

Coupled Analysis of Flow and Stress in a Pipe

In this tutorial model, the flow in a pipe with a bend is computed using the Pipe Flow interface. The computed fluid load is used as input to a stress analysis in the Pipe Mechanics interface. Gravity loads from the pipe and fluid are also taken into account.

Model Definition

A circular pipe with outer diameter $d_0 = 10$ cm consists of two straight 8 m long sections that are connected by a smooth 90-degree circular bend with a radius $r_b = 2$ m; see Figure 1.

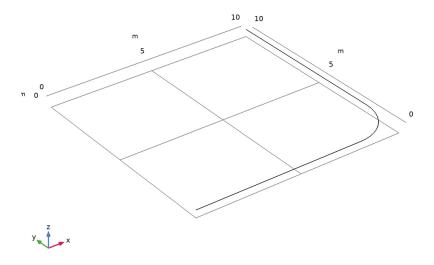


Figure 1: Pipe geometry.

Both ends are fixed, and the pipe is placed on three evenly spaced vertical supports.

The pipe wall thickness is t = 4 mm, so that the inner diameter is $d_i = 9.2$ cm. The inlet and outlet pressure are kept at 50 bar and 40 bar, respectively. A stationary flow of water in the pipe is driven by the resulting pressure drop. The pressure outside the pipe is assumed to be negligible. Thus, a significant internal overpressure, p, causes a hoop stress in the pipe walls.

The pipe is made of steel and has the inner surface roughness of e = 0.046 mm.

The system is subjected to the gravity, so that the pipe and fluid weight causes the pipe vertical bending. In addition, the flow acts on the pipe in two ways: the drag force due to the wall friction, and the centrifugal force in the bend. Both forces lead to the pipe horizontal deflection and bending.

The drag force acts along the pipe and is estimated using the Swamee-Jain formula (Ref. 1)

$$f_{\rm D} = \frac{0.25}{\left(\log_{10}\left(\left(\frac{e/d_i}{3.7}\right) + \frac{5.74}{({\rm Re})^{0.9}}\right)\right)^2}$$

which is valid for relative roughness $1 \cdot 10^{-6} < e/d_i < 1 \cdot 10^{-2}$ and $5 \cdot 10^3 < \text{Re} < 1 \cdot 10^8$. The Reynolds number is $Re = \rho u d_i / \mu$, where u is the flow velocity, ρ is water density, and μ is the dynamic viscosity.

The centrifugal force acts outward the bend perpendicular to the pipe, and its magnitude is given by: $\rho A u^2/r_h$, where A is the area of the pipe inner cross section.

The pressure distribution inside the pipe is shown in Figure 2. The flow has a uniform velocity around 23.8 m/s along the whole pipe, which corresponds to the Reynolds number Re = $2.2 \cdot 10^6$ that indicates that the flow regime is highly turbulent.

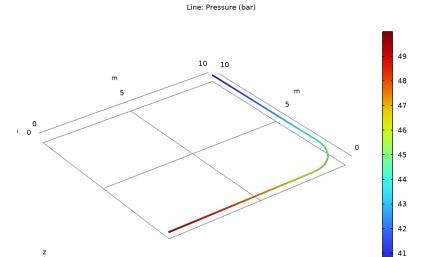


Figure 2: Pressure distribution.

The stress distribution in the pipe walls is shown in Figure 3. Due to the pressure drop in the fluid, the value is higher at the inlet than at the outlet. The pipe displacement

components are shown in Figure 4. The importance of the vertical supports is clearly visible.

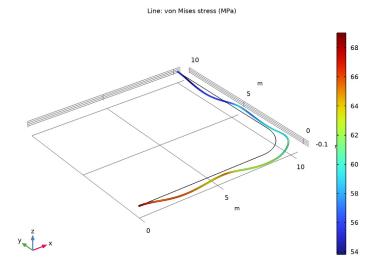


Figure 3: von Mises stress distribution along the deformed pipe. The deformation is scaled by approximately a factor of 150.

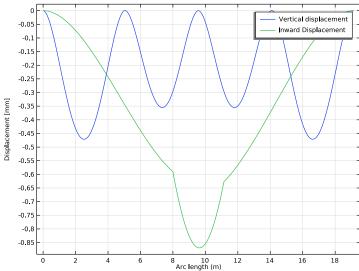


Figure 4: Pipe displacement.

The bending moments and shear forces along the pipe are shown in Figure 5 and Figure 6.

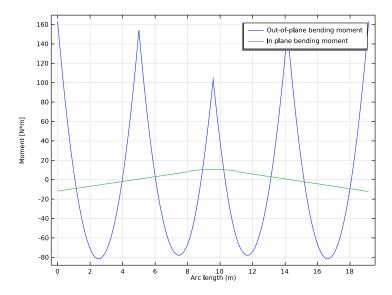


Figure 5: Bending moments.

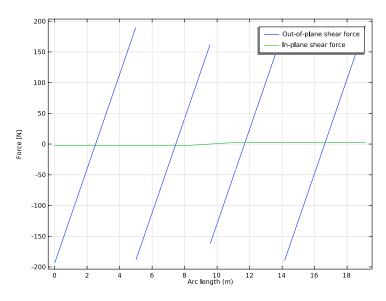


Figure 6: Shear forces.

The different contributions to the total stress state are shown in Figure 7. As is common in piping systems, the hoop stress caused by the internal pressure is dominant.

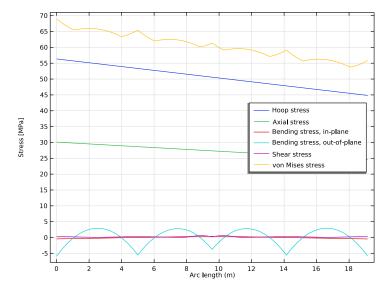


Figure 7: Stress contributions.

Notes About the COMSOL Implementation

You start the model setup by adding a multiphysics interface Fluid-Pipe Interaction, Fixed Geometry. This will bring in two physics interfaces, Pipe Flow and Pipe Mechanics, together with a multiphysics coupling feature Fluid-Pipe Interaction.

The interfaces are one-way coupled. Thus, the flow will affect the structural displacement, but the pipe geometry change because of the deformation is assumed to be small and will have no effect on the flow computations.

The flow induced forces such as internal overpressure, drag and centrifugal forces are computed and applied on the structure automatically by the coupling feature.

The Pipe Mechanics interface needs two materials, one for the pipe wall and the other for the contained fluid. The materials are chosen in the node Fluid and Pipe Materials under the interface. The material selection lists will contain all materials available in the component. The material data will be taken from the selected material even if the corresponding material node has no selection or is overridden under Materials in the component. The **Pipe Flow** interface can only take data from an active material with proper selection made under Materials in the component.

Reference

1. P.K Swamee and A.K. Jain, "Explicit Equations for Pipe-flow Problems", J. Hydraulics Division (ASCE), vol. 102, no. 5, pp. 657-664, 1976.

Application Library path: Pipe Flow Module/Pipe Mechanics/pipe flow stress

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click **3D**.
- 2 In the Select Physics tree, select Structural Mechanics>Fluid-Structure Interaction>Fluid-Pipe Interaction, Fixed Geometry.
- 3 Click Add.
- 4 Click 🗪 Study.
- 5 In the Select Study tree, select General Studies>Stationary.
- 6 Click M Done.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click Load from File.
- 4 Browse to the model's Application Libraries folder and double-click the file pipe_flow_stress_parameters.txt.

The undeformed pipe is located in the xy-plane.

GEOMETRY I

Work Plane I (wbl)

In the Geometry toolbar, click Work Plane.

The pipe consists of two straight sections connected by a circular bend.

Work Plane I (wb I)>Plane Geometry

In the Model Builder window, click Plane Geometry.

Work Plane I (wbl)>Polygon I (boll)

- I In the Work Plane toolbar, click / Polygon.
- 2 In the Settings window for Polygon, locate the Object Type section.
- **3** From the **Type** list, choose **Open curve**.
- **4** Locate the **Coordinates** section. In the table, enter the following settings:

xw (m)	yw (m)	
0	0	
Xs	0	
Xb-rb	0	

Work Plane I (wbl)>Circular Arc I (cal)

- I In the Work Plane toolbar, click More Primitives and choose Circular Arc.
- 2 In the Settings window for Circular Arc, locate the Radius section.
- 3 In the Radius text field, type rb.
- **4** Locate the **Center** section. In the **xw** text field, type Xb-rb.
- 5 In the yw text field, type rb.
- 6 Locate the Angles section. In the Start angle text field, type 270.
- 7 In the End angle text field, type 315.

Work Plane I (wbl)>Circular Arc 2 (ca2)

- I Right-click Component I (compl)>Geometry I>Work Plane I (wpl)>Plane Geometry> Circular Arc I (cal) and choose Duplicate.
- 2 In the Settings window for Circular Arc, locate the Angles section.
- 3 In the Start angle text field, type 315.
- 4 In the End angle text field, type 0.

Work Plane I (wp I)>Polygon 2 (pol2)

I In the Work Plane toolbar, click / Polygon.

- 2 In the Settings window for Polygon, locate the Object Type section.
- 3 From the Type list, choose Open curve.
- **4** Locate the **Coordinates** section. In the table, enter the following settings:

xw (m)	yw (m)	
Xb	rb	
Xb	Ys	
Xb	Yout	

5 In the Model Builder window, right-click Geometry I and choose Build All.

MESH I

- I In the Model Builder window, under Component I (compl) click Mesh I.
- 2 In the Settings window for Mesh, locate the Sequence Type section.
- 3 From the list, choose User-controlled mesh.

Size

- I In the Model Builder window, under Component I (compl)>Mesh I click Size.
- 2 In the Settings window for Size, locate the Element Size section.
- 3 From the Predefined list, choose Extremely fine.
- 4 Click the Custom button.
- 5 Locate the Element Size Parameters section. In the Maximum element size text field, type 0.02.
- 6 Click III Build All.

Add two materials for the pipe wall and contained fluid.

ADD MATERIAL

- I In the Home toolbar, click Radd Material to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Built-in>Structural steel.
- 4 Right-click and choose Add to Component I (compl).
- 5 In the tree, select Built-in>Water, liquid.
- 6 Right-click and choose Add to Component I (compl).
- 7 In the Home toolbar, click 🙀 Add Material to close the Add Material window.

MATERIALS

Water, liquid (mat2)

- I In the Settings window for Material, locate the Geometric Entity Selection section.
- 2 From the Selection list, choose All edges.

PIPE FLOW (PFL)

Pipe Properties 1

- I In the Model Builder window, under Component I (compl)>Pipe Flow (pfl) click Pipe Properties 1.
- 2 In the Settings window for Pipe Properties, locate the Pipe Shape section.
- 3 From the list, choose Circular.
- **4** In the d_i text field, type di.
- 5 Locate the Flow Resistance section. From the Friction model list, choose Swamee-Jain.
- 6 From the Surface roughness list, choose Commercial steel (0.046 mm).

In the Pipe Mechanics interface, you select the materials explicitly from the list.

PIPE MECHANICS (PIPEM)

Fluid and Pipe Materials 1

- I In the Model Builder window, under Component I (compl)>Pipe Mechanics (pipem) click Fluid and Pipe Materials 1.
- 2 In the Settings window for Fluid and Pipe Materials, locate the Fluid Properties section.
- 3 From the Fluid material list, choose Water, liquid (mat2).
- 4 Locate the Pipe Properties section. From the Pipe material list, choose Structural steel (matl).

Pipe Cross Section 1

- I In the Model Builder window, click Pipe Cross Section I.
- 2 In the Settings window for Pipe Cross Section, locate the Pipe Shape section.
- 3 From the list, choose Circular.
- **4** In the d_o text field, type do.
- **5** In the d_i text field, type di.

Orient the pipe cross section so that the second coordinate axis of the beam coordinate system is oriented normal to the pipe in the xy-plane. The first coordinate axis is always oriented along the pipe.

Section Orientation I

- I In the Model Builder window, click Section Orientation I.
- 2 In the Settings window for Section Orientation, locate the Section Orientation section.
- 3 From the Orientation method list, choose Orientation vector.
- **4** Specify the *V* vector as

- 1	Χ
1	Υ
0	Z

Both ends of the pipe are fixed.

Fixed Constraint I

- I In the Physics toolbar, click Points and choose Fixed Constraint.
- **2** Select Points 1 and 7 only.

The pipe is supported vertically at three locations.

Prescribed Displacement/Rotation I

- I In the Physics toolbar, click Points and choose Prescribed Displacement/Rotation.
- **2** Select Points 2, 4, and 6 only.
- 3 In the Settings window for Prescribed Displacement/Rotation, locate the Prescribed Displacement section.
- 4 From the Prescribed in z direction list, choose Prescribed.

Gravity I

In the Physics toolbar, click A Global and choose Gravity.

PIPE FLOW (PFL)

Pressure, inlet

- I In the Model Builder window, under Component I (compl) > Pipe Flow (pfl) click Pressure L.
- 2 In the Settings window for Pressure, type Pressure, inlet in the Label text field.
- **3** Locate the **Boundary Pressure** section. In the p_0 text field, type pin.

Pressure, outlet

- I In the Physics toolbar, click Points and choose Pressure.
- 2 In the Settings window for Pressure, type Pressure, outlet in the Label text field.
- **3** Select Point 7 only.
- **4** Locate the **Boundary Pressure** section. In the p_0 text field, type pout.

STUDY I

In the **Home** toolbar, click **Compute**.

The first three default plots show the pressure in the pipe, the flow velocity, and the stress distribution along the deformed pipe.

RESULTS

line 1

- I In the Model Builder window, expand the Pressure (pfl) node, then click Line I.
- 2 In the Settings window for Line, locate the Expression section.
- 3 From the Unit list, choose bar.
- 4 In the Pressure (pfl) toolbar, click **Plot**.

Velocity (bfl)

- I In the Model Builder window, under Results click Velocity (pfl).
- 2 In the Settings window for 3D Plot Group, locate the Color Legend section.
- 3 Select the **Show units** check box.

line l

- I In the Model Builder window, expand the Stress (pipem) node, then click Line I.
- 2 In the Settings window for Line, locate the Expression section.
- 3 From the Unit list, choose MPa.

Displacement

- I In the Home toolbar, click Add Plot Group and choose ID Plot Group. Add a plot of the pipe displacement components.
- 2 In the Settings window for ID Plot Group, type Displacement in the Label text field.
- 3 Locate the Plot Settings section.
- 4 Select the y-axis label check box. In the associated text field, type Displacement [mm].

Line Graph 1

- I Right-click **Displacement** and choose **Line Graph**.
- 2 In the Settings window for Line Graph, locate the Selection section.
- **3** From the **Selection** list, choose **All edges**.
- 4 Locate the y-Axis Data section. In the Expression text field, type w_pipe.
- **5** From the **Unit** list, choose **mm**.
- **6** Click to expand the **Title** section. From the **Title type** list, choose **None**.
- 7 Click to expand the **Legends** section. Select the **Show legends** check box.
- 8 From the Legends list, choose Manual.
- **9** In the table, enter the following settings:

Legends	
Vertical	displacement

Line Graph 2

- I Right-click Line Graph I and choose Duplicate.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- 3 In the Expression text field, type u_pipe*pipem.beamsys.e_y1+v_pipe* pipem.beamsys.e_y2.
- **4** Locate the **Legends** section. In the table, enter the following settings:

Legends Inward Displacement

5 In the **Displacement** toolbar, click **Plot**.

Next, plot the moment and force distributions along the pipe.

Bending Moment

- I In the Model Builder window, right-click Displacement and choose Duplicate.
- 2 In the Settings window for ID Plot Group, type Bending Moment in the Label text field.
- 3 Locate the Plot Settings section. In the y-axis label text field, type Moment [N*m].

Line Grabh I

- I In the Model Builder window, expand the Bending Moment node, then click Line Graph I.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type pipem.Myl.

Legends Out-of-plane bending moment

5 Click to expand the Quality section. From the Resolution list, choose No refinement.

Line Grabh 2

- I In the Model Builder window, click Line Graph 2.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type pipem.Mzl.
- **4** Locate the **Legends** section. In the table, enter the following settings:

Legends				
In	plane	bending	moment	

- 5 Locate the Quality section. From the Resolution list, choose No refinement.
- 6 In the Bending Moment toolbar, click **Plot**.

Shear Force

- I In the Model Builder window, right-click Bending Moment and choose Duplicate.
- 2 In the Settings window for ID Plot Group, type Shear Force in the Label text field.
- 3 Locate the Plot Settings section. In the y-axis label text field, type Force [N].

Line Graph 1

- I In the Model Builder window, expand the Shear Force node, then click Line Graph I.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type pipem.Tzl.
- **4** Locate the **Legends** section. In the table, enter the following settings:

Legends Out-of-plane shear force

Line Graph 2

- I In the Model Builder window, click Line Graph 2.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type pipem. Tyl.

```
Legends
In-plane shear force
```

5 In the Shear Force toolbar, click Plot.

Stress contributions

- I In the Home toolbar, click Add Plot Group and choose ID Plot Group.
 - Finally, create a plot to compare different stress contributions.
- 2 In the Settings window for ID Plot Group, type Stress contributions in the Label text field.
- 3 Locate the **Plot Settings** section.
- 4 Select the y-axis label check box. In the associated text field, type Stress [MPa].
- 5 Locate the Legend section. From the Position list, choose Middle right.

Line Graph 1

- I Right-click Stress contributions and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the Selection section.
- **3** From the **Selection** list, choose **All edges**.
- 4 Locate the y-Axis Data section. In the Expression text field, type pipem. shm.
- 5 From the Unit list, choose MPa.
- **6** Locate the **Title** section. From the **Title type** list, choose **None**.
- 7 Locate the **Legends** section. Select the **Show legends** check box.
- 8 From the Legends list, choose Manual.
- **9** In the table, enter the following settings:

Legends Hoop stress

Line Graph 2

- I Right-click Line Graph I and choose Duplicate.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type pipem.sn.

Legends Axial stress

Line Graph 3

- I Right-click Line Graph 2 and choose Duplicate.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- 3 In the Expression text field, type pipem.sb1.
- **4** Locate the **Legends** section. In the table, enter the following settings:

Legends Bending stress, in-plane

Line Graph 4

- I Right-click Line Graph 3 and choose Duplicate.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type pipem.sb2.
- **4** Locate the **Legends** section. In the table, enter the following settings:

Legends Bending stress, out-of-plane

Line Graph 5

- I Right-click Line Graph 4 and choose Duplicate.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- 3 In the Expression text field, type sqrt(pipem.txymax^2+pipem.txzmax^2).
- **4** Locate the **Legends** section. In the table, enter the following settings:

Legends Shear stress

Line Graph 6

- I Right-click Line Graph 5 and choose Duplicate.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type pipem.mises.

Legends von Mises stress