

Leaky Modes in a Microstructured Optical Fiber

In a regular optical fiber, light is confined to the core region of the fiber through total internal reflection. That is, the refractive index is higher in the core than in the surrounding cladding. Then if the wave hits the core-cladding interface with an angle from the interface normal that is larger than a certain critical angle, the wave will be perfectly reflected. Thus, ideally, this type of dielectric waveguide is lossless.

By the end of the seventies, it was realized that light could also be guided without relying on total internal reflection. If the core of the fiber was surrounded by concentric layers of materials with alternating high and low refractive indices, the modes can propagate along the fiber without losses, even though the core refractive index is lower than the refractive index of the exterior cladding. This type of fiber is called a Bragg fiber.

Also if you create a regular lattice of air holes in a silica fiber, a similar type of guiding as for the Bragg fiber can be created. This time, though, the guiding occurs through the photonic band gap effect. Consequently, these fibers are called photonic band gap fibers (PBGFs) or photonic crystal fibers (PCFs).

An advantage with these new kinds of fibers is that you can design them to make the guided mode overlap mainly with the air regions. This can potentially reduce the loss in the fiber and it makes the fibers less susceptible to optically nonlinear effects.

In reality, though, the band gap structures and the layer structures cannot be made infinitely large. Thus, there is always some loss associated with the modes in these microstructured optical fibers (MOFs). Thus, when designing these types of fibers, it is of great importance to be able to calculate the loss associated with a certain fiber design.

This model will demonstrate how to use COMSOL for making a mode analysis of a lossy microstructured optical fiber. The geometry is shown in Figure 1.

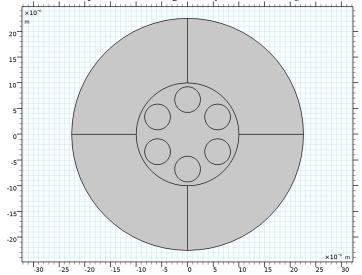


Figure 1: A microstructured optical fiber. The whole structure consists of silica, except for the small holes that consist of air. The outermost layer is used for the perfectly matched layer (PML), used in the first part of the simulation.

The fiber design implemented in this model has been used in several scientific papers for evaluating different computational methods. See for instance Ref. 1.

Figure 2 shows one of the two degenerate HE_{11} -like modes. As this is a mixed mode, both the electric and magnetic field have longitudinal field components, although their magnitude is much smaller than the tangential field components.



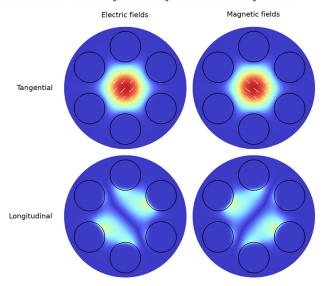


Figure 2: This graph shows the norm of the tangential and longitudinal electric and magnetic fields for one of the two degenerate HE_{11} -like modes. To make the longitudinal components visible, they are scaled by a factor of ten relative the tangential field components. The white arrows indicate the tangential electric and magnetic field directions.

This type of fiber is a high-index core fiber, where the core of the fiber has a higher refractive index than the surrounding air-hole ring. Thus, the guiding here could be said to be due to that the local effective index is higher in the core than in the surrounding airhole ring.

You could also calculate the in-plane wavelength

$$\lambda_{T,i} = \frac{\lambda}{\sqrt{n^2 - n_i^2}},\tag{1}$$

where λ is the vacuum wavelength, n is the refractive index of silica, and n_i is the effective index of mode i. For the modes with an effective index close to the silica refractive index, the in-plane wavelength will be much larger than the separation between the air holes.

Thus, less radiation can leak through the air-hole ring for those modes. When the effective index for the modes decreases, the in-plane wavelength gets smaller and more radiation can leak between the air holes.

Figure 3 shows the TE_{01} -like mode. A pure TE_{01} mode for a cylindrically symmetric waveguide, has rotational invariance. This TE_{01} -like mode has almost rotational invariance, with the electric field mainly polarized in the φ direction whereas the magnetic field has both a radial and longitudinal component.

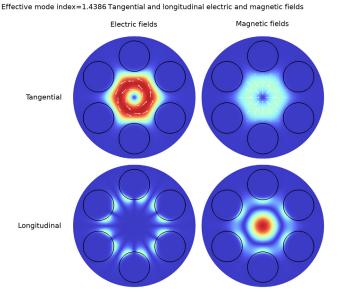
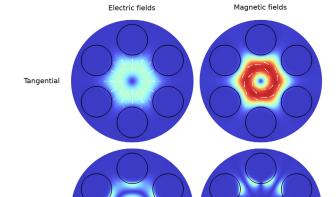


Figure 3: The TE_{01} -like mode.

Another mode example is the TM_{01} -like mode, shown in Figure 4. Again, the field has almost rotational invariance. However, this time the electric field has both radial and longitudinal components, whereas the magnetic field has mainly a φ -component.



Effective mode index=1.4384 Tangential and longitudinal electric and magnetic fields

Figure 4: The TM_{01} -like mode.

Longitudinal

Table 1 shows the effective indices for the ten modes found in the mode analysis studies. The first column indicates the mode's type. The second column, marked with PML, shows the result for the study performed with a PML to truncate the computation domain. The third column, shows the result for the study using a Scattering boundary condition to truncate the computation domain.

TABLE I: COMPARISON OF EFFECTIVE INDICES.

MODE	PML	SBC
HEII	1.44539464-3.18614991E-8i	1.44539464-4.11689498E-8i
HEII	1.44539457-3.18633520E-8i	1.44539457-4.04012333E-8i
TE01	1.43858017-5.33455430E-7i	1.43858018-5.10491523E-7i
HE21	1.43844305-9.69173128E-7i	1.43844283-1.18177443E-6i
HE21	1.43844288-9.69308091E-7i	1.43844267-1.17332710E-6i
TM01	1.43836454-1.40665012E-6i	1.43836412-1.82745066E-6i
HE31	1.42925271-8.69622507E-6i	1.42925277-8.57312825E-6i

TABLE I: COMPARISON OF EFFECTIVE INDICES.

MODE	PML	SBC
EHII	1.42995211-1.58836822E-5i	1.42994979-1.14846411E-5i
EHII	1.42995194-1.58836249E-5i	1.42995007-1.17868693E-5i
HE31	1.43039731-2.15696869E-5i	1.43039277-1.42539834E-5i

As seen in the table, the real parts agree for the first 5–6 decimals, whereas for the much smaller imaginary parts only the orders of magnitude agree. Also when comparing to values reported in Ref. 1, the same kind of agreement is found.

Notes About the COMSOL Implementation

In the first part of the of this simulation, PMLs are used to truncate the simulation domain. To efficiently absorb the wave in the PML, the wavelength corresponding to the wave vector component in the radial direction should be provided. This wavelength is stated in Equation 1 and implemented by the parameter w1r, where an estimation of the largest effective index is used.

In the second part of this modeling task, the Scattering boundary condition is used for truncating the simulation domain. Normally, when the Scattering boundary condition is used, it is assumed that the scattered wave reaching the boundary propagates with a wave vector close to the normal direction to the boundary. However, when we do a mode analysis, we know that the mode will also propagate in the out-of-plane direction, which is tangential to the boundary where the Scattering boundary condition is applied. Thus, the wave vector component in the normal direction to the boundary is

$$k_n = \sqrt{k^2 - \beta^2},$$

where k is the material wave number and β is the propagation constant for the mode. To make sure that this expression is used, enable the Subtract propagation constant from material wave number check box in the Mode Analysis section in the Settings for the **Scattering Boundary Condition** feature.

Reference

1. H.P. Uranus and H.J.W.M. Hoekstra, "Modelling of microstructured waveguides using a finite-element-based vectorial mode solver with transparent boundary conditions," Optics Express, vol. 12, no. 12, pp. 2795–2809, 2004.

Application Library path: Wave Optics Module/Verification Examples/ microstructured_optical_fiber

Modeling Instructions

From the **File** menu, choose **New**.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click **2** 2D.
- 2 In the Select Physics tree, select Optics>Wave Optics>Electromagnetic Waves, Frequency Domain (ewfd).
- 3 Click Add.
- 4 Click Study.
- 5 In the Select Study tree, select Preset Studies for Selected Physics Interfaces> Mode Analysis.
- 6 Click M Done.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click Load from File.
- 4 Browse to the model's Application Libraries folder and double-click the file microstructured_optical_fiber_parameters.txt.

The parameter wlr, the in-plane wavelength, will be used in the definition of the perfectly matched layer (PML).

GEOMETRY I

Start building the geometry. Add a circle for the computation domain and then a smaller circle that represents the air holes. The air-hole circle is rotated in steps of 60 degrees. In total, six air holes will be added.

Circle I (c1)

- I In the Geometry toolbar, click Circle.
- 2 In the Settings window for Circle, locate the Size and Shape section.
- **3** In the **Radius** text field, type rb+wlr.
- **4** Click to expand the **Layers** section. In the table, enter the following settings:

Layer name	Thickness (m)
Layer 1	wlr

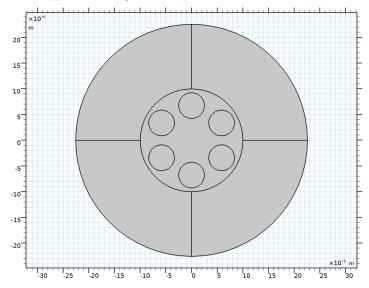
Circle 2 (c2)

- I In the Geometry toolbar, click Circle.
- 2 In the Settings window for Circle, locate the Size and Shape section.
- 3 In the Radius text field, type d/2.
- 4 Locate the Position section. In the y text field, type -Delta. Now, give the selection a name that can be referred to later.
- 5 Locate the Selections of Resulting Entities section. Find the Cumulative selection subsection. Click New.
- 6 In the New Cumulative Selection dialog box, type Air Holes in the Name text field.
- 7 Click OK.

Rotate I (rot1)

- I In the Geometry toolbar, click Transforms and choose Rotate.
- 2 Select the object c2 only.
- 3 In the Settings window for Rotate, locate the Rotation section.
- 4 In the Angle text field, type range (0,60,300).
- 5 Locate the Selections of Resulting Entities section. Find the Cumulative selection subsection. From the Contribute to list, choose Air Holes.

6 Click **Build All Objects**.



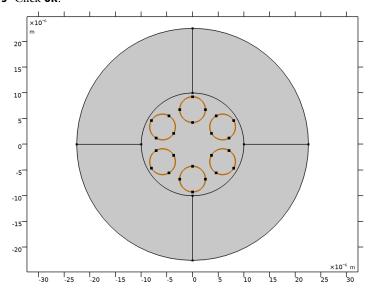
Add a selection for the air hole boundaries. This selection will be used later, when setting up the plots.

DEFINITIONS

Air Hole Boundaries

- I In the Definitions toolbar, click hadjacent.
- 2 In the Settings window for Adjacent, type Air Hole Boundaries in the Label text field.
- 3 Locate the Input Entities section. Under Input selections, click + Add.
- 4 In the Add dialog box, select Air Holes in the Input selections list.

5 Click OK.



MATERIALS

Now, add the materials.

Silica

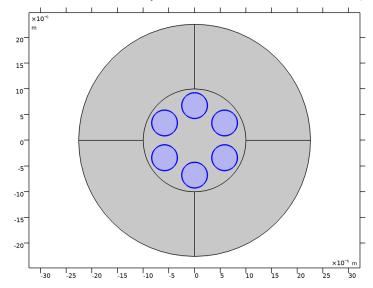
- I In the Model Builder window, under Component I (compl) right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type Silica in the Label text field.
- **3** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Refractive index, real part	n_iso ; nii = n_iso, nij = 0	nbg	I	Refractive index
Refractive index, imaginary part	ki_iso ; kiii = ki_iso, kiij = 0	0	1	Refractive index

Air

- I Right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type Air in the Label text field.

3 Locate the Geometric Entity Selection section. From the Selection list, choose Air Holes.



4 Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Refractive index, real part	n_iso ; nii = n_iso, nij = 0	nair	1	Refractive index
Refractive index, imaginary part	ki_iso ; kiii = ki_iso, kiij = 0	0	1	Refractive index

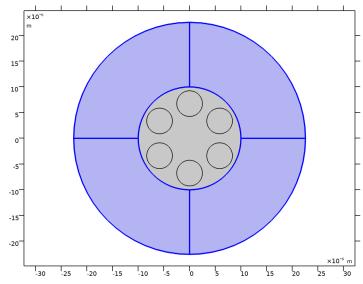
DEFINITIONS

In the first part of the model, a perfectly matched layer (PML) will be used for truncating the computation domain.

Perfectly Matched Layer I (pml1)

I In the Definitions toolbar, click Perfectly Matched Layer.

2 Select Domains 1–4 only.



- 3 In the Settings window for Perfectly Matched Layer, locate the Geometry section.
- 4 From the Type list, choose Cylindrical.
- 5 Locate the Scaling section. From the Typical wavelength from list, choose User defined.
- 6 In the **Typical wavelength** text field, type wlr. This parameter approximates the in-plane wavelength.

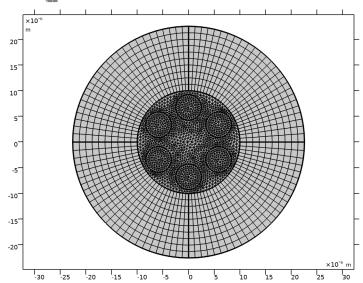
STUDY I

Step 1: Mode Analysis

- I In the Model Builder window, under Study I click Step I: Mode Analysis.
- 2 In the Settings window for Mode Analysis, locate the Study Settings section.
- 3 In the Mode analysis frequency text field, type c_const/wl.
- 4 From the Mode search method list, choose Region, as we will search for the complex effective indices in a rectangular region defined by the following parameters.
- 5 In the Approximate number of modes text field, type 10.
- 6 Find the Search region subsection. In the Smallest real part text field, type neffMin.
- 7 In the Largest real part text field, type neffMax.
- 8 In the Smallest imaginary part text field, type -3e-5.

MESH I

- I In the Model Builder window, under Component I (compl) click Mesh I.
- 2 In the Settings window for Mesh, locate the Physics-Controlled Mesh section.
- 3 From the Element size list, choose Extremely fine.
- 4 Click **Build All**.



The mesh plot shows that the PML domains have been meshed with a mapped mesh.

STUDY I

Step 1: Mode Analysis

In the **Home** toolbar, click **Compute**.

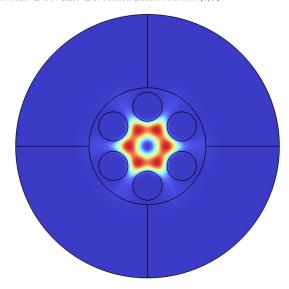
RESULTS

Electric Field (ewfd)

- I In the Settings window for 2D Plot Group, locate the Color Legend section.
- 2 Clear the Show legends check box, as the absolute amplitude of the mode field is not important.
- 3 In the Electric Field (ewfd) toolbar, click Plot.
- 4 Click the Show Grid button in the Graphics toolbar, to remove some more information that is not necessary in the plot.

5 Click the **Zoom Extents** button in the **Graphics** toolbar.

Effective mode index=1.4304-2.1574E-5i Surface: Electric field norm (V/m)



As seen, the mode field is localized to the central high-index region, with only a very small part of the field penetrating in between the holes.

The effective index is shown in the plot title. As seen, it is a complex number, where the imaginary part represents attenuation of the wave as it propagates along the fiber due to radiation leaking through the air-hole ring. let us evaluate the effective indices for the different modes.

Global Evaluation 1

- I In the Results toolbar, click (8.5) Global Evaluation.
- 2 In the Settings window for Global Evaluation, click Replace Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (compl)> Electromagnetic Waves, Frequency Domain>Global>ewfd.neff - Effective mode index.
- 3 Click **= Evaluate**.

TABLE

I Go to the Table window.

2 Click Full Precision in the window toolbar.

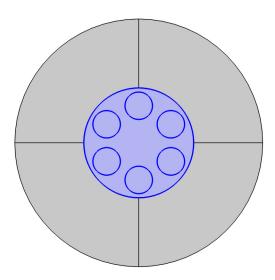
The imaginary part of the effective index is larger for the modes with a lower real part of the effective index. Those modes have a smaller in-plane wavelength and are, thus, more loosely bound to the central high-index region.

The effective indices in the table should be very close to the values in the second column of Table 1.

ELECTROMAGNETIC WAVES, FREQUENCY DOMAIN (EWFD)

Now, replace the PML with a Scattering boundary condition (SBC).

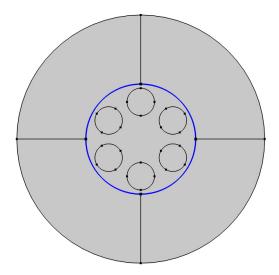
- I In the Model Builder window, under Component I (compl) click Electromagnetic Waves, Frequency Domain (ewfd).
- **2** Select Domains 5–11 only.



Scattering Boundary Condition I

- I In the Physics toolbar, click Boundaries and choose Scattering Boundary Condition.
- 2 In the Settings window for Scattering Boundary Condition, locate the Boundary Selection section.

3 From the Selection list, choose All boundaries.



- 4 Locate the Scattering Boundary Condition section. From the Scattered wave type list, choose Cylindrical wave.
- 5 Click to expand the Mode Analysis section. Select the Subtract propagation constant from material wave number check box, to subtract the mode propagation constant from the material wave number when calculating the wave vector component in the radial (normal) direction.
- 6 In the Home toolbar, click **Compute**.

RESULTS

Global Evaluation 1

- I In the Model Builder window, under Results>Derived Values click Global Evaluation I.
- 2 In the Settings window for Global Evaluation, click **= Evaluate**. The effective indices in the table should be very close to the values in the third column of Table 1.

TABLE

I Go to the **Table** window.

Comparing the effective indices from the PML and the SBC simulations, it is clear that the real parts agree up to 4-5 decimals, whereas the imaginary parts (that are much smaller in magnitude) only agree by the order of magnitude.

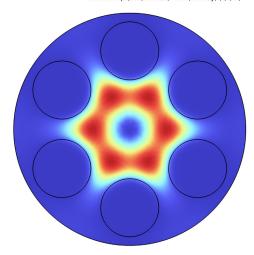
RESULTS

Now, add some additional plots, to make it possible to distinguish the different mode

Surface I

- I In the Model Builder window, expand the Results>Electric Field (ewfd) node, then click Surface 1.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type sqrt(abs(ewfd.Ex)^2+abs(ewfd.Ey)^2). This represents the norm of the tangential electric field.

Effective mode index=1.4304-1.4411E-5i Surface: sqrt(abs(ewfd.Ex)2+abs(ewfd.Ey)2) (V/m)



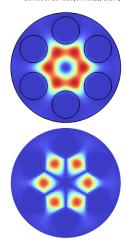
Surface 2

- I Right-click Results>Electric Field (ewfd)>Surface I and choose Duplicate.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type 10*abs(ewfd.Ez). This represents the norm of the longitudinal electric field. This component is scaled by a factor of ten, to make it visible when compared to the tangential electric field components.
- 4 Click to expand the Inherit Style section. From the Plot list, choose Surface 1.

- I Right-click Surface 2 and choose Translation.
- 2 In the Settings window for Translation, locate the Translation section.

- 3 In the y text field, type -2.1*rb.
- 4 Clear the Apply to dataset edges check box.
- 5 Click the **Zoom Extents** button in the **Graphics** toolbar.

Effective mode index=1.4304-1.4411E-5i Surface: sqrt(abs(ewfd.Ex)²+abs(ewfd.Ey)²) (V/m) Surface: 10*abs(ewfd.Ez) (V/m)



Surface 1, Surface 2

- I In the Model Builder window, under Results>Electric Field (ewfd), Ctrl-click to select Surface I and Surface 2.
- 2 Right-click and choose **Duplicate**.

Surface 3

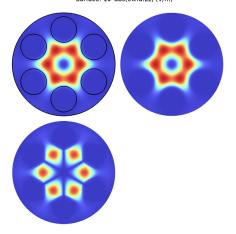
- I In the Settings window for Surface, locate the Expression section.
- 2 In the Expression text field, type sqrt(abs(ewfd.Hx)^2+abs(ewfd.Hy)^2). This represents the norm of the tangential magnetic field.

- I Right-click Surface 3 and choose Translation.
- 2 In the Settings window for Translation, locate the Translation section.
- 3 In the x text field, type 2.1*rb.
- 4 Clear the Apply to dataset edges check box.

5 Click the **Zoom Extents** button in the **Graphics** toolbar.

Surface: 10*abs(ewfd.Ez) (V/m) Surface: sqrt(abs(ewfd.Hx)2+abs(ewfd.Hy)2) (A/m)

Surface: 10*abs(ewfd.Ez) (V/m)



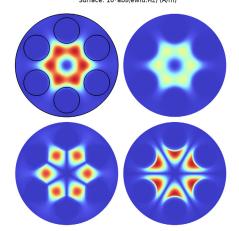
Surface 4

- I In the Model Builder window, expand the Results>Electric Field (ewfd)>Surface 4 node, then click Surface 4.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type 10*abs(ewfd.Hz). This represents the norm of the longitudinal magnetic field. Again, a scale factor of 10 is used here to make the longitudinal component visible when compared to the tangential components.
- 4 Locate the Inherit Style section. From the Plot list, choose Surface 3.

- I In the Model Builder window, click Translation I.
- 2 In the Settings window for Translation, locate the Translation section.

3 In the x text field, type 2.1*rb.

Surface: 10*abs(ewfd.Ez) (V/m) Surface: sqrt(abs(ewfd.Hx)2+abs(ewfd.Hy)2) (A/m) Surface: 10*abs(ewfd.Hz) (A/m)



Electric Field (ewfd)

- I In the Model Builder window, under Results click Electric Field (ewfd).
- 2 In the Settings window for 2D Plot Group, click to expand the Title section.
- 3 From the Title type list, choose Manual.
- 4 In the Title text area, type Tangential and longitudinal electric and magnetic fields.

Add arrow plots to visualize the polarization direction.

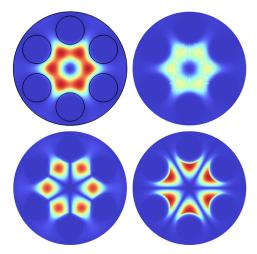
Arrow Surface 1

- I Right-click Electric Field (ewfd) and choose Arrow Surface.
- 2 In the Settings window for Arrow Surface, locate the Coloring and Style section.
- 3 From the Color list, choose White.

- I Right-click Arrow Surface I and choose Translation.
- 2 In the Settings window for Translation, locate the Translation section.
- 3 In the x text field, type 2.1*rb.

4 Clear the Apply to dataset edges check box.

Effective mode index=1.4304-1.4411E-5i Tangential and longitudinal electric and magnetic fields



Arrow Surface 2

- I In the Model Builder window, under Results>Electric Field (ewfd) right-click Arrow Surface I and choose Duplicate.
- 2 In the Settings window for Arrow Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)> Electromagnetic Waves, Frequency Domain>Electric>ewfd.Ex,ewfd.Ey - Electric field.

Translation 1

- I In the Model Builder window, expand the Arrow Surface 2 node.
- 2 Right-click Results>Electric Field (ewfd)>Arrow Surface 2>Translation I and choose Delete.

To clearly see the different polarization directions for the two degenerate modes with the highest effective indices, it helps here to change the phase of the solution to 45 degrees. Another option to see the different polarization directions would be to make an animation of one harmonic period.

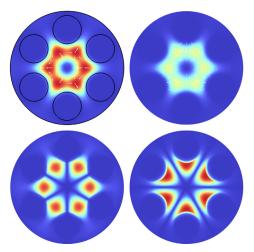
Study I/Solution I (soll)

- I In the Model Builder window, expand the Results>Datasets node, then click Study I/ Solution I (soll).
- 2 In the Settings window for Solution, locate the Solution section.

3 In the Solution at angle (phase) text field, type 45.

Arrow Surface 2

Effective mode index=1.4304-1.4411E-5i Tangential and longitudinal electric and magnetic fields



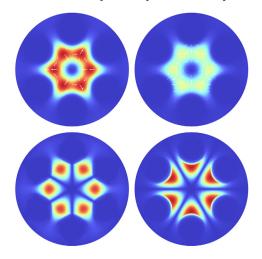
Electric Field (ewfd)

Now, remove the black edges and then add them back using line plots. This will make the location of the air holes more visible.

- I In the Model Builder window, click Electric Field (ewfd).
- 2 In the Settings window for 2D Plot Group, locate the Plot Settings section.

3 Clear the Plot dataset edges check box.

Effective mode index=1.4304-1.4411E-5i Tangential and longitudinal electric and magnetic fields



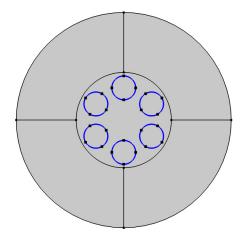
Line 1

- I Right-click Electric Field (ewfd) and choose Line.
- 2 In the Settings window for Line, locate the Coloring and Style section.
- **3** From the **Coloring** list, choose **Uniform**.
- 4 From the Color list, choose Black.

Selection I

- I Right-click Line I and choose Selection.
- 2 In the Settings window for Selection, locate the Selection section.

3 From the Selection list, choose Air Hole Boundaries.

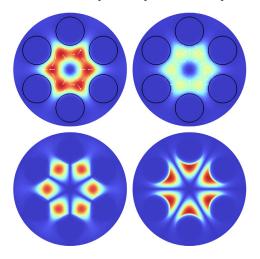


Line 2 In the Model Builder window, under Results>Electric Field (ewfd) right-click Line I and choose **Duplicate**.

- I In the Model Builder window, right-click Line 2 and choose Translation.
- 2 In the Settings window for Translation, locate the Translation section.

3 In the x text field, type 2.1*rb.

Effective mode index=1.4304-1.4411E-5i Tangential and longitudinal electric and magnetic fields



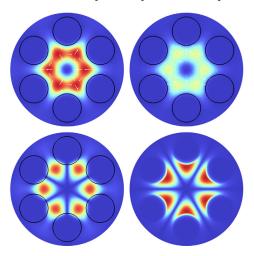
Line 1, Line 2

- I In the Model Builder window, under Results>Electric Field (ewfd), Ctrl-click to select Line I and Line 2.
- 2 Right-click and choose **Duplicate**.

- I In the Model Builder window, right-click Line 3 and choose Translation.
- 2 In the Settings window for Translation, locate the Translation section.

3 In the y text field, type -2.1*rb.

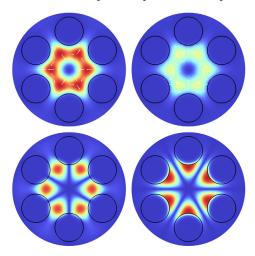
Effective mode index=1.4304-1.4411E-5i Tangential and longitudinal electric and magnetic fields



- I In the Model Builder window, expand the Results>Electric Field (ewfd)>Line 4 node, then click Translation 1.
- 2 In the Settings window for Translation, locate the Translation section.

3 In the y text field, type -2.1*rb.

Effective mode index=1.4304-1.4411E-5i Tangential and longitudinal electric and magnetic fields



Electric Field (ewfd)

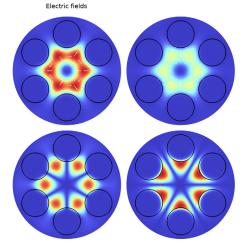
Finally, add some informative annotations.

Annotation I

- I In the Model Builder window, right-click Electric Field (ewfd) and choose Annotation.
- 2 In the Settings window for Annotation, locate the Annotation section.
- 3 In the **Text** text field, type Electric fields.
- 4 Locate the **Position** section. In the **Y** text field, type 1.2*rb.
- 5 Locate the Coloring and Style section. Clear the Show point check box.
- **6** From the **Anchor point** list, choose **Center**.

7 Click the Zoom Extents button in the Graphics toolbar.

Effective mode index=1.4304-1.4411E-5i Tangential and longitudinal electric and magnetic fields



Annotation 2

- I Right-click Annotation I and choose Duplicate.
- 2 In the Settings window for Annotation, locate the Annotation section.
- 3 In the **Text** text field, type Magnetic fields.

4 Locate the **Position** section. In the **X** text field, type 2.1*rb.

Magnetic fields Electric fields

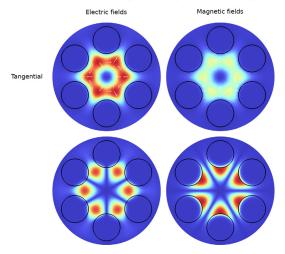
Effective mode index=1.4304-1.4411E-5i Tangential and longitudinal electric and magnetic fields

Annotation 3

- I In the Model Builder window, under Results>Electric Field (ewfd) right-click Annotation I and choose **Duplicate**.
- 2 In the Settings window for Annotation, locate the Annotation section.
- **3** In the **Text** text field, type Tangential.
- 4 Locate the **Position** section. In the **X** text field, type -1.1*rb.
- **5** In the **Y** text field, type 0.
- 6 Locate the Coloring and Style section. From the Anchor point list, choose Middle right.

7 Click the Zoom Extents button in the Graphics toolbar.

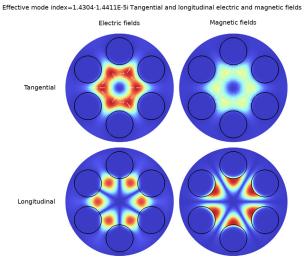
Effective mode index=1.4304-1.4411E-5i Tangential and longitudinal electric and magnetic fields



Annotation 4

- I Right-click Annotation 3 and choose Duplicate.
- 2 In the Settings window for Annotation, locate the Annotation section.
- 3 In the **Text** text field, type Longitudinal.

4 Locate the **Position** section. In the **Y** text field, type -2.1*rb.

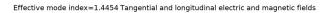


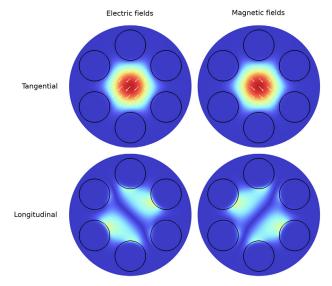
Electric Field (ewfd)

- I In the Model Builder window, click Electric Field (ewfd).
- 2 In the Settings window for 2D Plot Group, locate the Title section.
- 3 In the Parameter indicator text field, type Effective mode index=eval(ewfd.neff), to update the effective index in the title.

Now it is time to analyze the mode types, by stepping through the modes, starting with the mode with the largest effective index.

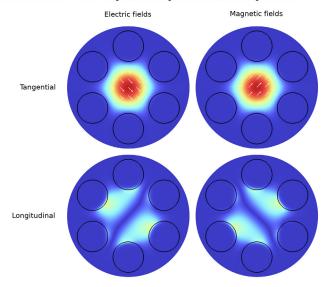
4 Click → Plot Last.



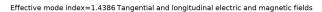


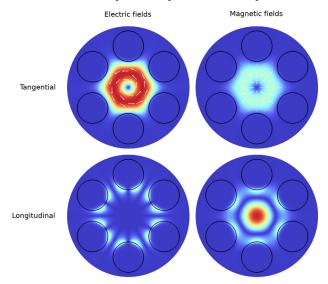
This is the first HE_{11} -like mode. These modes are degenerate with a degeneracy of two. This mixed mode has both longitudinal electric and magnetic field components.

Effective mode index=1.4454 Tangential and longitudinal electric and magnetic fields



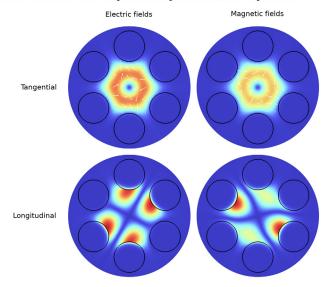
This is the second degenerate HE_{11} -like mode. The polarization is of course orthogonal to the first HE_{11} -like mode.





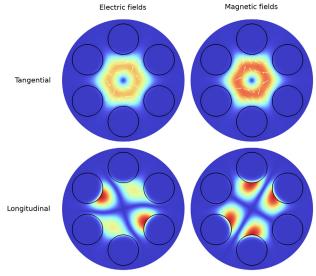
This is a TE₀₁-like mode, where the field is almost rotationally invariant and polarized in the ϕ direction. As seen, the longitudinal electric field is very small, whereas the longitudinal magnetic field is non-negligible.

Effective mode index=1.4384 Tangential and longitudinal electric and magnetic fields

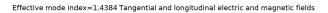


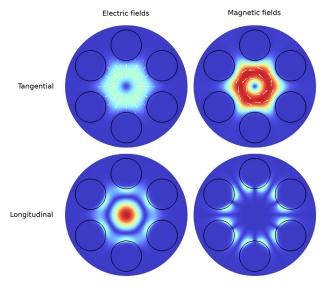
This is the first degenerate HE_{21} -like mode.

Effective mode index=1.4384 Tangential and longitudinal electric and magnetic fields



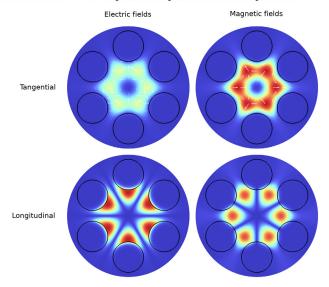
This is the second degenerate HE₂₁-like mode.





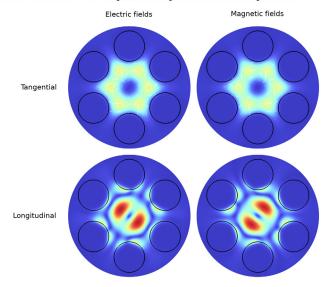
This is a TM₀₁-like mode, where the field is almost rotationally invariant and polarized in the radial direction. As seen, the longitudinal magnetic field is very small, whereas the longitudinal electric field is non-negligible.

Effective mode index=1.4293 Tangential and longitudinal electric and magnetic fields



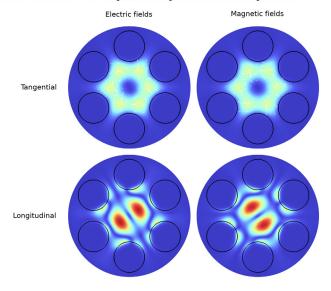
This is the first HE_{31} -like mode.

Effective mode index=1.4299 Tangential and longitudinal electric and magnetic fields



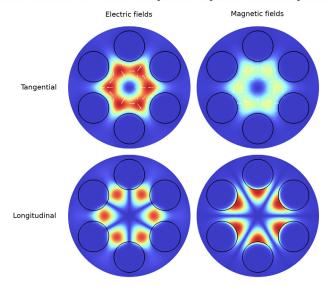
This is the first degenerate EH_{11} -like mode.

Effective mode index=1.4299 Tangential and longitudinal electric and magnetic fields



This is the second degenerate EH_{11} -like mode.

Effective mode index=1.4304-1.4411E-5i Tangential and longitudinal electric and magnetic fields



Finally, this is the second HE_{31} -like mode.