

# Modeling a Capacitive Position Sensor Using BEM

# Introduction

This electrostatics tutorial model uses the Electrostatics, Boundary Elements physics interface to model a five-terminal capacitive sensor and compute its capacitance matrix. The interelectrode capacitances (capacitance matrix elements) are influenced by the presence of a metallic test object and the model is solved for a range of test object positions. The model serves as a tutorial on how to extract lumped parameter matrices using the Stationary Source Sweep study. It is similar to the Modeling a Capacitive **Position Sensor Using FEM** model that uses the finite element method (FEM) featured in the Electrostatics physics interface. That model also provides a more comprehensive description of the Stationary Source Sweep study functionality. The main focus of this model is on how to use the boundary element method (BEM) for the task of analyzing the sensor.

## Model Definition

When using FEM, it is necessary to have a volumetric mesh in a portion of the surrounding air and in all dielectrics. An advantage of BEM is that meshing is only needed for object surfaces. More generally, the mesh is needed only on conductor surfaces and at the interfaces where dielectric properties change. For modeling the sensor and the infinite surrounding space, building the boundary mesh represented in Figure 1 is enough.



Figure 1: Mesh of the sensor.

Similarly, when introducing the metallic test object, the full geometry is shown in Figure 2 and Figure 3 (in different positions). An air domain is not necessary, and only the natural object boundaries need to be included.



Figure 2: Test object when it is far from the sensor.



Figure 3: Test object when it is approaching the sensor.

Moreover, since the metallic block moves as a rigid body, there is no need to create a new mesh when its position changes. The translation of the mesh is obtained by using the Deformed Geometry feature.

# Results and Discussion

Even though there is no mesh in the air, COMSOL Multiphysics produces default plots of the fields in volumes. One such electric potential plot is shown in Figure 4, where a slice of the electric potential in air is represented.



Figure 4: Electric potential in the infinite space outside the object.

As for the FEM-based Electrostatics interface, the capacitance matrix output is provided. Figure 5 represents the mutual capacitance matrix, in units of pF, when the test object is absent.

FEM and BEM results agree within an error margin of about 8% (considering the absolute value of the Maxwell capacitance). Changes in capacitance due to the sensed object are reproduced within about 1%. FEM and BEM should be seen as complementary methods.

Both are suitable for studying the capacitive position sensor system. The preferred method depends on the details of the simulation.



Figure 5: Mutual capacitance matrix.

Figure 6 and Figure 7 show the electric potential (log scale) with the first terminal excited and, when the test object is far from or just above the sensor, respectively. The presence of the metallic block changes the accumulated surface charge on the sensor electrodes and influences their capacitance values.



Figure 6: Cut plane of the electric potential (log scale) when the metallic block is far from the sensor.



Figure 7: Cut plane of the electric potential (log scale) when the metallic block is above the sensor.

6 | MODELING A CAPACITIVE POSITION SENSOR USING BEM

The BEM model accounts for the change in capacitance when the object is far away a lot more accurately. It can be verified that the absolute capacitance for the position shown in Figure 2 already has changed on the order of a percent with respect to the complete absence of the object.

The response of the inverse Maxwell capacitance for different positions of the test object is shown in Figure 8. The relative change is shown with respect to when the block is in the position shown in Figure 2. The blue curve in Figure 8 represents the change in inverse Maxwell self-capacitance of the electrode that initially is closest to the test object. The green curve represents the change in inverse Maxwell self-capacitance of the electrode that initially is farthest from the test object.

The absolute capacitance of an electrode may exhibit a long-term drift, so measuring relative changes in interelectrode capacitance is more robust. The ratio of relative change in inverse Maxwell self-capacitance of the first versus the last electrode is represented by the red curve in Figure 8. It is clear that the test object produces a change in the response of the nearest electrode with respect to the farthest electrode. This can trigger properly designed feeding circuitry that detects the presence of the object.



Figure 8: Change in inverse Maxwell capacitance as a function of position of the incoming metal object. The blue and green lines are the absolute changes of the nearest and the farthest electrodes, respectively. The ratio of relative change of the nearest to the farthest electrode is shown in red.

**Application Library path:** ACDC\_Module/Devices,\_Capacitive/ capacitive\_position\_sensor\_bem

# Modeling Instructions

From the File menu, choose New.

#### NEW

In the New window, click 🔗 Model Wizard.

## MODEL WIZARD

- I In the Model Wizard window, click 间 3D.
- 2 In the Select Physics tree, select AC/DC>Electric Fields and Currents>Electrostatics, Boundary Elements (esbe).
- 3 Click Add.
- 4 Click 🔿 Study.
- 5 In the Select Study tree, select Preset Studies for Selected Physics Interfaces> Stationary Source Sweep.
- 6 Click **M** Done.

#### GEOMETRY I

Block I (blk1)

- I In the **Geometry** toolbar, click 🗍 **Block**.
- 2 In the Settings window for Block, locate the Size and Shape section.
- 3 In the Width text field, type 11[cm].
- 4 In the **Depth** text field, type 11[cm].
- 5 In the **Height** text field, type 1[cm].

## Work Plane I (wp1)

- I In the Geometry toolbar, click 📥 Work Plane.
- 2 In the Settings window for Work Plane, locate the Plane Definition section.
- 3 In the z-coordinate text field, type 5[mm].
- 4 Click 📥 Show Work Plane.

Work Plane I (wpl)>Rectangle I (rl)

- I In the Work Plane toolbar, click 📃 Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- **3** In the **Width** text field, type 1[cm].
- 4 In the **Height** text field, type 11[cm].
- 5 Locate the **Position** section. In the **xw** text field, type 1[cm].

#### Work Plane I (wpI)>Array I (arrI)

- I In the Work Plane toolbar, click 👰 Transforms and choose Array.
- 2 Select the object rI only.
- 3 In the Settings window for Array, locate the Size section.
- 4 In the xw size text field, type 5.
- 5 Locate the **Displacement** section. In the **xw** text field, type 2[cm].
- 6 Click 📄 Build Selected.

## Work Plane I (wp1)

- In the Model Builder window, under Component I (comp1)>Geometry I click
   Work Plane I (wp1).
- 2 In the Settings window for Work Plane, click 📒 Build Selected.
- 3 Click the Wireframe Rendering button in the Graphics toolbar.

The next operations are needed to load materials. Pay special attention to the fact that **Air**, which is not necessarily explicitly modeled in a boundary element approach, will be added to the **Infinite void** entity, available under the **Domain Geometric entity level**.

#### ADD MATERIAL

- I In the Home toolbar, click 🙀 Add Material to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Built-in>Air.
- 4 Right-click and choose Add to Component I (compl).
- 5 In the tree, select Built-in>Nylon.
- 6 Right-click and choose Add to Component I (compl).
- 7 In the Home toolbar, click 🙀 Add Material to close the Add Material window.

## MATERIALS

Nylon (mat2) Select Domain 1 only.

Air (mat1)

- I In the Model Builder window, click Air (matl).
- 2 In the Settings window for Material, locate the Geometric Entity Selection section.
- 3 From the Selection list, choose All voids.

## ELECTROSTATICS, BOUNDARY ELEMENTS (ESBE)

## Charge Conservation 2

- In the Model Builder window, under Component I (compl) right-click Electrostatics, Boundary Elements (esbe) and choose Charge Conservation.
- **2** Select Domain 1 only.

Add ground and terminals for the feeding.

## Ground I

- I In the Physics toolbar, click 🔚 Boundaries and choose Ground.
- 2 Select Boundary 3 only.

#### Terminal I

- I In the Physics toolbar, click 🔚 Boundaries and choose Terminal.
- 2 Select Boundary 6 only.

#### Terminal 2

- I In the Physics toolbar, click 📄 Boundaries and choose Terminal.
- **2** Select Boundary 7 only.

## Terminal 3

- I In the Physics toolbar, click 🔚 Boundaries and choose Terminal.
- 2 Select Boundary 8 only.

## Terminal 4

- I In the Physics toolbar, click 🔚 Boundaries and choose Terminal.
- 2 Select Boundary 9 only.

#### Terminal 5

I In the Physics toolbar, click 🔚 Boundaries and choose Terminal.

**2** Select Boundary 10 only.

Generate the physics induced mesh for the sensor, which should be similar Figure 1 in the introduction.

## MESH I

- I In the Model Builder window, under Component I (compl) click Mesh I.
- 2 In the Settings window for Mesh, locate the Physics-Controlled Mesh section.
- 3 From the Element size list, choose Finer.
- 4 Click 📗 Build All.

The problem could be directly solved as it is, but for optimizing solution performance, direct solver and linear elements are selected.

## ELECTROSTATICS, BOUNDARY ELEMENTS (ESBE)

- In the Model Builder window, under Component I (compl) click Electrostatics, Boundary Elements (esbe).
- **2** In the **Settings** window for **Electrostatics**, **Boundary Elements**, click to expand the **Discretization** section.
- 3 From the Electric potential/Surface charge density list, choose Linear/Linear.

## STUDY I

Solution 1 (soll)

- I In the Study toolbar, click **here** Show Default Solver.
- 2 In the Model Builder window, expand the Solution I (soll) node.
- 3 In the Model Builder window, expand the Study I>Solver Configurations> Solution I (soll)>Stationary Solver I node.
- 4 Right-click Study I>Solver Configurations>Solution I (sol1)>Stationary Solver I>Direct and choose Enable.
- **5** In the **Study** toolbar, click **= Compute**.

### RESULTS

#### Electric Potential (esbe)

Make the following modification to the default graphs to reproduce figures in the introduction. Notice that the potential is displayed also in the unmeshed air regions.

#### Streamline Multislice 1

- I In the Model Builder window, expand the Electric Potential (esbe) node.
- 2 Right-click Streamline Multislice I and choose Disable.

#### Multislice 1

- I In the Model Builder window, click Multislice I.
- 2 In the Settings window for Multislice, locate the Multiplane Data section.
- 3 Find the x-planes subsection. In the Planes text field, type 0.
- 4 Find the z-planes subsection. In the Planes text field, type 0.
- **5** In the **Electric Potential (esbe)** toolbar, click **O Plot**.

The next operations generate the lumped capacitance matrices and a 2D plot of the mutual capacitance matrix. The plot should be similar to Figure 5 in the introduction.

Lumped Parameters (dset1, esbe)

In the Model Builder window, expand the Results>Lumped Parameters (dset1, esbe) node.

Maxwell capacitance (dset1, esbe)

In the Model Builder window, expand the Results>Lumped Parameters (dset1, esbe)> Maxwell capacitance (dset1, esbe) node.

Maxwell capacitance (dset1, esbe)

- I In the Model Builder window, expand the Results>Lumped Parameters (dset1, esbe)> Mutual capacitance (dset1, esbe) node, then click Results>Lumped Parameters (dset1, esbe)>Maxwell capacitance (dset1, esbe)>Maxwell capacitance (dset1, esbe).
- 2 In the Settings window for Global Matrix Evaluation, locate the Expression section.
- 3 From the Unit list, choose I/pF.

## Mutual capacitance (dset1, esbe)

- I In the Model Builder window, under Results>Lumped Parameters (dset1, esbe)> Mutual capacitance (dset1, esbe) click Mutual capacitance (dset1, esbe).
- 2 In the Settings window for Global Matrix Evaluation, locate the Expression section.
- **3** From the **Unit** list, choose **I/pF**.
- **4** In the **Results** toolbar, click **= Evaluate** and choose **Clear and Evaluate All**.

## TABLE

- I Go to the Table window.
- 2 Click Table Surface in the window toolbar.

## RESULTS

Table Surface 1

- I In the Model Builder window, under Results>2D Plot Group 3 click Table Surface I.
- 2 In the Settings window for Table Surface, locate the Data section.
- 3 From the Data format list, choose Cells.
- 4 Locate the Coloring and Style section. From the Function list, choose Discrete.

2D Plot Group 3

- I In the Model Builder window, click 2D Plot Group 3.
- 2 In the Settings window for 2D Plot Group, click to expand the Title section.
- 3 From the Title type list, choose Manual.
- 4 In the Title text area, type Mutual capacitance matrix [pF].
- 5 In the 2D Plot Group 3 toolbar, click 💽 Plot.
- 6 Click the **Zoom Extents** button in the **Graphics** toolbar.

# Addition of the sensed metallic object

Next, a metallic block is placed close to the sensor. The accumulated charge on the terminals will be influenced by the block. This makes it possible to determine the position of the block. As air does not need to be modeled, remeshing is not strictly necessary. To avoid remeshing the displacement is included by adding a **Deformed Geometry** node, meshing sensor and block in their base position. The displacement **L** is then applied to the **Deformed Geometry** and does not appear in the geometry.

## GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 In the table, enter the following settings:

Name	Expression	Value	Description
L	2[cm]	0.02 m	Displacement

#### GEOMETRY I

Block 2 (blk2)

- I In the **Geometry** toolbar, click **[]** Block.
- 2 In the Settings window for Block, locate the Object Type section.
- 3 From the Type list, choose Surface.
- 4 Locate the Size and Shape section. In the Width text field, type 25[cm].
- 5 In the **Depth** text field, type 5[cm].
- 6 In the **Height** text field, type 8[cm].
- 7 Locate the **Position** section. In the x text field, type -35[cm].
- 8 In the y text field, type 3[cm].
- 9 In the z text field, type 2[cm].

10 Click 🟢 Build All Objects.

## COMPONENT I (COMPI)

Prescribed Deformation 1

In the Definitions toolbar, click • • • Deformed Geometry and choose Domains> Prescribed Deformation.

## DEFORMED GEOMETRY

## Prescribed Deformation 1

- In the Model Builder window, expand the Component I (compl)>Definitions node, then click Component I (compl)>Deformed Geometry>Prescribed Deformation I.
- **2** In the **Settings** window for **Prescribed Deformation**, locate the **Geometric Entity Selection** section.
- 3 From the Geometric entity level list, choose Boundary.
- **4** Select Boundaries 1–6 only.
- **5** Locate the **Prescribed Deformation** section. Specify the dx vector as

## L X

The block boundaries are defined as an equipotential with no net accumulated charge, by assigning the **Floating Potential** boundary condition to the block boundaries. In this model, there is no need to know the interior material properties of the block as there will be no resulting electric fields inside.

## ELECTROSTATICS, BOUNDARY ELEMENTS (ESBE)

Floating Potential 1

- I In the Physics toolbar, click 🔚 Boundaries and choose Floating Potential.
- **2** Select Boundaries 1–6 only.
- 3 In the Model Builder window, click Electrostatics, Boundary Elements (esbe).
- **4** In the **Settings** window for **Electrostatics**, **Boundary Elements**, locate the **Domain Selection** section.
- 5 In the list, select Finite void I.
- 6 Click Remove from Selection.
- **7** Select Domains –1 only.

## MESH I

- I In the Model Builder window, under Component I (compl) click Mesh I.
- 2 In the Settings window for Mesh, locate the Physics-Controlled Mesh section.
- 3 From the Element size list, choose Extremely fine.
- 4 Click 📗 Build All.

## STUDY I

Parametric Sweep

- I In the Study toolbar, click **Parametric Sweep**.
- 2 In the Settings window for Parametric Sweep, locate the Study Settings section.

3 Click + Add.

**4** In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
L (Displacement)	range(2,2,28)	cm

**5** In the **Study** toolbar, click **= Compute**.

## RESULTS

#### Electric Potential (esbe) 1

Once the solution is generated, the postprocessing can be performed. The creation of the cut plane in air is first performed.

#### Surface 1

- I In the Model Builder window, expand the Electric Potential (esbe) I node.
- 2 Right-click Surface I and choose Disable.

#### Electric Potential (esbe) 1

- I In the Model Builder window, click Electric Potential (esbe) I.
- 2 In the Settings window for 3D Plot Group, locate the Data section.
- **3** Click **Go to Source**.

## Grid 3D 2

- I In the Model Builder window, under Results>Datasets click Grid 3D 2.
- 2 In the Settings window for Grid 3D, locate the Parameter Bounds section.
- **3** Find the **First parameter** subsection. In the **Minimum** text field, type -0.2.
- 4 In the Maximum text field, type 0.2.
- 5 Click to expand the Grid section. In the x resolution text field, type 100.

#### Streamline Multislice I

- I In the Model Builder window, under Results>Electric Potential (esbe) I right-click Streamline Multislice I and choose Disable.
- 2 Click the **J** Go to Default View button in the Graphics toolbar.

#### Multislice I

- I In the Model Builder window, click Multislice I.
- 2 In the Settings window for Multislice, locate the Multiplane Data section.
- 3 Find the x-planes subsection. In the Planes text field, type 0.
- 4 Find the z-planes subsection. In the Planes text field, type 0.
- 5 In the Electric Potential (esbe) I toolbar, click 🗿 Plot.
- 6 Click the  $\sqrt{-}$  Go to Default View button in the Graphics toolbar.
- 7 Click the 🕂 Zoom Extents button in the Graphics toolbar.

#### Electric Potential (esbe) 1

- I In the Model Builder window, click Electric Potential (esbe) I.
- 2 In the Settings window for 3D Plot Group, locate the Data section.
- 3 From the Parameter value (L (cm)) list, choose 2.
- 4 In the Electric Potential (esbe) I toolbar, click 🗿 Plot.

As the potential differences due to the change of position for the moving object are difficult to notice in linear scale, display the logarithm of the electric potential.

Multislice 1

- I In the Model Builder window, click Multislice I.
- 2 In the Settings window for Multislice, locate the Expression section.
- 3 In the **Expression** text field, type log10(esbe.V).
- 4 Click to expand the Range section. Select the Manual color range check box.
- **5** In the **Minimum** text field, type -4.
- 6 In the Maximum text field, type 0.
- 7 In the Electric Potential (esbe) I toolbar, click 🗿 Plot.

Electric Potential (esbe) 1

- I In the Model Builder window, click Electric Potential (esbe) I.
- 2 In the Settings window for 3D Plot Group, locate the Data section.
- 3 From the Parameter value (PortName) list, choose I.

The resulting plot for the object positioned far from the sensing electrodes should be similar to Figure 6 in the introduction. By changing the value of the displacement L, plots of the potential at other positions can be produced.

- **4** In the **Electric Potential (esbe) I** toolbar, click **I Plot**.
- 5 From the Parameter value (L (cm)) list, choose 10.



#### 17 | MODELING A CAPACITIVE POSITION SENSOR USING BEM

Finally, produce a plot of the change of the capacitance as a function of the change in position of the object. The results are similar to those in the *Capacitive Position Sensor* tutorial model, where the **Electrostatics** physics interface is used. The discrepancies between the results are mainly due to the different boundary conditions.

## ID Plot Group 6

- I In the Home toolbar, click 🚛 Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, locate the Data section.
- 3 From the Dataset list, choose Study I/Parametric Solutions I (sol2).
- 4 From the Parameter selection (PortName) list, choose First.
- 5 Click to expand the Title section. From the Title type list, choose Manual.
- 6 In the Title text area, type Relative change of capacitance.

Global I

- I Right-click ID Plot Group 6 and choose Global.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
<pre>with(1,esbe.Cinv11)/ withsol('sol2',with(1, esbe.Cinv11),setval(L, 0.02))</pre>	1	Terminal 1
<pre>with(5,esbe.Cinv55)/ withsol('sol2',with(5, esbe.Cinv55),setval(L, 0.02))</pre>	1	Terminal 5
<pre>with(5,esbe.Cinv55)/with(1, esbe.Cinv11)/ withsol('sol2',with(5, esbe.Cinv55)/with(1, esbe.Cinv11),setval(L, 0.02))</pre>	1	Ratio of capacitances for terminal 1 vs. 5

4 Locate the x-Axis Data section. From the Axis source data list, choose L.

5 Click to expand the Legends section. From the Legends list, choose Manual.

**6** In the table, enter the following settings:

Legends	
Change on terminal	1
Change on terminal	5
Relative change of	1 vs. 5

7 In the **ID Plot Group 6** toolbar, click **Plot**. The resulting plot should reproduce Figure 8 in the introduction.

20 | MODELING A CAPACITIVE POSITION SENSOR USING BEM