

# Journal Bearing

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# Introduction

Journal bearings are used to carry radial loads, for example, to support a rotating shaft.

A simple journal bearing consists of two rigid cylinders. The outer cylinder (bearing) wraps the inner rotating journal (shaft). Normally, the position of the journal center is eccentric with the bearing center. A lubricant fills the small annular gap or clearance between the journal and the bearing. The amount of eccentricity of the journal is related to the pressure that is generated in the bearing to balance the radial load. The lubricant is supplied through a hole or a groove and may or may not extend all around the journal.

Under normal operating conditions, the gases dissolved in the lubricant cause cavitation in the diverging clearance between the journal and the bearing. This happens because the pressure in the lubricant drops below the saturation pressure for the release of dissolved gases. The saturation pressure is normally similar to the ambient pressure. The following model does not account for cavitation and therefore predicts sub-ambient pressures. Such sub-ambient pressures are the result of the so-called Sommerfeld boundary condition. For practical purposes, these sub-ambient pressures should be neglected.

# Model Definition

The pressure in the lubricant (SAE 10 at  $70^{\circ}$  C) is governed by the Reynolds equation. For an incompressible fluid with no slip condition, the stationary Reynolds equation in the continuum range is given by

$$\nabla_t \cdot \left(\frac{-\rho h^3}{12\mu} \nabla_t p + \frac{\rho h}{2} (v_{\rm a} + v_{\rm b})\right) - \rho((\nabla_t b \cdot v_{\rm b}) - (\nabla_t a \cdot v_{\rm a})) = 0$$

In this equation,  $\rho$  is the density (SI unit: kg/m<sup>3</sup>), *h* is the lubricant thickness (SI unit: m),  $\mu$  is the viscosity (SI unit: Pa·s), *p* is the pressure (SI unit: Pa), *a* is the location (m) of the channel base,  $v_a$  is the tangential velocity (SI unit: m/s) of the channel base, *b* is the location (SI unit: m) of the solid wall, and  $v_b$  is the tangential velocity (SI unit: m/s) of the solid wall.

The rotating journal is considered to be the solid wall. Figure 1 shows the rotating journal wall on which you solve the Reynolds equation. Because the pressure is constant through the lubricant film thickness, COMSOL uses the tangential projection of the gradient operator,  $\nabla_t$ , to calculate the pressure distribution on the lubricant surface. Note that in this case the term  $\rho((\nabla_t b \cdot v_b) - (\nabla_t a \cdot v_a))$  equates to 0, so the governing equation simplifies to

$$\nabla_t \cdot \left(\frac{-\rho h^3}{12\mu} \nabla_t p + \frac{\rho h}{2} (v_a + v_b)\right) = 0$$

The lubricant thickness, h, is defined as

 $h = c(1 + \varepsilon \cos \theta)$ 

where  $c \equiv R_{\rm B} - R_{\rm J}$  is the difference between the bearing radius and the journal radius,  $\varepsilon$  is the eccentricity, and  $\theta$  is the polar angular coordinate of a point on the lubricant. Figure 2 shows the converging and diverging lubricant thickness around the journal.



Figure 1: Geometry (cylindrical journal) showing the base velocity direction with red arrows.



Figure 2: The lubricant thickness around the rotating journal.

# BORDER CONDITIONS

The pressure at the ends of the cylindrical journal is assumed to be similar to the ambient pressure. Therefore, the border conditions are

$$p = 0$$
 at  $z = 0, L$ 

where L is the length of the cylindrical journal.

# Results and Discussion

Figure 3 shows the calculated pressure distribution and pressure contours. As expected, the maximum pressure is reached in a region closer to the minimum lubricant thickness. Sub-ambient or negative pressure also results due to approximate boundary conditions. For a more accurate modeling of pressure distribution, gaseous cavitation has to be taken into account.



Figure 3: Pressure distribution and pressure contours on the journal.

# Application Library path: CFD\_Module/Thin-Film\_Flow/journal\_bearing

# Modeling Instructions

From the File menu, choose New.

# NEW

In the New window, click 🚳 Model Wizard.

## MODEL WIZARD

- I In the Model Wizard window, click 间 3D.
- 2 In the Select Physics tree, select Fluid Flow>Thin-Film Flow>Thin-Film Flow (tff).
- 3 Click Add.
- 4 Click  $\bigcirc$  Study.

5 In the Select Study tree, select General Studies>Stationary.

6 Click 🗹 Done.

## **GLOBAL DEFINITIONS**

## Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
R	0.03[m]	0.03 m	Journal radius
Н	0.05[m]	0.05 m	Journal height
С	0.03[mm]	3E-5 m	Clearance between the bearing and the journal
omega	1500/60*2*pi[rad/s]	157.08 rad/s	Journal angular velocity

#### GEOMETRY I

Cylinder I (cyl1)

- I In the **Geometry** toolbar, click **D** Cylinder.
- 2 In the Settings window for Cylinder, locate the Object Type section.
- 3 From the Type list, choose Surface.
- 4 Locate the Size and Shape section. In the Radius text field, type R.
- **5** In the **Height** text field, type H.
- 6 Click 🟢 Build All Objects.

# DEFINITIONS

Variables I

- I In the Home toolbar, click  $\partial =$  Variables and choose Local Variables.
- 2 In the Settings window for Variables, locate the Variables section.
- **3** In the table, enter the following settings:

Name	Expression	Unit	Description
angle	atan2(y,x)[rad]	rad	Angle along circumference
th	c*(1+0.6*cos(angle))	m	Lubricant film thickness

Name	Expression	Unit	Description
u_b	-omega*R*sin(angle)	m/s	x-component of journal velocity
v_b	omega*R*cos(angle)	m/s	y-component of journal velocity

#### THIN-FILM FLOW (TFF)

Fluid-Film Properties 1

- I In the Model Builder window, under Component I (comp1)>Thin-Film Flow (tff) click Fluid-Film Properties I.
- 2 In the Settings window for Fluid-Film Properties, locate the Fluid Properties section.
- **3** From the  $\rho$  list, choose **User defined**. In the associated text field, type 860[kg/m^3].
- 4 From the  $\mu$  list, choose User defined. In the associated text field, type 0.01[Pa\*s].
- **5** Locate the **Wall Properties** section. In the  $h_{w1}$  text field, type th.
- **6** Locate the **Base Properties** section. From the  $\mathbf{v}_b$  list, choose **User defined**. Specify the vector as

u_b	x
v_b	у
0	z

# Border I

As you can see in the **Border Settings** section, the default condition that applies at the cylinder ends is **Zero pressure**.

## STUDY I

In the **Home** toolbar, click **= Compute**.

## RESULTS

# Fluid Pressure (tff)

The default plot group shows the pressure field as a surface plot. Add a contour plot of the same quantity to reproduce the plot in Figure 3.

# Surface 1

- I In the Model Builder window, expand the Fluid Pressure (tff) node, then click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 From the Unit list, choose MPa.

- 4 Locate the Coloring and Style section. Click Change Color Table.
- 5 In the Color Table dialog box, select Linear>Cividis in the tree.
- 6 Click OK.
- 7 In the Settings window for Surface, locate the Coloring and Style section.
- 8 From the Color table transformation list, choose Reverse.

#### Contour I

- I In the Model Builder window, right-click Fluid Pressure (tff) and choose Contour.
- 2 In the Settings window for Contour, locate the Expression section.
- 3 From the Unit list, choose MPa.
- 4 Locate the Coloring and Style section. Click Change Color Table.
- 5 In the Color Table dialog box, select Linear>GrayScale in the tree.
- 6 Click OK.
- 7 In the Settings window for Contour, locate the Coloring and Style section.
- 8 Clear the Color legend check box.

#### Fluid Pressure (tff)

- I In the Model Builder window, click Fluid Pressure (tff).
- 2 In the Settings window for 3D Plot Group, click to expand the Title section.
- **3** From the **Title type** list, choose **Manual**.
- 4 In the Title text area, type Pressure (MPa).
- 5 In the Fluid Pressure (tff) toolbar, click 🗿 Plot.

To see the bearing from different angles just click and drag in the Graphics window.

The following steps reproduce Figure 1.

#### Velocity direction

- I In the Home toolbar, click 🚛 Add Plot Group and choose 3D Plot Group.
- 2 In the Settings window for 3D Plot Group, type Velocity direction in the Label text field.

#### Surface 1

- I Right-click Velocity direction and choose Surface.
- 2 In the Settings window for Surface, locate the Coloring and Style section.
- 3 From the Coloring list, choose Uniform.
- 4 From the Color list, choose Gray.

#### Arrow Surface 1

- I In the Model Builder window, right-click Velocity direction and choose Arrow Surface.
- 2 In the Settings window for Arrow Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>Thin-Film Flow>Wall and base properties>tff.vbx,tff.vby,tff.vbz Velocity of base.

#### Velocity direction

- I In the Model Builder window, click Velocity direction.
- 2 In the Settings window for 3D Plot Group, locate the Plot Settings section.
- **3** Clear the **Plot dataset edges** check box.
- 4 Locate the Title section. From the Title type list, choose None.

Reproduce Figure 2 by the following steps.

#### Lubricant thickness

- I In the Home toolbar, click 🚛 Add Plot Group and choose 3D Plot Group.
- 2 In the Settings window for 3D Plot Group, type Lubricant thickness in the Label text field.

#### Surface 1

- I Right-click Lubricant thickness and choose Surface.
- 2 In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>Thin-Film Flow> Wall and base properties>tff.h Total gap height m.
- 3 Locate the Expression section. From the Unit list, choose µm.
- 4 Locate the Coloring and Style section. Click Change Color Table.
- 5 In the Color Table dialog box, select Linear>Cividis in the tree.
- 6 Click OK.

#### Surface 1

- I In the Model Builder window, click Surface I.
- 2 In the Lubricant thickness toolbar, click **OM** Plot.

## Lubricant thickness

- I In the Model Builder window, click Lubricant thickness.
- 2 In the Settings window for 3D Plot Group, locate the Color Legend section.
- 3 Select the Show maximum and minimum values check box.

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