600 cycles.

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**Application Library path:** Fatigue\_Module/Energy\_Based/  
surface\_mount\_resistor


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### *Modeling Instructions*


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From the **File** menu, choose **New**.



#### **NEW**

In the **New** window, click  **Model Wizard**.

#### **MODEL WIZARD**



**1** In the **Model Wizard** window, click  **2D**.

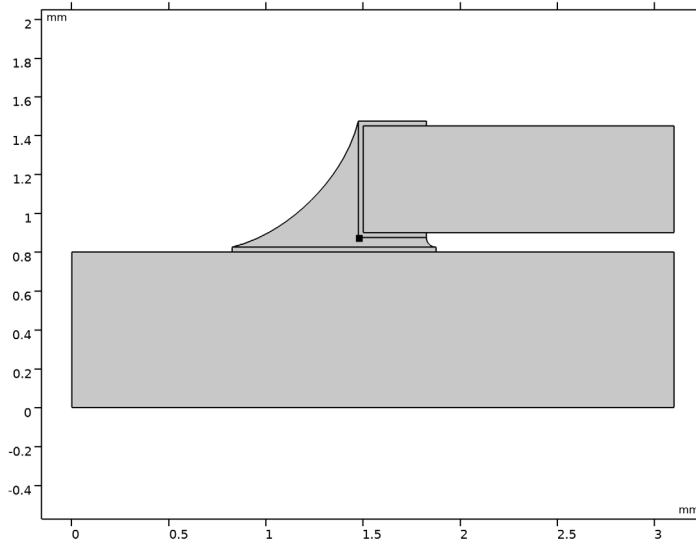
**2** In the **Select Physics** tree, select **Structural Mechanics > Solid Mechanics (solid)**.

- 3 Click **Add**.
- 4 Click  **Study**.
- 5 In the **Select Study** tree, select **General Studies > Time Dependent**.
- 6 Click  **Done**.

### GEOMETRY I


The geometry sequence for the model is available in a file. If you want to create it from scratch yourself, you can follow the instructions in the [Appendix — Geometry Modeling Instructions](#) section. Otherwise, insert the geometry sequence as follows:



- 1 In the **Geometry** toolbar, click **Insert Sequence** and choose **Insert Sequence**.
- 2 Browse to the model's Application Libraries folder and double-click the file `surface_mount_resistor_geom_sequence.mph`.
- 3 In the **Geometry** toolbar, click  **Build All**.
- 4 Click the  **Zoom Extents** button in the **Graphics** toolbar.
- 5 In the **Model Builder** window, under **Component 1 (comp1)** click **Geometry 1**.



### GLOBAL DEFINITIONS

#### *Interpolation 1 (int1)*

- 1 In the **Home** toolbar, click  **Functions** and choose **Global > Interpolation**.
- 2 In the **Settings** window for **Interpolation**, locate the **Definition** section.

- 3 From the **Data source** list, choose **File**.
- 4 Click  **Browse**.
- 5 Browse to the model's Application Libraries folder and double-click the file `surface_mount_resistor_thermal_load_cycle.txt`.
- 6 Click  **Import**.
- 7 In the **Function name** text field, type `thermLC`.
- 8 Locate the **Units** section. In the **Argument** table, enter the following settings:

Argument	Unit
t	min


- 9 In the **Function** table, enter the following settings:

Function	Unit
thermLC	degC


### SOLID MECHANICS (SOLID)

- 1 In the **Model Builder** window, under **Component 1 (comp1)** click **Solid Mechanics (solid)**.
- 2 In the **Settings** window for **Solid Mechanics**, locate the **Thickness** section.
- 3 In the *d* text field, type `1.55[mm]`.
- 4 Locate the **Structural Transient Behavior** section. From the list, choose **Quasistatic**.

#### *Linear Elastic Material 1*

- 1 Click the  **Show More Options** button in the **Model Builder** toolbar.
- 2 In the **Show More Options** dialog, in the tree, select the checkbox for the node **Physics > Advanced Physics Options**.
- 3 Click **OK**.
- 4 In the **Model Builder** window, under **Component 1 (comp1) > Solid Mechanics (solid)** click **Linear Elastic Material 1**.
- 5 In the **Settings** window for **Linear Elastic Material**, click to expand the **Energy Dissipation** section.
- 6 Select the **Calculate dissipated energy** checkbox.

#### *Thermal Expansion 1*



- 1 In the **Physics** toolbar, click  **Attributes** and choose **Thermal Expansion**.
- 2 In the **Settings** window for **Thermal Expansion**, locate the **Model Input** section.

3 From the  $T$  list, choose **User defined**. In the associated text field, type  $\text{thermLC}(t)$ .


#### *Linear Elastic Material 1*

In the **Model Builder** window, click **Linear Elastic Material 1**.


#### *Creep 1*

- 1 In the **Physics** toolbar, click  **Attributes** and choose **Creep**.
- 2 In the **Settings** window for **Creep**, locate the **Domain Selection** section.
- 3 From the **Selection** list, choose **Solder**.
- 4 Locate the **Model Input** section. From the  $T$  list, choose **User defined**. In the associated text field, type  $\text{thermLC}(t)$ .
- 5 Locate the **Creep Model** section. From the **Material model** list, choose **Garofalo (hyperbolic sine)**.
- 6 Find the **Thermal effects** subsection. From the  $g(T)$  list, choose **Arrhenius**.
- 7 In the  $Q$  text field, type 53200.
- 8 Locate the **Time Stepping** section. From the **Method** list, choose **Forward Euler**.
- 9 Click the  **Zoom Extents** button in the **Graphics** toolbar.

#### *Symmetry 1*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Symmetry**.
- 2 Select Boundaries 19 and 20 only.

#### *Roller 1*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Roller**.
- 2 Select Boundary 2 only.

## **MATERIALS**

#### *PCB*

- 1 In the **Model Builder** window, under **Component 1 (comp1)** right-click **Materials** and choose **Blank Material**.
- 2 In the **Settings** window for **Material**, type PCB in the **Label** text field.
- 3 Locate the **Geometric Entity Selection** section. From the **Selection** list, choose **Rectangle 1**.

4 Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	E	22 [GPa]	Pa	Young's modulus and Poisson's ratio
Poisson's ratio	nu	0.4	I	Young's modulus and Poisson's ratio
Density	rho	0	kg/m <sup>3</sup>	Basic
Coefficient of thermal expansion	alpha_iso ; alpha_ii = alpha_iso, alpha_ij = 0	21e-6	I/K	Basic

### Copper

- 1 Right-click **Materials** and choose **Blank Material**.
- 2 In the **Settings** window for **Material**, type Copper in the **Label** text field.
- 3 Locate the **Geometric Entity Selection** section. From the **Selection** list, choose **Rectangle 3**.
- 4 Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	E	141 [GPa]	Pa	Young's modulus and Poisson's ratio
Poisson's ratio	nu	0.35	I	Young's modulus and Poisson's ratio
Density	rho	0	kg/m <sup>3</sup>	Basic
Coefficient of thermal expansion	alpha_iso ; alpha_ii = alpha_iso, alpha_ij = 0	16.6e-6	I/K	Basic

### Solder

- 1 Right-click **Materials** and choose **Blank Material**.
- 2 In the **Settings** window for **Material**, type Solder in the **Label** text field.
- 3 Locate the **Geometric Entity Selection** section. From the **Selection** list, choose **Solder**.
- 4 Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	E	50 [GPa]	Pa	Young's modulus and Poisson's ratio
Poisson's ratio	nu	0.4		Young's modulus and Poisson's ratio
Density	rho	0	kg/m <sup>3</sup>	Basic
Coefficient of thermal expansion	alpha_iso ; alpha_ii = alpha_iso, alpha_ij = 0	21e-6	1/K	Basic
Creep rate coefficient	A_gar	262000	1/s	Garofalo (hyperbolic sine)
Reference stress	sigRef_gar	39.1 [MPa]	N/m <sup>2</sup>	Garofalo (hyperbolic sine)
Garofalo n parameter	n_gar	6.19		Garofalo (hyperbolic sine)

### NiCr

- 1 Right-click **Materials** and choose **Blank Material**.
- 2 In the **Settings** window for **Material**, type NiCr in the **Label** text field.
- 3 Locate the **Geometric Entity Selection** section. From the **Selection** list, choose **NiCr**.
- 4 Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	E	170 [GPa]	Pa	Young's modulus and Poisson's ratio
Poisson's ratio	nu	0.31		Young's modulus and Poisson's ratio

Property	Variable	Value	Unit	Property group
Density	rho	0	kg/m <sup>3</sup>	Basic
Coefficient of thermal expansion	alpha_iso ; alpha_ii = alpha_iso, alpha_ij = 0	13e-6	1/K	Basic

### Alumina

- 1 Right-click **Materials** and choose **Blank Material**.
- 2 In the **Settings** window for **Material**, type Alumina in the **Label** text field.
- 3 Locate the **Geometric Entity Selection** section. From the **Selection** list, choose **Rectangle 2**.
- 4 Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	E	300 [GPa]	Pa	Young's modulus and Poisson's ratio
Poisson's ratio	nu	0.22	1	Young's modulus and Poisson's ratio
Density	rho	0	kg/m <sup>3</sup>	Basic
Coefficient of thermal expansion	alpha_iso ; alpha_ii = alpha_iso, alpha_ij = 0	8e-6	1/K	Basic


### MESH 1

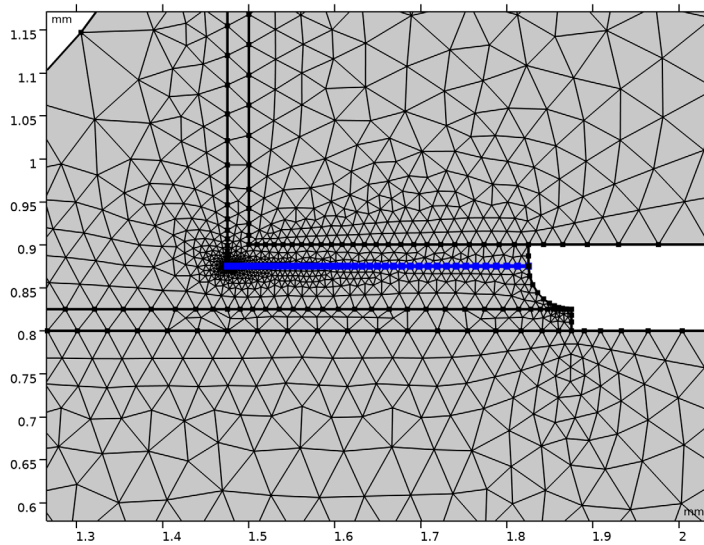
- 1 In the **Model Builder** window, under **Component 1 (comp1)** click **Mesh 1**.
- 2 In the **Settings** window for **Mesh**, locate the **Physics-Controlled Mesh** section.
- 3 From the **Element size** list, choose **Finer**.

### Free Triangular 1

In the **Mesh** toolbar, click  **Free Triangular**.

### *Distribution 1*

- 1 Right-click **Free Triangular 1** and choose **Distribution**.
- 2 Select Boundary 8 only.
- 3 In the **Settings** window for **Distribution**, locate the **Distribution** section.
- 4 From the **Distribution type** list, choose **Predefined**.
- 5 In the **Number of elements** text field, type 50.
- 6 In the **Element ratio** text field, type 0.1.
- 7 Click  **Build All**.




## **STUDY 1**

### *Step 1: Time Dependent*

Simulate a time history of 6 cycles.

- 1 In the **Model Builder** window, under **Study 1** click **Step 1: Time Dependent**.
- 2 In the **Settings** window for **Time Dependent**, locate the **Study Settings** section.
- 3 In the **Output times** text field, type range (0, 10, 60\*60).
- 4 From the **Tolerance** list, choose **User controlled**.
- 5 In the **Relative tolerance** text field, type 1e-4.
- 6 In the **Model Builder** window, click **Study 1**.
- 7 In the **Settings** window for **Study**, type Time History in the **Label** text field.



### *Solution 1 (soll)*

- 1 In the **Study** toolbar, click  **Show Default Solver**.  
Force strict time stepping in order to improve the creep results.
- 2 In the **Model Builder** window, expand the **Solution 1 (soll)** node, then click **Time-Dependent Solver 1**.
- 3 In the **Settings** window for **Time-Dependent Solver**, click to expand the **Time Stepping** section.
- 4 From the **Steps taken by solver** list, choose **Strict**.
- 5 In the **Model Builder** window, expand the **Time History > Solver Configurations > Solution 1 (soll) > Time-Dependent Solver 1** node.
- 6 Right-click **Time History** and choose **Compute**.

Set preferred units for result presentation.

## **RESULTS**

### *Preferred Units 1*

- 1 In the **Results** toolbar, click  **Configurations** and choose **Preferred Units**.
- 2 In the **Settings** window for **Preferred Units**, locate the **Units** section.
- 3 Click  **Add Physical Quantity**.
- 4 In the **Physical Quantity** dialog, select **Solid Mechanics > Stress tensor (N/m<sup>2</sup>)** in the tree.
- 5 Click **OK**.
- 6 In the **Settings** window for **Preferred Units**, locate the **Units** section.
- 7 In the table, enter the following settings:

Quantity	Unit	Preferred unit
Stress tensor	N/m <sup>2</sup>	MPa

- 8 Click  **Apply**.

### *Surface 1*



In the **Model Builder** window, expand the **Stress (solid)** node.

### *Deformation*

- 1 In the **Model Builder** window, expand the **Surface 1** node.
- 2 Right-click **Deformation** and choose **Enable**.
- 3 In the **Settings** window for **Deformation**, locate the **Scale** section.

4 Select the **Scale factor** checkbox. In the associated text field, type 20.

### RESULT TEMPLATES

- 1 In the **Results** toolbar, click  **Result Templates** to open the **Result Templates** window.
- 2 Go to the **Result Templates** window.
- 3 In the tree, select **Time History/Solution 1 (sol1) > Solid Mechanics > Equivalent Creep Strain (solid)**.
- 4 Click the **Add Result Template** button in the window toolbar.
- 5 In the **Results** toolbar, click  **Result Templates** to close the **Result Templates** window.

### RESULTS

#### *Surface 1*

Display creep strain history. The shear component gives the largest contribution to the equivalent creep strain.

#### *Creep Strain*

- 1 In the **Model Builder** window, expand the **Equivalent Creep Strain (solid)** node.
- 2 Right-click **Results** and choose **ID Plot Group**.
- 3 In the **Settings** window for **ID Plot Group**, type Creep Strain in the **Label** text field.

#### *Point Graph 1*

- 1 Right-click **Creep Strain** and choose **Point Graph**.
- 2 In the **Settings** window for **Point Graph**, locate the **Selection** section.
- 3 From the **Selection** list, choose **Point 1**.
- 4 Click **Replace Expression** in the upper-right corner of the **y-Axis Data** section. From the menu, choose **Component 1 (comp1) > Solid Mechanics > Strain > solid.eceGp - Equivalent creep strain - 1**.
- 5 Click to expand the **Legends** section. Select the **Show legends** checkbox.
- 6 From the **Legends** list, choose **Manual**.
- 7 In the table, enter the following settings:

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<b>Legends</b>
Effective

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#### *Point Graph 2*

- 1 Right-click **Point Graph 1** and choose **Duplicate**.

- 2 In the **Settings** window for **Point Graph**, click **Replace Expression** in the upper-right corner of the **y-Axis Data** section. From the menu, choose **Component 1 (comp1) > Solid Mechanics > Strain > Creep strain tensor, local coordinate system > solid.eclGp12 - Creep strain tensor, local coordinate system, 12-component**.
- 3 Locate the **Legends** section. In the table, enter the following settings:

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#### Legends

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Shear


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#### *Creep Strain*


- 1 In the **Model Builder** window, click **Creep Strain**.
- 2 In the **Settings** window for **ID Plot Group**, locate the **Legend** section.
- 3 From the **Position** list, choose **Upper left**.
- 4 In the **Creep Strain** toolbar, click  **Plot**.

Display stress-strain hysteresis of the shear behavior.


#### *Shear Hysteresis*

- 1 In the **Results** toolbar, click  **ID Plot Group**.
- 2 In the **Settings** window for **ID Plot Group**, type **Shear Hysteresis** in the **Label** text field.

#### *Point Graph 1*

- 1 Right-click **Shear Hysteresis** and choose **Point Graph**.
- 2 In the **Settings** window for **Point Graph**, locate the **Selection** section.
- 3 From the **Selection** list, choose **Point 1**.
- 4 Click **Replace Expression** in the upper-right corner of the **y-Axis Data** section. From the menu, choose **Component 1 (comp1) > Solid Mechanics > Stress > Stress tensor (spatial frame) - N/m<sup>2</sup> > solid.sGpxy - Stress tensor, xy-component**.
- 5 Locate the **x-Axis Data** section. From the **Parameter** list, choose **Expression**.
- 6 Click **Replace Expression** in the upper-right corner of the **x-Axis Data** section. From the menu, choose **Component 1 (comp1) > Solid Mechanics > Strain > Creep strain tensor, local coordinate system > solid.eclGp12 - Creep strain tensor, local coordinate system, 12-component**.
- 7 In the **Shear Hysteresis** toolbar, click  **Plot**.

#### ADD PHYSICS


- 1 In the **Home** toolbar, click  **Add Physics** to open the **Add Physics** window.

- 2 Go to the **Add Physics** window.
- 3 In the tree, select **Structural Mechanics > Fatigue (ftg)**.
- 4 Find the **Physics interfaces in study** subsection. In the table, clear the **Solve** checkbox for **Time History**.
- 5 Click the **Add to Component 1** button in the window toolbar.


#### **FATIGUE, COFFIN-MANSON**

In the **Settings** window for **Fatigue**, type **Fatigue**, **Coffin-Manson** in the **Label** text field.

##### *Strain-Life 1*

- 1 In the **Physics** toolbar, click  **Domains** and choose **Strain-Life**.
- 2 In the **Settings** window for **Strain-Life**, locate the **Domain Selection** section.
- 3 From the **Selection** list, choose **Solder**.
- 4 Locate the **Solution Field** section. From the **Physics interface** list, choose **Solid Mechanics (solid)**.
- 5 Locate the **Fatigue Model Selection** section. From the **Criterion** list, choose **Coffin-Manson**.
- 6 From the **Strain type** list, choose **Equivalent creep strain**.


#### **ADD PHYSICS**

- 1 Go to the **Add Physics** window.
- 2 In the tree, select **Structural Mechanics > Fatigue (ftg)**.
- 3 Find the **Physics interfaces in study** subsection. In the table, clear the **Solve** checkbox for **Time History**.
- 4 Click the **Add to Component 1** button in the window toolbar.
- 5 In the **Home** toolbar, click  **Add Physics** to close the **Add Physics** window.

#### **FATIGUE, MORROW**

In the **Settings** window for **Fatigue**, type **Fatigue**, **Morrow** in the **Label** text field.

##### *Energy-Based 1*

- 1 In the **Physics** toolbar, click  **Domains** and choose **Energy-Based**.
- 2 In the **Settings** window for **Energy-Based**, locate the **Domain Selection** section.
- 3 From the **Selection** list, choose **Solder**.
- 4 Locate the **Solution Field** section. From the **Physics interface** list, choose **Solid Mechanics (solid)**.

- 5 Locate the **Fatigue Model Selection** section. From the **Energy type** list, choose **Creep dissipation density**.

## MATERIALS

*Solder (mat3)*


- 1 In the **Model Builder** window, expand the **Component 1 (comp1) > Materials > Solder (mat3)** node, then click **Solder (mat3)**.
- 2 In the **Settings** window for **Material**, click to expand the **Material Properties** section.
- 3 In the **Material properties** tree, select **Solid Mechanics > Fatigue Behavior > Energy-Based > Morrow**.
- 4 Click **+ Add to Material**.
- 5 In the **Material properties** tree, select **Solid Mechanics > Fatigue Behavior > Strain-Based > Coffin–Manson**.
- 6 Click **+ Add to Material**.
- 7 In the **Model Builder** window, under **Component 1 (comp1) > Materials > Solder (mat3)** click **Morrow (fatigueEnergyMorrow)**.
- 8 In the **Settings** window for **Morrow**, locate the **Output Properties** section.
- 9 In the table, enter the following settings:


Property	Variable	Expression	Unit	Size
Fatigue energy coefficient	Wf_Morrow	55e6[J/m^3]	J/m <sup>3</sup>	x
Fatigue energy exponent	m_Morrow	-0.69		x

- 10 In the **Model Builder** window, under **Component 1 (comp1) > Materials > Solder (mat3)** click **Coffin–Manson (fatigueStrainCoffinManson)**.
- 11 In the **Settings** window for **Coffin–Manson**, locate the **Output Properties** section.
- 12 In the table, enter the following settings:

Property	Variable	Expression	Unit	Size
Fatigue ductility coefficient	epsilononf_CM	0.218		x
Fatigue ductility exponent	c_CM	-0.51		x

## ADD STUDY


- 1 In the **Home** toolbar, click  **Add Study** to open the **Add Study** window.
- 2 Go to the **Add Study** window.

- 3 Find the **Physics interfaces in study** subsection. In the table, clear the **Solve** checkbox for **Solid Mechanics (solid)**.
- 4 Find the **Studies** subsection. In the **Select Study** tree, select **Preset Studies for Selected Physics Interfaces > Fatigue**.
- 5 Click the **Add Study** button in the window toolbar.
- 6 In the **Home** toolbar, click  **Add Study** to close the **Add Study** window.

## FATIGUE

In the **Settings** window for **Study**, type **Fatigue** in the **Label** text field.

### *Step 1: Fatigue*

- 1 In the **Model Builder** window, under **Fatigue** click **Step 1: Fatigue**.
- 2 In the **Settings** window for **Fatigue**, locate the **Values of Dependent Variables** section.
- 3 Find the **Values of variables not solved for** subsection. From the **Settings** list, choose **User controlled**.
- 4 From the **Method** list, choose **Solution**.
- 5 From the **Study** list, choose **Time History, Time Dependent**.
- 6 From the **Time (s)** list, choose **From list**.
- 7 From the **Time (s)** selection list, select time steps from 3000 s to 3600 s.
- 8 In the **Study** toolbar, click  **Compute**.

Two new plot groups are created. They show the cycles to failure for each fatigue model, see [Figure 6](#) and [Figure 7](#).

## RESULTS

### *Cycles to Failure, Coffin-Manson*

- 1 In the **Settings** window for **2D Plot Group**, type **Cycles to Failure, Coffin-Manson** in the **Label** text field.
- 2 In the **Model Builder** window, expand the **Cycles to Failure, Coffin-Manson** node.

### *Marker 1*

- 1 In the **Model Builder** window, expand the **Results > Cycles to Failure, Coffin-Manson > Surface 1** node, then click **Marker 1**.
- 2 In the **Settings** window for **Marker**, locate the **Coloring and Style** section.
- 3 From the **Anchor point** list, choose **Lower right**.

### *Cycles to Failure, Morrow*

- 1 In the **Model Builder** window, under **Results** click **Cycles to Failure (ftg2)**.
- 2 In the **Settings** window for **2D Plot Group**, type **Cycles to Failure, Morrow** in the **Label** text field.
- 3 In the **Model Builder** window, expand the **Cycles to Failure, Morrow** node.

### *Marker 1*

- 1 In the **Model Builder** window, expand the **Results > Cycles to Failure, Morrow > Surface 1** node, then click **Marker 1**.
- 2 In the **Settings** window for **Marker**, locate the **Coloring and Style** section.
- 3 From the **Anchor point** list, choose **Lower right**.


## *Appendix — Geometry Modeling Instructions*

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### **GEOMETRY 1**

- 1 In the **Model Builder** window, under **Component 1 (comp1)** click **Geometry 1**.
- 2 In the **Settings** window for **Geometry**, locate the **Units** section.
- 3 From the **Length unit** list, choose **mm**.

### *Rectangle 1 (r1)*


- 1 In the **Geometry** toolbar, click  **Rectangle**.
- 2 In the **Settings** window for **Rectangle**, locate the **Size and Shape** section.
- 3 In the **Width** text field, type **3.1**.
- 4 In the **Height** text field, type **0.8**.
- 5 Locate the **Selections of Resulting Entities** section. Select the **Resulting objects selection** checkbox.

### *Rectangle 2 (r2)*


- 1 In the **Geometry** toolbar, click  **Rectangle**.
- 2 In the **Settings** window for **Rectangle**, locate the **Size and Shape** section.
- 3 In the **Width** text field, type **1.6**.
- 4 In the **Height** text field, type **0.55**.
- 5 Locate the **Position** section. In the **x** text field, type **1.5**.
- 6 In the **y** text field, type **0.9**.


- 7 Locate the **Selections of Resulting Entities** section. Select the **Resulting objects selection** checkbox.

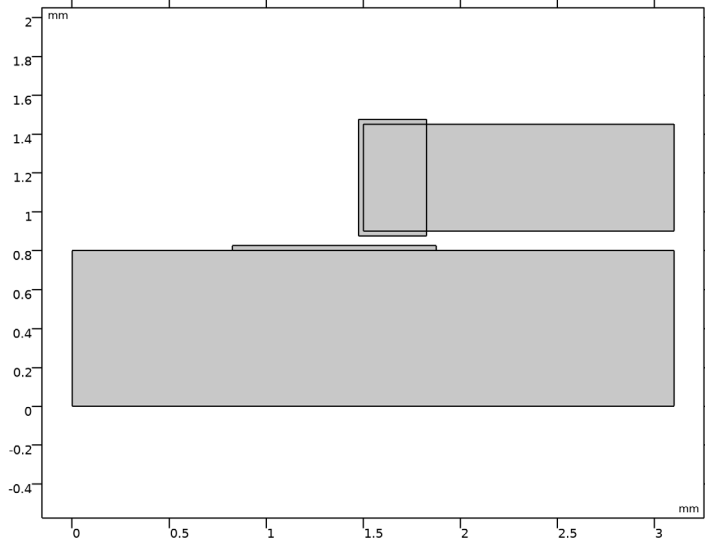
*Rectangle 3 (r3)*

- 1 In the **Geometry** toolbar, click  **Rectangle**.
- 2 In the **Settings** window for **Rectangle**, locate the **Size and Shape** section.
- 3 In the **Width** text field, type 1.05.
- 4 In the **Height** text field, type 0.025.
- 5 Locate the **Position** section. In the **x** text field, type 0.825.
- 6 In the **y** text field, type 0.8.
- 7 Locate the **Selections of Resulting Entities** section. Select the **Resulting objects selection** checkbox.



*Rectangle 4 (r4)*

- 1 In the **Geometry** toolbar, click  **Rectangle**.
- 2 In the **Settings** window for **Rectangle**, locate the **Size and Shape** section.
- 3 In the **Width** text field, type 0.35.
- 4 In the **Height** text field, type 0.6.
- 5 Locate the **Position** section. In the **x** text field, type 1.475.
- 6 In the **y** text field, type 0.875.
- 7 Locate the **Selections of Resulting Entities** section. Find the **Cumulative selection** subsection. Click **New**.
- 8 In the **New Cumulative Selection** dialog, type NiCr in the **Name** text field.
- 9 Click **OK**.


10 In the **Geometry** toolbar, click  **Build All**.



#### *Quadratic Bézier 1 (qb1)*

- 1 In the **Geometry** toolbar, click  **More Primitives** and choose **Quadratic Bézier**.
- 2 In the **Settings** window for **Quadratic Bézier**, locate the **Control Points** section.
- 3 In row **1**, set **x** to 0.825.
- 4 In row **1**, set **y** to 0.825.
- 5 In row **2**, set **x** to 1.35.
- 6 In row **2**, set **y** to 0.95.
- 7 In row **3**, set **x** to 1.475.
- 8 In row **3**, set **y** to 1.475.
- 9 Click  **Build Selected**.

#### *Polygon 1 (pol1)*

- 1 In the **Geometry** toolbar, click  **Polygon**.
- 2 In the **Settings** window for **Polygon**, locate the **Object Type** section.
- 3 From the **Type** list, choose **Open curve**.

4 Locate the **Coordinates** section. In the table, enter the following settings:

x (mm)	y (mm)
1.475	1.475
1.475	0.875
1.825	0.875

5 Click  **Build Selected**.

*Circular Arc 1 (ca1)*

1 In the **Geometry** toolbar, click  **More Primitives** and choose **Circular Arc**.

2 In the **Settings** window for **Circular Arc**, locate the **Center** section.

3 In the **x** text field, type 1.875.

4 In the **y** text field, type 0.875.

5 Locate the **Radius** section. In the **Radius** text field, type 0.05.

6 Locate the **Angles** section. In the **Start angle** text field, type 180.

7 In the **End angle** text field, type 270.

8 Click  **Build Selected**.

*Line Segment 1 (ls1)*

1 In the **Geometry** toolbar, click  **More Primitives** and choose **Line Segment**.

2 On the object **ca1**, select Point 2 only.

3 In the **Settings** window for **Line Segment**, locate the **Endpoint** section.

4 Click to select the  **Activate Selection** toggle button for **End vertex**.

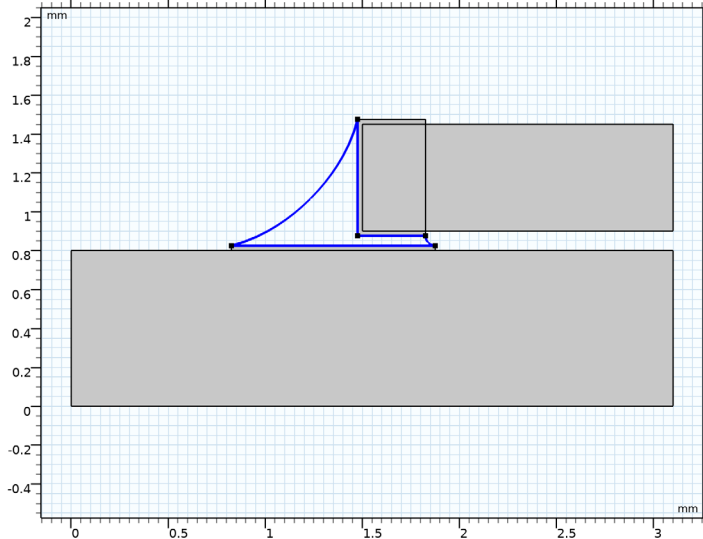
5 On the object **qb1**, select Point 1 only.

6 Click  **Build Selected**.

*Convert to Solid 1 (csol1)*

1 In the **Geometry** toolbar, click  **Conversions** and choose **Convert to Solid**.

2 Select the objects **cal**, **Isl**, **poll**, and **qbl** only.



3 In the **Settings** window for **Convert to Solid**, locate the **Selections of Resulting Entities** section.

4 Find the **Cumulative selection** subsection. Click **New**.

5 In the **New Cumulative Selection** dialog, type **Solder** in the **Name** text field.

6 Click **OK**.

7 In the **Settings** window for **Convert to Solid**, click  **Build Selected**.

#### *Point 1 (pt1)*

1 In the **Geometry** toolbar, click  **Point**.

2 In the **Settings** window for **Point**, locate the **Point** section.

3 In the **x** text field, type 1.48.

4 In the **y** text field, type 0.87.

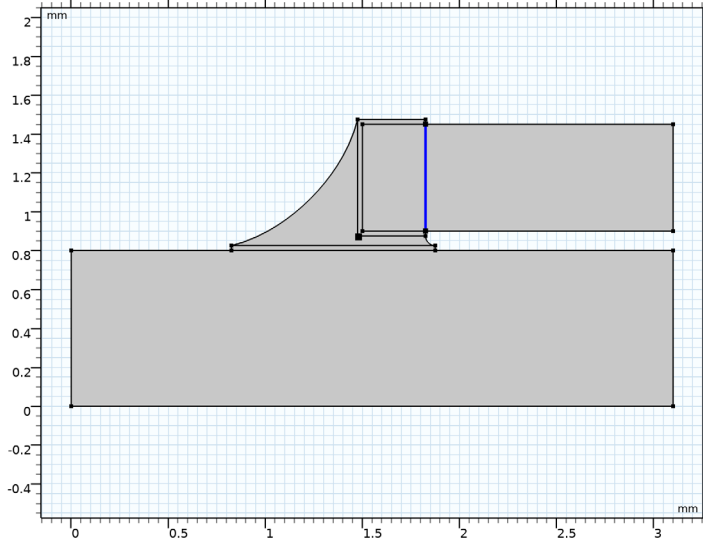
5 Locate the **Selections of Resulting Entities** section. Select the **Resulting objects selection** checkbox.


6 Click  **Build Selected**.

#### *Ignore Edges 1 (ige1)*

1 In the **Geometry** toolbar, click  **Virtual Operations** and choose **Ignore Edges**.

2 On the object **fin**, select Boundary 14 only.



3 In the **Geometry** toolbar, click  **Build All**.

*Form Union (fin)*

1 Click  **Build All**.

2 In the **Model Builder** window, click **Form Union (fin)**.

