

# Steady-State 2D Axisymmetric Heat Transfer with Conduction

The following example illustrates how to build and solve a conductive heat transfer problem using the Heat Transfer interface. The model, taken from a NAFEMS benchmark collection, shows an axisymmetric steady-state thermal analysis. As opposed to the NAFEMS benchmark model, the COMSOL Multiphysics simulation uses the kelvin temperature unit instead of degrees Celsius.

# Model Definition

The modeling domain describes the cross section of a 3D solid as shown in Figure 1.

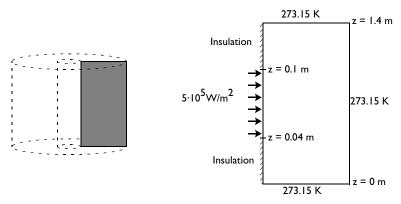


Figure 1: Model geometry and boundary conditions.

You set three types of boundary conditions:

- · Prescribed heat flux
- Insulation/Symmetry
- Prescribed temperature

The governing equation for this problem is the steady-state heat equation for conduction with the volumetric heat source set to zero:

$$\nabla \cdot (-k\nabla T) = 0$$

The thermal conductivity k is 52 W/(m·K).

The plot in Figure 2 shows the temperature distribution.

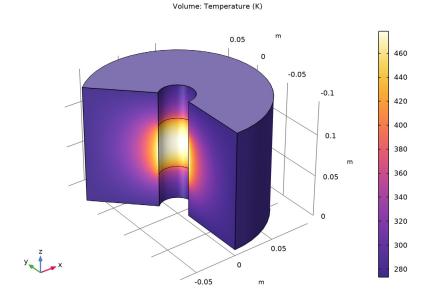


Figure 2: Temperature distribution.

The benchmark result for the target location (r = 0.04 m and z = 0.04 m) is a temperature of 59.82 °C (332.97 K). The COMSOL Multiphysics model, using a default mesh with about 540 elements, gives a temperature of 332.96 K at the same location.

# Reference

1. A.D. Cameron, J.A. Casey, and G.B. Simpson, NAFEMS Benchmark Tests for Thermal Analysis (Summary), NAFEMS, 1986.

Application Library path: Heat\_Transfer\_Module/Tutorials,\_Conduction/ cylinder\_conduction

From the File menu, choose New.

#### NEW

In the New window, click Model Wizard.

## MODEL WIZARD

- I In the Model Wizard window, click 2D Axisymmetric.
- 2 In the Select Physics tree, select Heat Transfer>Heat Transfer in Solids (ht).
- 3 Click Add.
- 4 Click 🔵 Study.
- 5 In the Select Study tree, select General Studies>Stationary.
- 6 Click **Done**.

## GEOMETRY I

Rectangle I (rI)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 0.08.
- 4 In the Height text field, type 0.14.
- **5** Locate the **Position** section. In the **r** text field, type 0.02.

Point I (ptl)

- I In the Geometry toolbar, click Point.
- 2 In the Settings window for Point, locate the Point section.
- **3** In the **r** text field, type 0.02 0.02.
- 4 In the z text field, type 0.04 0.1.
- 5 In the Geometry toolbar, click **Build All**.

## HEAT TRANSFER IN SOLIDS (HT)

Solid 1

- I In the Model Builder window, under Component I (compl)>Heat Transfer in Solids (ht) click Solid I.
- 2 In the Settings window for Solid, locate the Heat Conduction, Solid section.

- **3** From the k list, choose **User defined**. In the associated text field, type 52.
- **4** Locate the **Thermodynamics, Solid** section. From the  $C_p$  list, choose **User defined**. From the  $\rho$  list, choose **User defined**.

## Temperature I

- I In the Physics toolbar, click Boundaries and choose Temperature.
- 2 In the Settings window for Temperature, locate the Temperature section.
- **3** In the  $T_0$  text field, type 273.15[K].
- 4 Select Boundaries 2, 5, and 6 only.

## Heat Flux 1

- I In the Physics toolbar, click Boundaries and choose Heat Flux.
- 2 In the Settings window for Heat Flux, locate the Heat Flux section.
- **3** In the  $q_0$  text field, type 5e5.
- 4 Select Boundary 3 only.

## MESH I

In the Model Builder window, under Component I (compl) right-click Mesh I and choose Build All.

#### STUDY I

In the **Home** toolbar, click **Compute**.

## RESULTS

## Temperature (ht)

The default plot shows the temperature field on the 2D slice.

I Click the **Zoom Extents** button in the **Graphics** toolbar.

## ADD PREDEFINED PLOT

- I In the Home toolbar, click Windows and choose Add Predefined Plot.
- 2 Go to the Add Predefined Plot window.

Add a predefined plot showing a 3D temperature distribution on a revolved surface; compare with Figure 2.

- 3 In the tree, select Study I/Solution I (soll)>Heat Transfer in Solids>Temperature (ht).
- 4 Click Add Plot in the window toolbar.

#### RESULTS

Temperature 3D (ht)

- I In the **Settings** window for **3D Plot Group**, type Temperature 3D (ht) in the **Label** text field.
- 2 Click the **Zoom Extents** button in the **Graphics** toolbar.

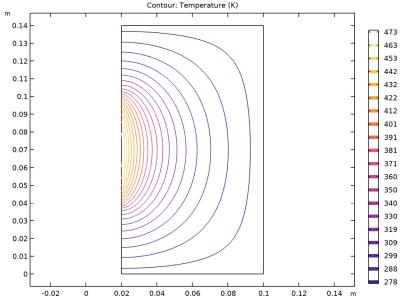
  Add another predefined plot showing isothermal contours in 2D section.

## ADD PREDEFINED PLOT

- I In the Home toolbar, click Windows and choose Add Predefined Plot.
- 2 Go to the Add Predefined Plot window.
- 3 In the tree, select Study I/Solution I (soll)>Heat Transfer in Solids> Isothermal Contours (ht).
- 4 Click Add Plot in the window toolbar.

## RESULTS

Isothermal Contours (ht)



To obtain the temperature value at any point, just click at that point in the **Graphics** window; The result appears in the Table window at the bottom of the COMSOL Desktop.

Alternatively, you can create a Cut Point dataset and Point Evaluation feature as follows.

## Cut Point 2D I

- I In the Results toolbar, click Cut Point 2D.
- 2 In the Settings window for Cut Point 2D, locate the Point Data section.
- 3 In the R text field, type 0.04.
- 4 In the **Z** text field, type 0.04.

## Point Evaluation 1

- I In the Results toolbar, click 8.85 Point Evaluation.
- 2 In the Settings window for Point Evaluation, locate the Data section.
- 3 From the Dataset list, choose Cut Point 2D 1.
- 4 Click **= Evaluate**.

## TABLE I

I Go to the Table I window.

The result is approximately 333 K.