

Effect of Bearing Misalignment on Rotor Vibration

Introduction

In this example, a rotor shaft supported by two hydrodynamic bearings is analyzed. The gravity load acts on the rotor. An eccentric disk is also mounted on the rotor between the bearings. One of the bearings is misaligned with the axis of the rotor. The rotor whirls due to the mass imbalance.

The built-in multiphysics interface Beam Rotor with Hydrodynamic Bearing is used for the combined simulation of the rotor and bearings. A time dependent analysis is performed for two cases, first without misalignment and then including the misalignment. Results for both cases are compared to understand the effect of the misalignment.

The results include stress in the rotor, pressure distribution in the bearings, orbit of the rotor near the disk and the bearings.

Model Definition

The rotor is driven by a motor and is supported by two hydrodynamic bearings. The distance between the motor and the first bearing is a, and between the bearings is L. Thus, the rotor between the motor and first bearing is overhung with overhung length a. Diameter of the rotor is d. A disk is mounted on the rotor between the bearings, and it has certain amount of imbalance. The rotor rotates inside the bearings with an angular speed Ω . The bearing rotor assembly is shown in Figure 1 below.



Figure 1: Rotor configuration.

The material parameters of the rotor are listed in Table 1.

TABLE I: ROTOR MATERIAL PARAMETERS.

PARAMETER	VALUE		
Density	7780 kg/m ³		
Young's modulus	2.00·10 ¹¹ Pa		
Poisson's ratio	0.29		

Geometric properties of the rotor are given in Table 2.

TABLE 2: ROTOR GEOMETRIC PARAMETERS.

PARAMETER	VALUE
Shaft diameter, d	10 mm
Shaft length, L	100 mm
Shaft overhung length, a	20 mm
Angular speed of the shaft, Ω	210 rad/s
Disk distance from the left bearing	40 mm
Disk diameter, D _d	50 mm
Disk thickness, h _d	10 mm
Disk unbalance magnitude	8e-9 kg-m

The parameters needed for the fluid-film simulation of the plain journal bearings are the dynamic viscosity, density at cavitation pressure, and compressibility. Values of the parameters are summarized in Table 3 below.

TABLE 3: BEARING PARAMETERS.

PARAMETER	VALUE
Bearing length, L _b	5 mm
Bearing initial clearance, C	0.05 mm
Oil viscosity, μ	9.4 mPa-s
Density, ρ	866 kg/m ³
Compressibility, β	10-7 Pa ⁻¹

Results and Discussion

Figure 2 shows the stress profile on the rotor for the misaligned rotor with the maximum bending stress in the middle part. The pressure distribution in the bearings is also shown.



para(2)=1 Time=0.5 s Surface: Pressure (Pa) Contour: Pressure (Pa) Line: von Mises stress (N/m²)

Figure 2: Bearing pressure and rotor stress.

A comparison of the pressure in the first bearing for with and without misalignment is shown in Figure 3. In the case of misalignment, the pressure distribution in the bearing becomes skewed.



para(1)=0 Time=0.5 s Contour: Physical pressure (Pa) Contour: Physical pressure (Pa)

Figure 3: Comparison of bearing pressure with and without misalignment.

The orbit of the journal in the *yz*-plane in the first bearing is shown in Figure 4. The orbit consists of a transient response followed by steady state whirl. An equilibrium position in the orbit is decided by the gravity load, and the whirl around the equilibrium position is

the response to the mass imbalance. The journal orbit in the left bearing is not significantly affected by the misalignment in the right bearing.



Figure 4: Journal orbit in left bearing.

An orbit of the journal in the second bearing is shown in Figure 5. The characteristics of the orbit in this bearing are similar to that in the left bearing. The only noticeable difference is that the equilibrium positions of the journal in this bearing depends on the misalignment. Note that the vertical component of the steady state equilibrium position

with the misalignment is higher than the one without misalignment due to skewed pressure distribution.



Figure 5: Journal orbit in the right bearing.

A comparison of the velocity of the journal in the right bearing is shown in Figure 6. The oscillation in the velocity has a leading phase for the misaligned bearing as compared to

the same for the normal bearing. Thus, the journal reaches the equilibrium position much quicker when the bearing is misaligned.



Figure 6: Horizontal velocity of the journal in the right bearing.

Figure 7 shows the orbit of the rotor at the disk. The equilibrium position of the orbit at this location is also affected by the misalignment in the right bearing. In steady state, the rotor is slightly inclined from its initial axis due to misalignment.



Figure 7: Rotor orbit at disk.

Application Library path: Rotordynamics_Module/Tutorials/misaligned_rotor

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click **Model Wizard**.

MODEL WIZARD

- I In the Model Wizard window, click 间 3D.
- 2 In the Select Physics tree, select Structural Mechanics>Rotordynamics> Beam Rotor with Hydrodynamic Bearing.
- 3 Click Add.

- 4 Click \bigcirc Study.
- 5 In the Select Study tree, select General Studies>Time Dependent.
- 6 Click **M** Done.

Start by defining the parameters of the rotor.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
Ow	210[rad/s]	210 rad/s	Angular speed of shaft
d	10[mm]	0.01 m	Shaft diameter
L	100[mm]	0.1 m	Shaft length
а	20[mm]	0.02 m	Shaft overhung length
E_r	200[GPa]	2EII Pa	Young's modulus
nu_r	0.29	0.29	Poisson's ratio
rho_r	7780[kg/m^3]	7780 kg/m³	Shaft and disk density
xd	40[mm]	0.04 m	Disk distance from left bearing
Dd	50[mm]	0.05 m	Disk diameter
hd	10[mm]	0.01 m	Disk thickness
me	8e-9[kg*m]	8E-9 kg∙m	Disk unbalance magnitude
Lb	5[mm]	0.005 m	Bearing length
С	0.05[mm]	5E-5 m	Bearing initial clearance
muO	9.4[mPa*s]	0.0094 Pa·s	Oil viscosity
para	0	0	Misalignment switch parameter

GEOMETRY I

Polygon I (poll)

- I In the Geometry toolbar, click \bigoplus More Primitives and choose Polygon.
- 2 In the Settings window for Polygon, locate the Coordinates section.

- 3 From the Data source list, choose Vectors.
- 4 In the x text field, type 0 a a+xd a+L.
- **5** In the **y** text field, type **0**.
- **6** In the **z** text field, type **0**.

Define the rotor selection for later use.

- 7 Locate the Selections of Resulting Entities section. Find the Cumulative selection subsection. Click New.
- 8 In the New Cumulative Selection dialog box, type Rotor in the Name text field.
- 9 Click OK.

Cylinder I (cyl1)

- I In the **Geometry** toolbar, click 🔲 **Cylinder**.
- 2 In the Settings window for Cylinder, locate the Object Type section.
- 3 From the Type list, choose Surface.
- 4 Locate the Size and Shape section. In the Radius text field, type d/2.
- **5** In the **Height** text field, type Lb.
- 6 Locate the **Position** section. In the **x** text field, type a-Lb/2.
- 7 Locate the Axis section. From the Axis type list, choose x-axis.

Define the bearing selection.

- 8 Locate the Selections of Resulting Entities section. Find the Cumulative selection subsection. Click New.
- 9 In the New Cumulative Selection dialog box, type Bearing 1 in the Name text field.

IO Click OK.

Cylinder 2 (cyl2)

- I Right-click Cylinder I (cyll) and choose Duplicate.
- 2 In the Settings window for Cylinder, locate the Position section.
- **3** In the **x** text field, type a+L-Lb.

Define the selection for second bearing.

- **4** Locate the **Selections of Resulting Entities** section. Find the **Cumulative selection** subsection. Click **New**.
- 5 In the New Cumulative Selection dialog box, type Bearing 2 in the Name text field.
- 6 Click OK.

Define some more selections that will be useful in meshing.

DEFINITIONS

Bearings

- I In the **Definitions** toolbar, click 📑 **Union**.
- 2 In the Settings window for Union, type Bearings in the Label text field.
- 3 Locate the Geometric Entity Level section. From the Level list, choose Boundary.
- 4 Locate the Input Entities section. Under Selections to add, click + Add.
- 5 In the Add dialog box, in the Selections to add list, choose Bearing I and Bearing 2.
- 6 Click OK.

Bearings Left Edges

- I In the **Definitions** toolbar, click **here Explicit**.
- 2 In the Settings window for Explicit, locate the Input Entities section.
- 3 From the Geometric entity level list, choose Edge.
- **4** Select Edges 3 and 17 only.
- **5** Select the **Group by continuous tangent** check box.
- 6 In the Label text field, type Bearings Left Edges.

MATERIALS

Material I (mat1)

- I In the Model Builder window, under Component I (compl) right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Edge.
- **4** From the **Selection** list, choose **Rotor**.
- 5 Locate the Material Contents section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	E	E_r	Pa	Young's modulus and Poisson's ratio
Poisson's ratio	nu	nu_r	1	Young's modulus and Poisson's ratio
Density	rho	rho_r	kg/m³	Basic

BEAM ROTOR (ROTBM)

- I In the Model Builder window, under Component I (compl) click Beam Rotor (rotbm).
- 2 In the Settings window for Beam Rotor, locate the Edge Selection section.
- **3** From the **Selection** list, choose **Rotor**.
- 4 Locate the Rotor Speed section. From the list, choose Angular velocity.
- **5** In the text field, type Ow.

Rotor Cross Section 1

- I In the Model Builder window, under Component I (compl)>Beam Rotor (rotbm) click Rotor Cross Section I.
- 2 In the Settings window for Rotor Cross Section, locate the Cross-Section Definition section.
- **3** In the d_o text field, type d.

Disk I

- I In the Physics toolbar, click 🗁 Points and choose Disk.
- **2** Select Point 11 only.
- 3 In the Settings window for Disk, locate the Disk Properties section.
- 4 From the Center of mass list, choose Offset from selected points.
- **5** In the z_r text field, type me/rotbm.disk1.mass.
- 6 From the Specified by list, choose Geometric dimensions.
- 7 In the ρ text field, type rho_r.
- 8 In the *d* text field, type Dd.
- **9** In the *h* text field, type hd.

Gravity I

In the **Physics** toolbar, click 🔚 **Edges** and choose **Gravity**.

HYDRODYNAMIC BEARING (HDB)

- I Click the 🐱 Show More Options button in the Model Builder toolbar.
- 2 In the Show More Options dialog box, in the tree, select the check box for the node Physics>Advanced Physics Options.
- 3 Click OK.
- 4 In the Model Builder window, under Component I (compl) click Hydrodynamic Bearing (hdb).
- 5 In the Settings window for Hydrodynamic Bearing, locate the Physical Model section.

6 From the Fluid type list, choose Liquid with cavitation.

Hydrodynamic Journal Bearing 1

- I In the Model Builder window, under Component I (compl)>Hydrodynamic Bearing (hdb) click Hydrodynamic Journal Bearing I.
- **2** In the **Settings** window for **Hydrodynamic Journal Bearing**, locate the **Bearing Properties** section.
- **3** In the *C* text field, type C.
- **4** Locate the **Fluid Properties** section. From the μ list, choose **User defined**. In the associated text field, type mu0.
- **5** In the ρ_c text field, type 866[kg/m³].

Hydrodynamic Journal Bearing 2

- I Right-click Component I (comp1)>Hydrodynamic Bearing (hdb)> Hydrodynamic Journal Bearing I and choose Duplicate.
- **2** In the Settings window for Hydrodynamic Journal Bearing, locate the Boundary Selection section.
- 3 From the Selection list, choose Bearing 2.

Misalignment 1

- I In the Physics toolbar, click 📃 Attributes and choose Misalignment.
- 2 In the Settings window for Misalignment, locate the Parallel Misalignment section.
- **3** In the u_{0z} text field, type **0.6***C*para.
- **4** Locate the **Angular Misalignment** section. In the θ_{0z} text field, type 0.004*para.

MULTIPHYSICS

Beam Rotor Bearing Coupling 2 (brbc2)

- In the Model Builder window, under Component I (comp1)>Multiphysics right-click
 Beam Rotor Bearing Coupling I (brbc1) and choose Duplicate.
- **2** In the **Settings** window for **Beam Rotor Bearing Coupling**, locate the **Boundary Selection** section.
- **3** From the Selection list, choose Bearing **2**.

Create a mapped mesh on the bearing surface.

MESH I

Mapped I

- I In the Mesh toolbar, click A Boundary and choose Mapped.
- 2 In the Settings window for Mapped, locate the Boundary Selection section.
- 3 From the Selection list, choose Bearings.

Distribution I

- I Right-click Mapped I and choose Distribution.
- 2 Select Edges 8 and 22 only.

Distribution 2

- I In the Model Builder window, right-click Mapped I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Edge Selection section.
- **3** From the Selection list, choose Bearings Left Edges.
- **4** Locate the **Distribution** section. In the **Number of elements** text field, type **10**.

Edge 1

- I In the Mesh toolbar, click \bigwedge Boundary and choose Edge.
- 2 In the Settings window for Edge, locate the Edge Selection section.
- **3** From the **Selection** list, choose **Rotor**.

Distribution I

- I Right-click Edge I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Edge Selection section.
- 3 Click 📉 Clear Selection.
- 4 Select Edge 1 only.
- 5 Locate the Distribution section. In the Number of elements text field, type 20.

Distribution 2

- I Right-click Distribution I and choose Duplicate.
- 2 In the Settings window for Distribution, locate the Edge Selection section.
- 3 Click Clear Selection.
- 4 Select Edge 10 only.
- 5 Locate the Distribution section. In the Number of elements text field, type 40.

Distribution 3

I Right-click **Distribution 2** and choose **Duplicate**.

- 2 In the Settings window for Distribution, locate the Edge Selection section.
- 3 Click Clear Selection.
- 4 Select Edge 15 only.
- 5 Locate the Distribution section. In the Number of elements text field, type 60.
- 6 Click 📗 Build All.

STUDY I

Step 1: Time Dependent

- I In the Model Builder window, under Study I click Step I: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- 3 In the **Output times** text field, type range(0,1e-3,0.5).
- **4** Click the **5** Show More Options button in the Model Builder toolbar.
- 5 In the Show More Options dialog box, select Study>Batch and Cluster in the tree.
- 6 In the tree, select the check box for the node Study>Batch and Cluster.
- 7 Click OK.

Use the batch sweep to perform two simulations, one without misalignment and the other with misalignment.

Batch Sweep

- I In the Study toolbar, click 🔛 Batch and choose Batch Sweep.
- 2 In the Settings window for Batch Sweep, locate the Batch Settings section.
- 3 Find the Before sweep subsection. Clear the Clear_meshes check box.
- 4 Clear the **Clear solutions** check box.
- 5 Locate the Advanced Settings section. In the Number of simultaneous jobs text field, type2.
- 6 Locate the Study Settings section. Click + Add.
- 7 In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
para (Misalignment switch parameter)	0 1	

Batch Data

In the **Study** toolbar, click **= Compute**.

RESULTS

Stress (rotbm)

- I In the Model Builder window, expand the Results node, then click Stress (rotbm).
- 2 In the Settings window for 3D Plot Group, locate the Plot Settings section.
- **3** From the **View** list, choose **New view**.
- 4 In the Stress (rotbm) toolbar, click **I** Plot.

Copy the **Line** node from the **Stress (rotbm)** plot group and paste it into the **Fluid Pressure** (**hdb**) plot group to show both rotor and bearings together. This plot is shown in Figure 2.

Line I

- I In the Model Builder window, expand the Stress (rotbm) node.
- 2 Right-click Line I and choose Copy.

Line I

- I In the Model Builder window, right-click Fluid Pressure (hdb) and choose Paste Line.
- 2 In the Settings window for Line, locate the Coloring and Style section.
- 3 Click Change Color Table.
- 4 In the Color Table dialog box, select Aurora>JupiterAuroraBorealis in the tree.
- 5 Click OK.
- 6 In the Settings window for Line, locate the Coloring and Style section.
- 7 In the Radius scale factor text field, type 0.2.

Fluid Pressure (hdb)

- I In the Model Builder window, click Fluid Pressure (hdb).
- 2 In the Settings window for 3D Plot Group, locate the Color Legend section.
- **3** From the **Position** list, choose **Right double**.
- **4** Click the **Comextents** button in the **Graphics** toolbar.
- 5 In the Fluid Pressure (hdb) toolbar, click 💿 Plot.

Follow the instructions below to compare the disk orbit for normal and misaligned bearing cases as shown in Figure 7.

Disk Orbit

- I In the Home toolbar, click 🚛 Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Disk Orbit in the Label text field.

3 Locate the Data section. From the Dataset list, choose Study 1/ Parametric Solutions 1 (sol2).

Point Graph 1

- I Right-click Disk Orbit and choose Point Graph.
- **2** Select Point 11 only.
- 3 In the Settings window for Point Graph, locate the y-Axis Data section.
- 4 In the **Expression** text field, type w.
- 5 Locate the x-Axis Data section. From the Axis source data list, choose Time.
- 6 From the Parameter list, choose Expression.
- 7 In the Expression text field, type v.
- 8 Click to expand the **Legends** section. Find the **Include** subsection. Clear the **Point** check box.
- 9 Select the Show legends check box.
- **IO** From the **Legends** list, choose **Manual**.

II In the table, enter the following settings:

Legends

Without Misalignment

With Misalignment

12 In the Disk Orbit toolbar, click 💽 Plot.

Disk Orbit

- I In the Model Builder window, click Disk Orbit.
- 2 In the Settings window for ID Plot Group, locate the Data section.
- 3 From the Dataset list, choose Study I/Parametric Solutions I (sol2).
- 4 Locate the Legend section. From the Position list, choose Upper left.
- 5 Click to expand the Title section. From the Title type list, choose Label.

Duplicate the **Disk Orbit** plot and change the selection to compare the left bearing orbit for both cases as shown in Figure 4.

Bearing I Orbit

- I Right-click **Disk Orbit** and choose **Duplicate**.
- 2 In the Settings window for ID Plot Group, type Bearing 1 Orbit in the Label text field.

Point Graph 1

- I In the Model Builder window, expand the Bearing I Orbit node, then click Point Graph I.
- 2 In the Settings window for Point Graph, locate the Selection section.
- 3 Click Clear Selection.
- **4** Select Point 6 only.
- **5** In the **Bearing I Orbit** toolbar, click **I** Plot.

Duplicate the **Bearing I Orbit** plot and change the selection to compare the right bearing orbit for both cases as shown in Figure 5.

Bearing 2 Orbit

- I In the Model Builder window, right-click Bearing I Orbit and choose Duplicate.
- 2 In the Settings window for ID Plot Group, type Bearing 2 Orbit in the Label text field.

Point Graph 1

- I In the Model Builder window, expand the Bearing 2 Orbit node, then click Point Graph I.
- 2 In the Settings window for Point Graph, locate the Selection section.
- **3** Click Clear Selection.
- **4** Select Point 18 only.
- 5 In the Bearing 2 Orbit toolbar, click 💿 Plot.

Compare the velocity of the journal in the right bearing for both normal and misaligned cases, as shown in Figure 6, using the following instructions.

Journal Velocity (Bearing 2)

- I In the Home toolbar, click 🚛 Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, locate the Data section.
- 3 From the Dataset list, choose Study I/Parametric Solutions I (sol2).
- 4 In the Label text field, type Journal Velocity (Bearing 2).

Point Graph 1

- I Right-click Journal Velocity (Bearing 2) and choose Point Graph.
- **2** Select Point 18 only.
- 3 In the Settings window for Point Graph, locate the y-Axis Data section.
- 4 In the **Expression** text field, type vt.
- 5 Locate the Legends section. Select the Show legends check box.
- 6 From the Legends list, choose Manual.

7 In the table, enter the following settings:

Legends Without misalignment

With misalignment

8 In the Journal Velocity (Bearing 2) toolbar, click 🗿 Plot.

The pressure distributions in the right bearing for the normal and misaligned cases are compared in Figure 3. To reproduce this result, start by creating a dataset with only the right bearing selection.

Study I/Parametric Solutions I (3) (sol2)

I In the Model Builder window, expand the Results>Datasets node.

2 Right-click Results>Datasets>Study I/Parametric Solutions I (sol2) and choose Duplicate.

Selection

- I In the Results toolbar, click 🖣 Attributes and choose Selection.
- 2 In the Settings window for Selection, locate the Geometric Entity Selection section.
- **3** From the **Geometric entity level** list, choose **Boundary**.
- 4 From the Selection list, choose Bearing 2.

Pressure Comparison: Right Bearing

- I In the Results toolbar, click 间 3D Plot Group.
- 2 In the Settings window for 3D Plot Group, type Pressure Comparison: Right Bearing in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study I/ Parametric Solutions I (3) (sol2).
- 4 From the Parameter value (para) list, choose 0.
- 5 Locate the Plot Settings section. Clear the Plot dataset edges check box.
- 6 From the View list, choose New view.

Contour I

- I Right-click Pressure Comparison: Right Bearing and choose Contour.
- 2 In the Settings window for Contour, locate the Expression section.
- **3** In the **Expression** text field, type hdb.p.
- 4 Locate the Coloring and Style section. From the Contour type list, choose Filled.
- 5 Click Change Color Table.

- 6 In the Color Table dialog box, select Rainbow>RainbowLight in the tree.
- 7 Click OK.

Contour 2

- I Right-click Contour I and choose Duplicate.
- 2 In the Settings window for Contour, locate the Data section.
- 3 From the Dataset list, choose Study I/Parametric Solutions I (3) (sol2).
- 4 Click to expand the Inherit Style section. From the Plot list, choose Contour I.
- 5 In the Model Builder window, click Results.
- 6 In the Settings window for Results, locate the Update of Results section.
- 7 Select the **Only plot when requested** check box.

Translation 1

- I In the Model Builder window, right-click Contour 2 and choose Translation.
- 2 In the Settings window for Translation, locate the Translation section.
- 3 In the x text field, type 3*Lb.

Pressure Comparison: Right Bearing

In the Model Builder window, under Results click Pressure Comparison: Right Bearing.

Table Annotation 1

- I In the Pressure Comparison: Right Bearing toolbar, click i More Plots and choose Table Annotation.
- 2 In the Settings window for Table Annotation, locate the Data section.
- **3** From the **Source** list, choose **Local table**.
- **4** In the table, enter the following settings:

x-coordinate	y-coordinate	z-coordinate	Annotation
L+6.1*Lb	-d/2	d/4	Misaligned
L+3.1*Lb	-d/2	d/4	Normal

Pressure Comparison: Right Bearing

- I In the Model Builder window, click Pressure Comparison: Right Bearing.
- 2 In the Settings window for 3D Plot Group, locate the Color Legend section.
- **3** From the **Position** list, choose **Right double**.
- **4** Click the \longleftrightarrow **Zoom Extents** button in the **Graphics** toolbar.
- 5 In the Pressure Comparison: Right Bearing toolbar, click 💽 Plot.

22 | effect of bearing misalignment on rotor vibration