



# Metal Processing Module

User's Guide

# Metal Processing Module User's Guide

© 1998–2022 COMSOL

Protected by patents listed on [www.comsol.com/patents](http://www.comsol.com/patents), or see Help>About COMSOL Multiphysics on the File menu in the COMSOL Desktop for a less detailed lists of U.S. Patents that may apply. Patents pending.

This Documentation and the Programs described herein are furnished under the COMSOL Software License Agreement ([www.comsol.com/sla](http://www.comsol.com/sla)) and may be used or copied only under the terms of the license agreement.

COMSOL, the COMSOL logo, COMSOL Multiphysics, COMSOL Desktop, COMSOL Compiler, COMSOL Server, and LiveLink are either registered trademarks or trademarks of COMSOL AB. All other trademarks are the property of their respective owners, and COMSOL AB and its subsidiaries and products are not affiliated with, endorsed by, sponsored by, or supported by those trademark owners. For a list of such trademark owners, see [www.comsol.com/trademarks](http://www.comsol.com/trademarks).

Version: COMSOL 6.1

## Contact Information

Visit the Contact COMSOL page at [www.comsol.com/contact](http://www.comsol.com/contact) to submit general inquiries or search for an address and phone number. You can also visit the Worldwide Sales Offices page at [www.comsol.com/contact/offices](http://www.comsol.com/contact/offices) for address and contact information.

If you need to contact Support, an online request form is located on the COMSOL Access page at [www.comsol.com/support/case](http://www.comsol.com/support/case). Other useful links include:

- Support Center: [www.comsol.com/support](http://www.comsol.com/support)
- Product Download: [www.comsol.com/product-download](http://www.comsol.com/product-download)
- Product Updates: [www.comsol.com/support/updates](http://www.comsol.com/support/updates)
- COMSOL Blog: [www.comsol.com/blogs](http://www.comsol.com/blogs)
- Discussion Forum: [www.comsol.com/forum](http://www.comsol.com/forum)
- Events: [www.comsol.com/events](http://www.comsol.com/events)
- COMSOL Video Gallery: [www.comsol.com/videos](http://www.comsol.com/videos)
- Support Knowledge Base: [www.comsol.com/support/knowledgebase](http://www.comsol.com/support/knowledgebase)

Part number: CM025001

# C o n t e n t s

## Chapter 1: Introduction

<b>About the Metal Processing Module</b>	<b>8</b>
What Can the Metal Processing Module Do? . . . . .	8
Where Do I Access the Documentation and Application Libraries? . . . . .	9
<b>Overview of the User's Guide</b>	<b>12</b>

## Chapter 2: Metal Processing Modeling

<b>Selecting Physics Interfaces</b>	<b>16</b>
Metal Phase Transformation . . . . .	16
Austenite Decomposition . . . . .	17
Alpha-Beta Phase Transformation . . . . .	17
Carburization . . . . .	18
<b>Study Types</b>	<b>19</b>
<b>Modeling Phase Transformations</b>	<b>20</b>
Metallurgical Phases . . . . .	20
Phase Transformations . . . . .	20
Calibration of Phase Transformation Models . . . . .	23
<b>Defining Multiphysics Models</b>	<b>28</b>
Heat Transfer with Phase Transformations . . . . .	28
Steel Quenching . . . . .	29
Phase Transformation Latent Heat . . . . .	30
Phase Transformation Strain . . . . .	30
<b>Selecting Discretizations</b>	<b>31</b>
Phase Transformation Modeling . . . . .	31
Carburization Modeling . . . . .	31

<b>Using Effective Material Properties</b>	<b>32</b>
<b>Importing Material Properties and Phase Transformation Data</b>	<b>33</b>
Material Properties . . . . .	33
Phase Transformation Data . . . . .	33
<b>Modeling Carburization</b>	<b>35</b>
Defining a Carburization Environment. . . . .	35
Modeling Carbon Diffusion . . . . .	35
Boundary Conditions . . . . .	36
<b>References</b>	<b>37</b>

## Chapter 3: Metal Processing Theory

<b>Metal Phase Transformation Theory</b>	<b>40</b>
<b>Metallurgical Phase Transformations</b>	<b>41</b>
Definitions . . . . .	41
Phase Transformation Models . . . . .	43
Parameterized TTT Diagram . . . . .	52
<b>Compound Material Properties</b>	<b>54</b>
Heat Transfer Properties. . . . .	54
Electromagnetic Properties . . . . .	55
Mechanical Properties . . . . .	55
<b>Phase Transformation Strains</b>	<b>58</b>
Thermal Expansion . . . . .	58
Transformation-Induced Plasticity . . . . .	59
Total Strain Contribution . . . . .	60

<b>Phase Transformation Latent Heat</b>	<b>61</b>
<b>Carburization</b>	<b>62</b>
Carbon Potential Model . . . . .	62
Boundary Conditions . . . . .	63
<b>References</b>	<b>65</b>

## Chapter 4: Metal Phase Transformation

<b>The Metal Phase Transformation Interface</b>	<b>68</b>
Metallurgical Phase . . . . .	70
Phase Transformation . . . . .	73
Transformation Condition . . . . .	77
Additional Source Phase . . . . .	77

## Chapter 5: Austenite Decomposition

<b>The Austenite Decomposition Interface</b>	<b>80</b>
--	-----------

## Chapter 6: Alpha-Beta Phase Transformation

<b>The Alpha-Beta Phase Transformation Interface</b>	<b>84</b>
--	-----------

## Chapter 7: Carburization

<b>The Carburization Interface</b>	<b>88</b>
Carburization . . . . .	88
Carbon Flux. . . . .	89
Zero Carbon Flux . . . . .	89
Carbon Concentration . . . . .	89
Initial Values . . . . .	89

## Chapter 8: Multiphysics Interfaces and Couplings

<b>Heat Transfer with Phase Transformations</b>	<b>92</b>
On the Constituent Physics Interfaces . . . . .	92
<b>Steel Quenching</b>	<b>93</b>
On the Constituent Physics Interfaces . . . . .	93
<b>Phase Transformation Latent Heat Multiphysics Coupling</b>	<b>94</b>
<b>Phase Transformation Strain Multiphysics Coupling</b>	<b>96</b>

# Introduction

This guide describes the Metal Processing Module, an optional add-on package for the COMSOL Multiphysics® simulation software. The module is designed to perform transient analyses of processes involving metallurgical (solid-solid) phase transformations in, mainly, steels. This chapter introduces you to the capabilities of the Metal Processing Module and includes a summary of the physics interfaces and where you can find the documentation.

In this chapter:

- [About the Metal Processing Module](#)

# About the Metal Processing Module

In this section:

- [What Can the Metal Processing Module Do?](#)
- [Where Do I Access the Documentation and Application Libraries?](#)

## *What Can the Metal Processing Module Do?*

---

The Metal Processing Module can be used to model different physical phenomena related to heat treatment of metals. Using this module, you can study how metallurgical phase transformations change the microstructure of a metallic material during a heating or cooling process. One example is the quenching of automotive steel transmission components, where the resulting microstructure is tailored to meet specific demands on strength and durability. Other examples include the study of phase transformations that occur during additive manufacturing of metal components and phase transformations in the heat-affected zone during welding.

There are five physics interfaces in the Metal Processing Module:

- The *Metal Phase Transformation* interface for studying diffusive and displacive metallurgical phase transformations in materials like steels.
- The *Austenite Decomposition* interface for specifically studying the cooling of steel from an austenitic state.
- The *Alpha-Beta Phase Transformation* interface for specifically studying thermal transients in  $\alpha$ - $\beta$  titanium alloys.
- The *Carburization* interface for studying the heat treatment process of carburization.
- The *Heat Transfer with Phase Transformations* interface for modeling thermal processes involving metallurgical phase transformations.
- The *Steel Quenching* interface for modeling coupled thermal and mechanical processes involving metallurgical phase transformations.

Throughout the *Metal Processing User's Guide*, the Metal Phase Transformation, the Austenite Decomposition, and the Alpha-Beta Phase Transformation physics interfaces are collectively referred to as *phase transformation* physics interfaces.



The physics interfaces in the Metal Processing Module can be added from the Model Wizard's **Select Physics** page under **Heat Transfer>Metal Processing**. The physics interfaces can also be added by right-clicking a **Component** node and selecting **Add Physics**.

### *Where Do I Access the Documentation and Application Libraries?*

---

#### **ACCESSING THE METAL PROCESSING MODULE DOCUMENTATION**

The Metal Processing Module feature information, including theory and modeling details, is included in the *Metal Processing Module User's Guide*.

When you install COMSOL Multiphysics, the documentation sets are installed in several locations, both on your computer and most easily accessible while you are working in COMSOL Multiphysics. The next section details where to access it.

#### **ACCESSING COMSOL DOCUMENTATION AND APPLICATION LIBRARIES**

A number of online resources have more information about COMSOL, including licensing and technical information. The electronic documentation, topic-based (or context-based) help, and the Application Libraries are all accessed through the COMSOL Desktop.



If you are reading the documentation as a PDF file on your computer, the [blue links](#) do not work to open an application or content referenced in a different guide. However, if you are using the Help system in COMSOL Multiphysics, these links work to open other modules, application examples, and documentation sets.

---

#### **THE DOCUMENTATION AND ONLINE HELP**

The *COMSOL Multiphysics Reference Manual* describes the core physics interfaces and functionality included with the COMSOL Multiphysics license. This book also has instructions on how to use COMSOL Multiphysics and how to access the electronic Documentation and Help content.

##### *Opening Topic-Based Help*

The Help window is useful as it is connected to the features in the COMSOL Desktop. To learn more about a node in the Model Builder, or a window on the Desktop, click to highlight a node or window, then press F1 to open the Help window, which then displays information about that feature (or click a node in the Model Builder followed



## *Opening the Documentation Window*

### **THE APPLICATION LIBRARIES WINDOW**

Each model or application includes documentation with the theoretical background and step-by-step instructions to create a model or application. The models and applications are available in COMSOL Multiphysics as MPH-files that you can open for further investigation. You can use the step-by-step instructions and the actual models as templates for your own modeling. In most models, SI units are used to describe the relevant properties, parameters, and dimensions, but other unit systems are available.

Once the Application Libraries window is opened, you can search by name or browse under a module folder name. Click to view a summary of the model or application and its properties, including options to open it or its associated PDF document.

### *Opening the Application Libraries Window*

To open the **Application Libraries** window ():

### **CONTACTING COMSOL BY EMAIL**

For general product information, contact COMSOL at [info@comsol.com](mailto:info@comsol.com).

### **COMSOL ACCESS AND TECHNICAL SUPPORT**

To receive technical support from COMSOL for the COMSOL products, please contact your local COMSOL representative or send your questions to [support@comsol.com](mailto:support@comsol.com). An automatic notification and a case number will be sent to you by email. You can also access technical support, software updates, license information, and other resources by registering for a COMSOL Access account.

## COMSOL ONLINE RESOURCES

COMSOL website	<a href="http://www.comsol.com">www.comsol.com</a>
Contact COMSOL	<a href="http://www.comsol.com/contact">www.comsol.com/contact</a>
COMSOL Access	<a href="http://www.comsol.com/access">www.comsol.com/access</a>
Support Center	<a href="http://www.comsol.com/support">www.comsol.com/support</a>
Product Download	<a href="http://www.comsol.com/product-download">www.comsol.com/product-download</a>
Product Updates	<a href="http://www.comsol.com/support/updates">www.comsol.com/support/updates</a>
COMSOL Blog	<a href="http://www.comsol.com/blogs">www.comsol.com/blogs</a>
Discussion Forum	<a href="http://www.comsol.com/forum">www.comsol.com/forum</a>
Events	<a href="http://www.comsol.com/events">www.comsol.com/events</a>
COMSOL Application Gallery	<a href="http://www.comsol.com/models">www.comsol.com/models</a>
COMSOL Video Gallery	<a href="http://www.comsol.com/video">www.comsol.com/video</a>
Support Knowledge Base	<a href="http://www.comsol.com/support/knowledgebase">www.comsol.com/support/knowledgebase</a>

# Overview of the User's Guide

## **TABLE OF CONTENTS AND INDEX**

To help you navigate this guide, see the Contents and Index sections.

## **MODELING WITH THE METAL PROCESSING MODULE**

The Metal Processing Modeling chapter discusses how to model different problems involving phase transformations. The content covers the topics Selecting Physics Interfaces, Study Types, Modeling Phase Transformations, Defining Multiphysics Models, Selecting Discretizations, and Using Effective Material Properties.

## **METAL PROCESSING THEORY**

The Metal Processing Theory chapters outlines the theory for the interfaces present in the Metal Processing Module. The chapter covers the topics Metallurgical Phase Transformations, Compound Material Properties, Phase Transformation Strains, Phase Transformation Latent Heat, and Carburization.

## **THE METAL PHASE TRANSFORMATION INTERFACE**

The Metal Phase Transformation chapter describes the Metal Phase Transformation interface and its feature nodes.

## **THE AUSTENITE DECOMPOSITION INTERFACE**

The Austenite Decomposition chapter describes the Austenite Decomposition interface and how it is based on the Metal Phase Transformation interface.

## **THE ALPHA-BETA PHASE TRANSFORMATION INTERFACE**

The Alpha-Beta Phase Transformation chapter describes the Alpha-Beta Phase Transformation interface, and how it is based on the Metal Phase Transformation interface.

## **THE CARBURIZATION INTERFACE**

The Carburization chapter describes the Carburization interface and its feature nodes.

## MULTIPHYSICS INTERFACES AND COUPLINGS

The Multiphysics Interfaces and Couplings chapter describes two multiphysics interfaces found under the Metal Processing branch when adding a physics interface:

- The Heat Transfer with Phase Transformations interface combines a Metal Phase Transformation interface with a Heat Transfer in Solids interface. The coupling of the interfaces appears on a domain level, where produced latent heat from the (temperature-dependent) phase transformations gives rise to a heat source in the heat equation. Optionally, phase-composition-dependent thermal material properties can be used in the heat transfer analysis.
- The Steel Quenching Interface combines an Austenite Decomposition interface with a Heat Transfer in Solids interface and a Solid Mechanics interface. There are two domain-level multiphysics couplings: In the first coupling, produced latent heat from the (temperature-dependent) phase transformations gives rise to a heat source in the heat equation. In the second coupling, phase transformation strains that result from thermal expansion or transformation-induced plasticity (TRIP) are transferred to the Solid Mechanics interface as inelastic strain contributions for the computation of stresses. In the case of plasticity, the coupling also involves equivalent plastic strains and hardening functions. Optionally, phase-composition-dependent thermal and mechanical properties can be used in the heat transfer and solid mechanics analyses.
- The Phase Transformation Latent Heat multiphysics coupling adds the latent heat that is produced during phase transformations, as a heat source term, to the heat equation in a Heat Transfer interface.
- The Phase Transformation multiphysics coupling adds the transformation strains that are produced during phase transformations, as an inelastic strain contribution, to the equation for stress in a Solid Mechanics interface. The coupling also transfers stresses and the equivalent plastic strain from a Solid Mechanics interface to the coupled phase transformation interface.



# Metal Processing Modeling

The goal of this chapter is to show you how to model different problems involving phase transformations in steels and how to include various physical phenomena that may be relevant in specific situations.

In this chapter:

- [Selecting Physics Interfaces](#)
- [Study Types](#)
- [Modeling Phase Transformations](#)
- [Defining Multiphysics Models](#)
- [Selecting Discretizations](#)
- [Using Effective Material Properties](#)
- [Importing Material Properties and Phase Transformation Data](#)
- [Modeling Carburization](#)

# Selecting Physics Interfaces

The Metal Processing Module contains three basic physics interfaces and two multiphysics interfaces. The three basic physics interfaces are:

- [Metal Phase Transformation](#) — For modeling general metallurgical phase transformations
- [Austenite Decomposition](#) — For modeling the specific case of austenite decomposing into a combination of destination phases, on cooling
- [Alpha-Beta Phase Transformation](#) — For modeling phase transformations in  $\alpha$ - $\beta$  titanium alloys.
- [Carburization](#) — For modeling carburization; the process by which carbon from a surrounding carbon rich environment diffuses into a component.

## *Metal Phase Transformation*

---

The Metal Phase Transformation interface provides a basic way to model phase transformations in metals. Four common models for phase transformations in steels are provided. The Leblond–Devaux, the Johnson–Mehl–Avrami–Kolmogorov (JMAK), the Kirkaldy–Venugopalan, and the Hyperbolic rate models are used to model time-dependent (diffusion-controlled) phase transformations, such as the transformation of austenite into pearlite during steel hardening. In contrast, the Koistinen–Marburger model is used to model the transformation of austenite into martensite, where the amount of undercooling below the so-called martensite start temperature controls the formation of martensite. In addition to these five types of phase transformations, you can define your own phase transformation models and let them coexist with other active phase transformations in your analysis. You can use an arbitrary number of phase transformations in a model. The Metal Phase Transformation interface lets you generate a compound material whose properties are phase composition dependent. This material can be used by other physics interfaces, such as Solid Mechanics and Heat Transfer in Solids.



- [Modeling Phase Transformations](#)
  - [Metallurgical Phase Transformations](#)
-



## *Austenite Decomposition*

---

The Austenite Decomposition interface is a specialized interface that considers hardening of steel from an austenitic state. During hardening of steels, the material is heated above the austenitizing temperature. It is then cooled, and depending on the rate of cooling, a combination of destination phases such as ferrite, pearlite, bainite, and martensite can form. The Austenite Decomposition interface automatically creates corresponding phase nodes and phase transformation nodes. You can also define an arbitrary number of additional phases and phase transformations. Optionally, you can define your own phase transformation models and let them coexist with other active phase transformations in the analysis. The Austenite Decomposition interface lets you generate a compound material whose properties are phase-composition dependent. This material can be used by other physics interfaces, such as Solid Mechanics and Heat Transfer in Solids.



- [Modeling Phase Transformations](#)
  - [Metallurgical Phase Transformations](#)
- 

## *Alpha-Beta Phase Transformation*

---

The Alpha-Beta Phase Transformation interface is a specialized interface that is used to model phase transformations in  $\alpha$ - $\beta$  titanium alloys, such as Ti-6Al-4V. These alloys find uses in welding as well as additive manufacturing. In these applications, the material typically undergoes both heating and cooling, and depending on the rates at which this happens, different fractions of beta phase and alpha phases can form. The Alpha-Beta Phase Transformation interface automatically creates phase nodes and phase transformation nodes. In addition, transformation conditions are imposed the phase transformation nodes to, for example, restrict phase transformations to cooling or heating. The Alpha-Beta Phase Transformation interface lets you generate a compound material whose properties are phase-composition dependent. This material can be used by other physics interfaces, such as Solid Mechanics and Heat Transfer in Solids.



- [Modeling Phase Transformations](#)
  - [Metallurgical Phase Transformations](#)
-

## *Carburization*

---

The Carburization interface provides a way to model the heat treatment process of carburization. The process involves placing a component in a carbon rich environment, at an elevated temperature. Over time, carbon is transferred into the surface of the component, and then progresses to the interior via diffusion. You can specify the carbon potential (the carbon concentration of the surrounding environment) as a function of time, to emulate a particular process. Or, you can use a simplified boost-diffuse carburization cycle that is provided by the interface. You can model the mass transfer of carbon into the surface of the component in different ways. You can prescribe the carbon concentration at the surface, or use a convective, thermally activated carbon mass transfer. Additionally, you can model selective carburization by prescribing zero carbon flux in certain regions of the component surface.

# Study Types

Metallurgical Phase transformations are inherently time dependent. Phase transformations are defined by a set of ordinary differential equations in time. The Carburization interface solves the time-dependent diffusion of carbon in a component. The only supported study type for the Metal Processing physics interfaces is therefore Time Dependent.



In the *COMSOL Multiphysics Reference Manual*:

- [Time-Dependent Solver](#)
  - [Studies and Solvers](#)
-

# Modeling Phase Transformations

This section describes how to model metallurgical solid-solid phase transformations. When you simulate processes such as hardening of steel, these phase transformations are fundamental because they ultimately determine the final properties of the material. In the phase transformation interfaces, each phase transformation is defined by a certain evolution equation that defines the time rate of change of the algebraic proportion of a destination phase at the expense of a source phase. In the following, the two modeling concepts of phases and phase transformations are discussed.

## *Metallurgical Phases*

---

When you model phase transformations in a material, each transformation defines how a source phase transforms into a destination phase as a function of time. When you create a metallurgical phase node, you have to define its initial phase fraction. This is the value from which the phase fraction evolves during the analysis.

You have the option, at the physics interface level, to compute effective thermal, electromagnetic, and mechanical properties for the compound material. If you have opted to do this, you also need to define the corresponding properties of each phase. At each phase node, you can choose to create a component-level phase material. This material can be populated with properties that define the behavior of the phase. As an alternative, you can use imported material properties. This is described in [Importing Material Properties and Phase Transformation Data](#).

The phase material properties are averaged (phase-fraction averaged) into effective material properties of a compound material that can be used in other physics interfaces. This is described in [Using Effective Material Properties](#).

## *Phase Transformations*

---

When you have created a phase transformation node, you have to choose a source phase and a destination phase. These are the two phases that are fundamentally involved in the phase transformation. You also have the option of specifying additional source phases that contribute to the formation of the destination phase. The selected phase transformation model defines the underlying type of phase transformation. They are described below.

## THE LEBLOND–DEVAUX MODEL

Phase transformations in steels are based on diffusion of carbon, and the Leblond–Devaux phase transformation model is suitable to model this. You can choose between four formulations for the model — **General coefficients, Time and equilibrium, TTT diagram data**, and **Parameterized TTT diagram**. The first and second formulations require generally temperature-dependent functions that determine the characteristics of the phase transformation. The functions will be different for different phase transformations. The **TTT diagram data** formulation requires information that can be extracted from a TTT diagram, namely the time it takes at each temperature to reach a specified relative phase fraction. Typically, you would choose the transformation start line (for example, 1%). The **Parameterized TTT diagram** formulation is used to input three points from a TTT diagram, and let COMSOL Multiphysics construct a simplified TTT diagram using these points and additional curve shape parameters. The constructed TTT diagram is used internally to calculate the required parameters for the phase transformation model.



### The Leblond–Devaux Model

---

## THE JOHNSON–MEHL–AVRAMI–KOLMOGOROV (JMAK) MODEL

You can choose between five formulations for the model — **Time, equilibrium, and exponent, TTT diagram data, TTT diagram data, fixed exponent, Parameterized TTT diagram**, and **Parameterized TTT diagram, fixed exponent**. The first formulation can be viewed as a generalization of the **Time and equilibrium** form of the Leblond–Devaux model. In addition to the generally time-dependent functions describing the equilibrium phase fraction and the time constant, a time-dependent exponent is used. The exponent is called the Avrami exponent, and it alters the characteristic of the phase transformation. The **TTT diagram data** and **TTT diagram data, fixed exponent formulations** require information that can be extracted from the curves in a TTT diagram, namely the time it takes at each temperature to reach a specified relative phase fraction. The former requires two times to calculate the time constant and the Avrami exponent, at two respective relative phase fractions. These can represent, for example the transformation start (for example, 1%) and finish (for example, 90%) times, at each temperature. The **TTT diagram data, fixed exponent** formulation requires that you specify the Avrami exponent separately, and then use a single transformation time, such as the transformation start. The **Parameterized TTT diagram** and **Parameterized TTT diagram, fixed exponent** formulations are used to input points from a TTT diagram, and

let COMSOL Multiphysics construct a simplified TTT diagram using these points and additional curve shape parameters. The constructed TTT diagram is used internally to calculate the required parameters of the phase transformation model. In the former, two TTT curves are used. These can represent, for example, the start and finish curves of the transformation. In the latter, a single TTT curve is used to internally calculate the time constant, and the Avrami exponent is specified separately.



### The Johnson–Mehl–Avrami–Kolmogorov (JMAK) Model

---

#### THE KIRKALDY–VENUGOPALAN MODEL

This phase transformation model is suitable for diffusion-based phase transformations, such as occur in steels during quenching. You can choose between three formulations for the model — **Rate coefficient**, **TTT diagram data**, and **Parameterized TTT diagram**. The first formulation requires a rate coefficient that represents a lumped effect of temperature and chemical composition on the rate equation for the phase transformation. The **TTT diagram data** formulation requires information that can be extracted from a TTT diagram, namely the time it takes at each temperature to reach a given relative phase fraction. This information is then used internally to calculate the required parameters for the phase transformation model. The **Parameterized TTT diagram** formulation is used to input three points from a TTT diagram, and let COMSOL Multiphysics construct a simplified TTT diagram using these points and additional curve shape parameters. The constructed TTT diagram is used internally to calculate the required parameters for the phase transformation model.



### The Kirkaldy–Venugopalan Model

---

#### THE KOISTINEN–MARBURGER MODEL

This phase transformation model is suitable to model the displacive martensitic transformation in steel, on rapid cooling. You can choose between two formulations for the model — **Koistinen–Marburger coefficient** and **Martensite finish temperature**. In the first formulation, you specify the **Martensite start temperature**  $M_s$  and the **Koistinen–Marburger coefficient**  $\beta$ . The martensite start temperature defines the onset of the phase transformation, and the Koistinen–Marburger coefficient defines how rapidly the phase transformation progresses as the temperature decreases. The martensite start temperature  $M_s$  can be experimentally obtained from dilatometry

experiments. If the integrated form of the phase transformation model is used (Equation 3-22), a value for the **Koistinen-Marburger coefficient**  $\beta$  can be correlated to the temperature at which the martensitic transformation is considered complete (see, for example, Ref. 8). In the second formulation, the phase transformation is defined by the **Martensite start temperature**  $M_s$  and the **Martensite finish temperature**  $M_{90}$ . The latter is the temperature corresponding to 90% martensite formation, using the integrated form of the phase transformation model.



### The Koistinen–Marburger Model

---



For an example how to model phase transformations, see *Phase Transformations in a Round Bar*: Application Library path **Metal\_Processing\_Module/Tutorial\_Examples/phase\_transformations\_in\_a\_round\_bar**.

## THE HYPERBOLIC RATE MODEL

This phase transformation model can be used for example to model dissolution of  $\alpha$  phase in titanium, on heating. The model assumes that the rate of formation of the destination phase is inversely proportional to the phase fraction of the destination phase.

### *Calibration of Phase Transformation Models*

---

During a thermal transient, a material point may undergo varying rates of cooling and heating. During this transient, several phase transformations can be active at the same time. This suggests that it is difficult to calibrate phase transformation models individually, as they tend to affect one another. For example, in the case of austenite decomposition, it is common in practice to present the complicated nature of phase transformations as continuous cooling transformation (CCT) or time-temperature transformation (TTT) diagrams; see Figure 2-1 and Figure 2-2 for schematic examples. Both diagrams show the start temperatures for the formation of a small fraction of different phases ( $F_s$  for the start temperature of ferrite, and so on). The

fraction can be chosen arbitrarily but is often 0.1% or 1%. The difference between the two diagram types, as their names imply, is the following:

- A CCT diagram is constructed by performing experiments where a small specimen is cooled at a specified, constant, *temperature rate*.
- A TTT diagram is constructed by performing experiments where a small specimen is rapidly cooled to a temperature  $T_0$  that is subsequently kept constant.

One method to measure the actual start temperatures required to draw each diagram is to use dilatometry experiments. Metallurgical phase transformations are accompanied by a change in volume, owing to the density difference between phases. In a dilatometer, a specimen is cooled (or heated), and its length is monitored. The specimen length will change according to basic thermal expansion, but phase transformations will induce additional length changes that can be measured.

In a real quenching situation, it is clear that material points do not experience either of the two extremes represented by the CCT and TTT diagrams (constant temperature rate versus constant temperature). Nevertheless, because experimentally obtained CCT and TTT diagrams are very common in the heat treatment community, phase transformation models must in practice be calibrated using them.

It is here useful to examine one formulation of the Leblond–Devaux model:

$$\xi^d = \frac{\xi_{\text{eq}}^d - \xi^d}{\tau_{s \rightarrow d}}$$

In this equation, the phase fraction for the destination phase tends toward an equilibrium value  $\xi_{\text{eq}}^d$ , and the rate at which this occurs is characterized by the time constant  $\tau_{s \rightarrow d}$ . Note here that the equilibrium phase fraction and the time constant are in general both temperature dependent, and that temperature in turn varies with time. At constant temperature, the equation can be integrated analytically, giving

$$\xi^d = \xi_{\text{eq}}^d \left( 1 - \exp\left(-\frac{t}{\tau_{s \rightarrow d}}\right) \right)$$

The equilibrium phase fraction can be deduced from an (equilibrium) iron-carbon diagram (Ref. 1) or from dilatometry experiments at a very low temperature rate (or at constant temperature after a rapid temperature drop). If we know this equilibrium phase fraction at a given temperature  $t_1$ , we can compute the temperature dependent time constant from knowing the time it takes to reach a specific phase fraction (isothermally):



$$\tau_{s \rightarrow d} = -\frac{t_1}{\ln\left(1 - \frac{\xi^d}{\xi_{eq}^d}\right)}$$

Alternatively, if we know the time to reach, for example, 1% of the equilibrium phase fraction, that is, the *relative* phase fraction

$$X = \frac{\xi^d}{\xi_{eq}^d}$$

the time constant is obtained without knowing the equilibrium phase fraction. Thus, a TTT diagram showing curves of transformation times corresponding to relative phase fractions  $X$  can straightforwardly be used to compute the temperature dependent time constant. In this sense, a TTT diagram is easier to use for phase transformation model calibration than a CCT diagram. This method to the calibration of phase transformation models to TTT diagram data can be used also for the Johnson–Mehl–Avrami–Kolmogorov (JMAK) and Kirkaldy–Venugopalan models. It should be pointed out that given a set of phase transformation model parameters, it is straightforward to *compute* both types of diagrams and to adjust the model parameters based on comparisons of the computed diagrams and experimental information. It is sometimes necessary to iterate in this manner to find a sufficiently accurate set of model parameters.

As a final alternative to performing the calibration using TTT or CCT diagrams, you can import computed phase transformation data. This is described in [Importing Material Properties and Phase Transformation Data](#).

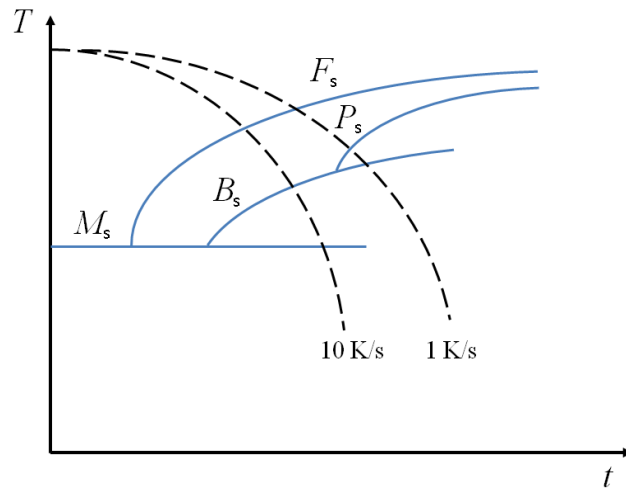


Figure 2-1: A CCT diagram showing how phases appear during cooling at two different rates. The temperatures corresponding to 1% formed fraction of ferrite, pearlite, and bainite are shown. The martensite start temperature is shown as a straight line. The time is shown on a logarithmic axis.

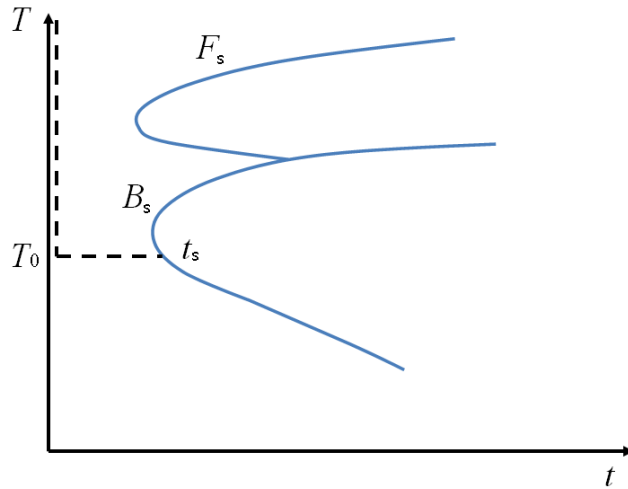


Figure 2-2: A TTT diagram showing how the temperature is rapidly decreased to a fixed value  $T_0$  and then kept constant.



For an example how to compute CCT and TTT diagrams, see *Transformation Diagram Computation*: Application Library path **Metal\_Processing\_Module/Transformation\_Diagrams/transformation\_diagram\_computation**.



For an example how to calibrate a phase transformation model based on experimental TTT diagram data, see *Transformation Diagram Computation*: Application Library path **Metal\_Processing\_Module/Transformation\_Diagrams/calibration\_against\_ttt\_data**.

# Defining Multiphysics Models

This chapter describes how to couple the phase transformation interfaces to the Heat Transfer in Solids and Solid Mechanics interfaces. A good place to start reading is in [Building a COMSOL Multiphysics Model](#) in the *COMSOL Multiphysics Reference Manual*.

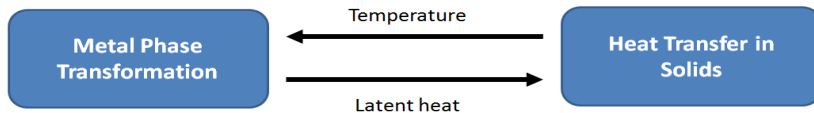
In this chapter:

- [Heat Transfer with Phase Transformations](#) — For modeling phase transformations coupled to heat transfer.
- [Steel Quenching](#) — For modeling the specific case of austenite decomposition coupled to heat transfer and solid mechanics.
- [Phase Transformation Latent Heat](#) — A predefined unidirectional coupling that adds latent heat from phase transformations as a heat source term in the coupled heat transfer interface.
- [Phase Transformation Strain](#) — A predefined bidirectional coupling that is used to transfer strains and stresses to, and from, the coupled solid mechanics interface.

## *Heat Transfer with Phase Transformations*

---

The Heat Transfer with Phase Transformations multiphysics interface combines the Metal Phase Transformation interface with the Heat Transfer in Solids interface. Phase transformations are generally temperature dependent, and this interface is a suitable starting point for modeling metallurgical phase transformations that occur during a thermal transient. Latent heat is generated during phase transformations, and the interface transfers this generated heat to the heat equation that is used by the Heat Transfer in Solids interface, as shown in [Figure 2-3](#). This is done using the [Phase Transformation Latent Heat](#) multiphysics coupling.



*Figure 2-3: The constituent interfaces of the Heat Transfer with Phase Transformations interface*

## Steel Quenching

The Steel Quenching multiphysics interface combines the Austenite Decomposition interface with the Heat Transfer in Solids and the Solid Mechanics interfaces. This is the most specialized interface of the Metal Processing Module. It can be used to study heat treatment processes by which steel parts, which have been heated to a fully austenitic state, are quenched. The multiphysics interface couples the constituent interfaces so that effects of latent heat and phase transformation strains can be included in the analysis. Phase compositions, distortions, and residual stresses can be computed using the Steel Quenching multiphysics interface. Figure 2-4 shows how this information is passed to, and from, the Austenite Decomposition interface. Note that, for example, material properties used in Solid Mechanics can be temperature dependent, and that plastic dissipation can act as a heat source in Heat Transfer in Solids (this is not shown in Figure 2-4). The Steel Quenching multiphysics interface uses the [Phase Transformation Latent Heat](#) multiphysics coupling and the [Phase Transformation Strain](#) multiphysics coupling.

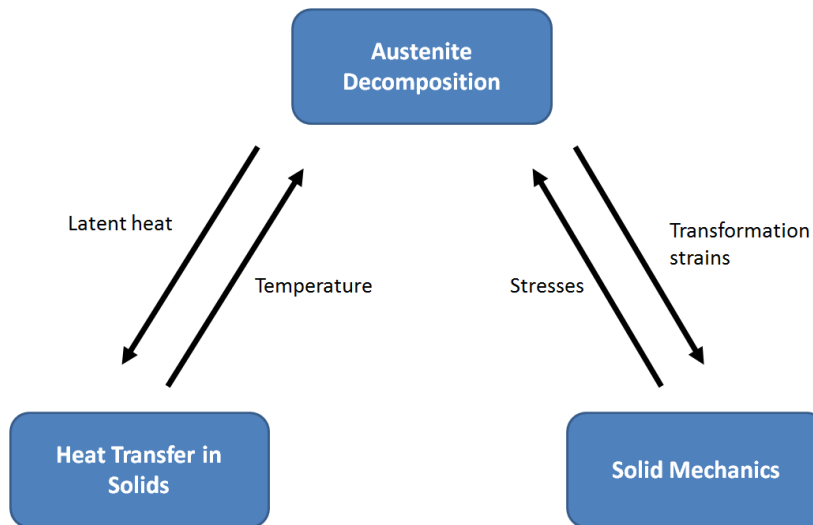


Figure 2-4: The constituent interfaces of the Steel Quenching interface.



For an example how to use the Steel Quenching interface, see *Carburization and Quenching of a Steel Gear*: Application Library path **Metal\_Processing\_Module/Steel\_Quenching/carburization\_and\_quenching\_of\_a\_steel\_gear**.

### *Phase Transformation Latent Heat*

---

This unidirectional multiphysics coupling generates a heat source term in the heat equation of the coupled Heat Transfer in Solids interface. The heat source term corresponds to the latent heat produced during phase transformations.



See [Phase Transformation Latent Heat](#) in the theory chapter.

---

### *Phase Transformation Strain*

---

This bidirectional multiphysics coupling is used to transfer strains and stresses to, and from, the coupled Solid Mechanics interface.

- If **Enable transformation-induced plasticity** is selected, the stress tensor from the Solid Mechanics interface is used to compute TRIP strains during phase transformations. These strains are used by the Solid Mechanics interface as an inelastic strain contribution.
- If **Enable thermal strains** is selected, the thermal strains are used by the Solid Mechanics interface as an inelastic contribution.



When you use this coupling, you should not use the [Thermal Expansion](#) node to compute thermal strains to be used in the Solid Mechanics interface.

---

- If **Enable phase plasticity** is selected, and if the **Plasticity** subnode under **Linear Elastic Material** is used by the coupled Solid Mechanics interface, the equivalent plastic strain is transferred to the phase transformation interface. This way, the individual hardening function for each phase can be evaluated.

# Selecting Discretizations

## *Phase Transformation Modeling*

---

The Metal Phase Transformation, Austenite Decomposition, and Alpha-Beta Phase Transformation interfaces provide discretization settings — **Discretization for phase fractions** and **Discretization for displacements**. The former sets the shape function order for the phase fractions, and it should match the settings for the temperature field used by the Heat Transfer in Solids interface. The latter sets the shape function order for strains. There are two types of strains that this setting affects:

- Phase transformation strains (that is, the thermal strains and TRIP strains)
- Equivalent plastic strains of the phases

Both of these strains are intrinsically related to strains used by a coupled Solid Mechanics interface. The **Discretization for displacements** setting should therefore match the discretization order for the displacement field used in the Solid Mechanics interface. For example, if the Solid Mechanics interface uses a quadratic shape function order for its displacement field, the **Discretization for displacements** should be set to quadratic.

Both discretization types are set to quadratic by default to match the default settings of the Heat Transfer in Solids and Solid Mechanics interfaces.

## *Carburization Modeling*

---

The discretization setting for Carburization interface controls the shape function order for the carbon concentration. The **Element order** is set to quadratic by default.

# Using Effective Material Properties

When a material undergoes phase transformations during a thermal transient, its material properties will change. The properties are typically temperature dependent and tend to be phase dependent, too. For example, the initial yield stress at a given temperature will be higher in martensite than in ferrite — two metallurgical phases that appear during hardening of steel. When the Metal Phase Transformation, Austenite Decomposition, or Alpha-Beta Phase Transformation interface is used with Heat Transfer in Solids or Solid Mechanics, it can compute effective material properties that can be utilized by these interfaces. The benefit is that the Heat Transfer in Solids and Solid Mechanics interfaces themselves do not need to perform phase averaging of the material properties that are used.

You can generate a compound material that can be used by other physics interfaces as a domain material. The compound material is created if you use the **Create Compound Material** option at the physics interface level. This material contains effective material properties that are computed from the corresponding material properties defined for each phase.



## Compound Material Properties

---



Note that if **Enable phase plasticity** has been selected at the physics interface level, the **User defined** option should be used for the **Isotropic hardening model** in the **Plasticity** node in Solid Mechanics.

---



# Importing Material Properties and Phase Transformation Data

When the Metal Phase Transformation, Austenite Decomposition, or Alpha-Beta Phase Transformation interface is used, parameters for the different phase transformations have to be defined. Additionally, if the interface is used with Heat Transfer in Solids or Solid Mechanics, the material properties of the metallurgical phases have to be defined. Phase transformations and material properties are typically temperature dependent. In the case of plasticity, the material properties also depend on plastic strain and plastic strain rate.

The effort involved in obtaining material properties and phase transformation data experimentally, or by consulting literature sources, can be time consuming and expensive. As an alternative, material properties and phase transformation data for general steels can be imported from the software JMatPro<sup>®</sup>. The following sections describe how this is done.

## *Material Properties*

---

When you import material properties, one material is created for each of the metallurgical phases austenite, ferrite, pearlite, bainite and martensite. These materials can then be used as **Phase Material** in the **Metallurgical Phase** nodes in the Metal Phase Transformation, Austenite Decomposition, and Alpha-Beta Phase Transformation interfaces. The import can be performed under **Global Definitions**.

### **LOCATION IN USER INTERFACE**

#### *Context Menu*

With **Global Definitions** selected:

**Materials>Import**

## *Phase Transformation Data*

---

When you import phase transformation data, one phase transformation node is created for each of the phase transformations involved in the decomposition of austenite:

- austenite to ferrite

- austenite to pearlite
- austenite to bainite
- austenite to martensite

In addition to data that describe the phase transformation kinetics, other data is imported and added to each phase transformation node. They are:

- phase transformation latent heat
- the parameter for transformation induced plasticity (TRIP)

The import can be performed under the **Metal Phase Transformation, Austenite Decomposition**, and **Alpha-Beta Phase Transformation** interfaces, although the **Austenite Decomposition** interface is the natural interface to perform the import from.

#### **LOCATION IN USER INTERFACE**

##### *Context Menu*

With **Metal Phase Transformation** or **Austenite Decomposition** interface selected:

##### **Import Phase Transformations**

# Modeling Carburization

This section describes how to model the heat treatment process of carburization. The process typically involves placing a component in a carbon rich environment, and letting carbon diffuse into the component over time. When you use the Carburization interface, you need to specify the characteristics of the surrounding carburization environment, specify the way in which carbon can move across the component surface, and finally specify how carbon is able to diffuse internally in the component. This is described below.

## *Defining a Carburization Environment*

---

When you use the Carburization interface, you can define the carbon concentration of the environment surrounding the component to be carburized. This is done by selecting the type of **Carburizing Cycle**. You can either specify the carbon concentration directly, as a function of time, or you can use the built-in **Boost-diffuse cycle**. In the latter situation, you use a simple cycle where the carbon potential  $c_{\text{pot}}$  is at a high value for an initial time ( $t \leq t_{\text{boost}}$ ), and after this boost period, the carbon potential is lowered, and the diffuse stage begins.



See [Carbon Potential Model](#) in the theory chapter.

---

## *Modeling Carbon Diffusion*

---

The diffusion of carbon into a component is modeled using Fick's second law of diffusion. When you solve the carbon diffusion problem, you need to specify the initial carbon concentration in the component using the **Initial Values** node. You then need to define the diffusion coefficient to be used in the diffusion equation. This diffusion coefficient can either be specified as an expression, or specified using a provided thermally activated (Arrhenius type) form.



See [Carburization](#) in the theory chapter.

---

## *Boundary Conditions*

---

You can model the exchange of carbon with the surrounding environment in different ways. You can apply two types boundary conditions to model the carbon mass transfer. They are of Dirichlet (prescribed carbon concentration) or of Neumann (prescribed carbon flux) types. In the case of a prescribed carbon flux, you have the option of using a thermally activated (Arrhenius type) description for the carbon mass transfer coefficient. By default, the external surfaces of a component have zero flux, which means that they do not transfer any carbon from or to the surrounding environment. The zero flux boundary conditions are replaced by the boundary conditions discussed previously. In a situation where you model selective carburization, you may want to leave parts of the external component surface with a zero carbon flux condition, as this would correspond to partially masking the surface from the surrounding environment.



See [Boundary Conditions](#) in the theory chapter.

---

# References

1. T. Holm, P. Olsson, and E. Troell (Eds.), “Steel and its heat treatment — A handbook”, *Sverea IVE*, Mölndal, 2012.



# Metal Processing Theory

This chapter introduces you to the theory for the Metal Processing Module.

In this chapter:

- Metallurgical Phase Transformations
- Phase Transformation Strains
- Phase Transformation Latent Heat
- Compound Material Properties
- Carburization

# Metal Phase Transformation Theory

In the following, the theory for the Metal Phase Transformation physics interface is described. This section also covers the theory for the Austenite Decomposition physics interface. These physics interfaces can be used to model metallurgical phase transformations in metals. They can be coupled to Heat Transfer in Solids and Solid Mechanics, where, for example, quenching of steel components can be performed.



# Metallurgical Phase Transformations

## *Definitions*

---

The material consists of a number of metallurgical phases. The fraction of each phase  $i$  is denoted  $\xi^i$ . There are in general  $N$  phases, where

$$\sum_{i=1}^N \xi^i = 1$$

The initial phase fraction must be defined for each phase, and the sum of initial phase fractions should be one. At the onset of an analysis, some phases may not be present, and have zero initial phase fraction.



- The phase fractions are defined in the material frame.
  - Because of the employed weighting scheme for the effective mass density of the compound material, the phase fractions become algebraic fractions.
  - See [Compound Material Properties](#).
- 

Each phase transformation describes how a source phase  $s$  transforms into a destination phase  $d$ . A phase transformation is formally defined by the rate  $A_{s \rightarrow d}$  at which the destination phase  $d$  forms at the expense of the source phase  $s$ . This can be expressed as

$$A_{s \rightarrow d} = \dot{\xi}^d = -\dot{\xi}^s \quad (3-1)$$

Note that this equation describes only a single contribution to the total rates at which the destination phase forms, and the source phase decomposes. With several simultaneous phase transformations, some phases may receive more than one contribution. As an example, consider the case of three phases and two phase transformations, where phase 1 transforms into phases 2 and 3. Using the terminology above, the total rate equations for the three phases can be expressed as

$$\dot{\xi}^1 = -A_{1 \rightarrow 2} - A_{1 \rightarrow 3}$$

$$\dot{\xi}^2 = A_{1 \rightarrow 2}$$

$$\dot{\xi}^3 = A_{1 \rightarrow 3}$$

Note that these rate equations satisfy

$$\sum_{i=1}^N \dot{\xi}^i = 0$$

In COMSOL Multiphysics, a weak contribution is generated for each phase  $i$ :

$$\left( \dot{\xi}^i - \sum_j A_{j \rightarrow i} \right) \delta \xi^i$$

where the summation is done over every phase transformation for which phase  $j$  transforms into phase  $i$ .

In some situations, you may want to lump several phase transformations into one, so that several source phases decompose using the same phase transformation kinetics. One example is a simplified description of austenitization, if you are not concerned with the exact order in which phases like martensite and pearlite transform into austenite. Here, the destination phase is taken to form according to

$$\dot{\xi}^d = A_{s \rightarrow d}$$

The negative of this rate is taken to be the sum of the rates of the (now several) source phases so that

$$-A_{s \rightarrow d} = \sum_j \dot{\xi}^j$$

where the summation is taken over the participating source phases. The contribution of each source phase to the total rate is arbitrary, and a modeling decision has to be made with regard to this indeterminacy. In COMSOL Multiphysics, the use of multiple source phases in a phase transformation is handled by assuming that each source phase rate is proportional to  $-A_{s \rightarrow d}$  through its own current phase fraction divided by the phase fraction sum of all participating source phases. For each source phase, the rate contribution is therefore

$$\xi^s = -\xi^s \frac{A_{s \rightarrow d}}{\sum_i \xi^i} \quad (3-2)$$

By using Equation 3-2, the correct sum of the source phase rates is ensured, and the indeterminacy of their respective contributions is eliminated. Moreover, Equation 3-2 reduces to the standard form given by Equation 3-1 in the case of a single source phase.

### *Phase Transformation Models*

---

In this section, the different types of phase transformations are described.

#### **THE LEBLOND–DEVAUX MODEL**

This phase transformation model is based on the work of Leblond and Devaux (Ref. 1). The model primarily considers carbon-diffusion-based phase transformations that occur in steels during heat treatment. Such transformations include austenite to ferrite, and austenite to bainite. There are four formulations for the Leblond–Devaux model:

- General coefficients
- Time and equilibrium
- TTT diagram data
- Parameterized TTT diagram

#### *General coefficients*

Using this form, the transformation of a source phase into a destination phase is given by

$$\xi^d = K_{s \rightarrow d} \xi^s - L_{s \rightarrow d} \xi^d \quad (3-3)$$

where the phase transformation is active only when  $\xi^d > 0$ ; that is, when the right-hand side of Equation 3-3 is strictly positive. In general, the functions  $K_{s \rightarrow d}$  and  $L_{s \rightarrow d}$  are functions of temperature  $T$ . It was shown in Ref. 1 that the bainitic transformation additionally depends on the rate of cooling,  $\dot{T}$ . In this case, the functions  $K_{s \rightarrow d}$  and  $L_{s \rightarrow d}$  are functions of both  $T$  and  $\dot{T}$ .

### Time and Equilibrium

This form is a special case of the general-coefficients form. The phase transformation is defined by an equilibrium phase fraction for the destination phase  $\xi_{\text{eq}}^{\text{d}}$  and a time constant  $\tau_{\text{s} \rightarrow \text{d}}$ . The phase transformation is given by

$$\xi^{\text{d}} = \frac{\xi_{\text{eq}}^{\text{d}} - \xi^{\text{d}}}{\tau_{\text{s} \rightarrow \text{d}}} \quad (3-4)$$

where the phase transformation is active only when  $\xi^{\text{d}} > 0$ ; that is, when the right side of Equation 3-4 is strictly positive. The equilibrium phase fraction  $\xi_{\text{eq}}^{\text{d}}$  and the time constant  $\tau_{\text{s} \rightarrow \text{d}}$  are typically functions of temperature.

### TTT Diagram Data

At constant temperature, the time-temperature formulation of the Leblond-Devaux phase transformation model can be integrated analytically:

$$\xi^{\text{d}} = \xi_0^{\text{d}} + (\xi_{\text{eq}}^{\text{d}} - \xi_0^{\text{d}}) \left( 1 - \exp\left(-\frac{t}{\tau_{\text{s} \rightarrow \text{d}}}\right) \right) \quad (3-5)$$

where  $\xi_0^{\text{d}}$  is the initial phase fraction. This enables straightforward calibration of the model parameters from TTT diagram data. At a given temperature, and assuming that the initial phase fraction is zero, the equilibrium phase fraction of the destination phase is  $\xi_{\text{eq}}^{\text{d}}$ . A relative phase fraction of the destination phase is defined such that it is 1.0 as the equilibrium phase fraction is reached. The relative phase fraction  $X$  is given by

$$X = \frac{\xi^{\text{d}}}{\xi_{\text{eq}}^{\text{d}}} \quad (3-6)$$

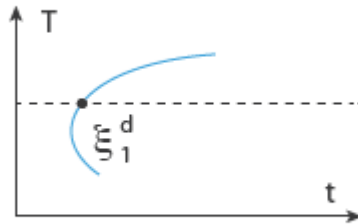
In the TTT diagram in Figure 3-1, a curve representing a fixed destination phase fraction  $\xi_1^{\text{d}}$  is shown. At a fixed temperature  $T$ , this destination phase fraction is reached at time  $t_1$ , so that

$$\xi_1^{\text{d}} = \xi^{\text{d}}(t_1) \quad (3-7)$$

The characteristic time is then expressed as

$$\tau_{\text{s} \rightarrow \text{d}} = -\frac{t_1}{\ln(1 - X_1)} \quad (3-8)$$

where  $t_1$  will vary with temperature, and the relative phase fraction  $X_1$  is understood to be the relative phase fraction corresponding to  $\xi_1^{\text{d}}$ .



*Figure 3-1: Constant phase fraction curve in a TTT diagram*

This way of fitting the Leblond-Devaux model to TTT diagram data will be most accurate near the chosen phase fraction curve in the TTT diagram. If, for example, the 0.1% curve is used, the phase transformation model will likely predict the onset of destination phase formation well, but it will show poorer agreement with the TTT diagram near completion.

#### *Parameterized TTT Diagram*

The Leblond-Devaux model can use a parameterized TTT diagram as input, in which a single TTT curve is used to identify the time constant. See [Parameterized TTT Diagram](#).

### **THE JOHNSON-MEHL-AVRAMI-KOLMOGOROV (JMAK) MODEL**

This phase transformation model is based on the work by Leblond and others ([Ref. 3](#)).

There are five formulations for the JMAK model:

- Time, equilibrium, and exponent
- TTT diagram data
- TTT diagram data, fixed exponent
- Parameterized TTT diagram
- Parameterized TTT diagram, fixed exponent

### Time, Equilibrium, and Exponent

The first formulation can be viewed as a generalization of the time-temperature formulation for the Leblond–Devaux model. It is based on an Avrami law of the form

$$\xi^d = \xi_0^d + (\xi_{eq}^d - \xi_0^d) \left( 1 - \exp \left( - \left( \frac{t}{\tau_{s \rightarrow d}} \right)^{n_{s \rightarrow d}} \right) \right) \quad (3-9)$$

In the equation above, the initial phase fraction is  $\xi_0^d$ , and the equilibrium phase fraction  $\xi_{eq}^d$ , the time constant  $\tau_{s \rightarrow d}$  and the Avrami exponent  $n_{s \rightarrow d}$  are typically functions of temperature. On rate form, Equation 3-9 can be expressed as

$$\dot{\xi}^d = \frac{\xi_{eq}^d - \xi^d}{\tau_{s \rightarrow d}} n_{s \rightarrow d} \left( \ln \left( \frac{\xi_{eq}^d - \xi_0^d}{\xi_{eq}^d - \xi^d} \right) \right)^{1 - \frac{1}{n_{s \rightarrow d}}} \quad (3-10)$$

where the explicit time dependence has been eliminated. The phase transformation is active only when  $\dot{\xi}^d > 0$ ; that is, when the right side of Equation 3-10 is strictly positive. For the special case of  $n_{s \rightarrow d} = 1$ , the equation reduces to the time-and-equilibrium form of the Leblond–Devaux model (Equation 3-4). The JMAK phase transformation model in Equation 3-10 has a mathematical disadvantage in that an initial destination phase fraction equal to zero will yield a trivial zero solution, as the logarithm will evaluate to zero. There are different ways to circumvent this problem. One way is to require the initial phase fraction be assigned a small, but finite, value. Another way is to modify the rate equation itself, so that a zero initial phase fraction does not yield a trivial zero solution. In the phase transformation interfaces, the JMAK phase transformation model in Equation 3-10 is modified for phase fractions  $\xi^d$  in the vicinity of  $\xi_0^d$ . Below a certain threshold, the argument for the logarithm is modified so that the logarithm does not produce a zero value. This threshold phase fraction is set to  $10^{-5}$  by default. A problem can arise in the case of non-zero initial phase fractions. Namely, if other phase transformations in the model operate such that the metallurgical phase that is the destination phase fraction above *decreases*, the JMAK model would run into problems as  $\xi^d < \xi_0^d$ , whereby the argument in the logarithm becomes negative. One way to handle this is to exclude the effect of the initial phase fraction in the rate expression in Equation 3-10. This is done

in COMSOL Multiphysics. A judgment has to be made in each situation whether this is a proper modeling assumption.



The phase fraction threshold variable used by the JMAK phase transformation model can be modified in the **Equation View** of the **Phase Transformation** node. Typically, the default value of  $10^{-5}$  should not have to be changed.



Note that the Avrami exponent used by the JMAK phase transformation model should be greater than or equal to one. If a smaller value is encountered, it will be replaced by an exponent of one.

#### *TTT Diagram Data*

As in the case of the Leblond–Devaux model, the JMAK model can be calibrated using TTT diagram data. The integrated form in Equation 3-9 is used to calibrate the time constant  $\tau_{s \rightarrow d}$  and the Avrami exponent  $n_{s \rightarrow d}$ . To calibrate these two phase transformation model parameters, two curves are needed from a TTT diagram; see Figure 3-2. As for the Leblond-Devaux model, a zero initial phase fraction is assumed when calibrating the JMAK model. At a fixed temperature  $T$ , the two destination phase fractions are reached at times  $t_1$  and  $t_2$ , respectively, so that

$$\xi_1^d = \xi^d(t_1) \quad (3-11)$$

$$\xi_2^d = \xi^d(t_2) \quad (3-12)$$

After some algebra, the time constant and Avrami exponent can be expressed as

$$n_{s \rightarrow d} = \ln\left(\frac{\ln(1-X_1)}{\ln(1-X_2)}\right) / \ln\left(\frac{t_1}{t_2}\right) \quad (3-13)$$

$$\tau_{s \rightarrow d} = t_1 / (-\ln(1-X_1))^{\frac{1}{n_{s \rightarrow d}}} \quad (3-14)$$

where the relative phase fractions  $X_1$  and  $X_2$  are understood to be the relative phase fractions corresponding to  $\xi_1^d$  and  $\xi_2^d$ , respectively. The transformation times  $t_1$  and  $t_2$  will vary with temperature.

### Parameterized TTT Diagram

The JMAK model can use a parameterized TTT diagram as input, in which two TTT curves are used to identify the time constant and the Avrami exponent. See [Parameterized TTT Diagram](#).

### Parameterized TTT Diagram, Fixed Exponent

The JMAK model can use a parameterized TTT diagram as input, in which a single TTT curve is used to identify the time constant. Using this formulation, you specify the Avrami exponent separately. See [Parameterized TTT Diagram](#).

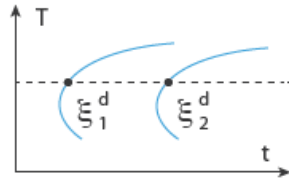


Figure 3-2: Constant phase fraction curves in a TTT diagram

### THE KIRKALDY–VENUGOPALAN MODEL

This phase transformation model is based on the work by Kirkaldy and Venugopalan (Ref. 10), and extended and modified by several others. There are two formulations for the Kirkaldy–Venugopalan phase transformation model:

- Rate coefficient
- TTT diagram data
- Parameterized TTT diagram

### Rate Coefficient

The rate form describing the phase transformation model is given by

$$\dot{\xi}^d = \xi_{eq}^d \dot{\xi}_0^d \frac{\frac{2(1-X)}{3} (1-X)^{\frac{2X}{3}}}{\exp(C_r X^2)} \quad (3-15)$$



where  $\xi_{\text{eq}}^{\text{d}}$  is the equilibrium phase fraction;  $\xi_0^{\text{d}}$  is a reference rate that in principle depends on temperature, chemical composition, and grain size; and  $C_{\text{r}}$  is a retardation coefficient. The relative phase fraction  $X$  is defined as

$$X = \frac{\xi^{\text{d}}}{\xi_{\text{eq}}^{\text{d}}} \quad (3-16)$$

so that the rate of formation of the destination phase approaches zero as the relative phase fraction approaches one; that is, when the phase transformation nears completion. The Kirkaldy–Venugopalan phase transformation model shares the mathematical disadvantage with the JMAK model in that an initial destination phase fraction of zero will yield a trivial zero solution. Similar to the JMAK phase transformation model, the Kirkaldy–Venugopalan phase transformation model is modified. A small threshold value for the destination phase fraction  $\xi^{\text{d}}$  is introduced, so that the phase transformation model produces a non-zero rate below this value.



The phase fraction threshold variable used by the Kirkaldy–Venugopalan phase transformation model can be modified in the **Equation View** of the **Phase Transformation** node. Typically, the default value of  $10^{-5}$  should not have to be changed.

---

#### TTT Diagram Data

The Kirkaldy–Venugopalan phase transformation model can be calibrated using TTT diagram data. Similar to the cases of the Leblond-Devaux and JMAK phase transformation models, the expression for the rate of destination phase formation is used to identify the model parameters, here the rate coefficient  $\xi_0^{\text{d}}$ . If we re-arrange the rate expression in Equation 3-15, we get an expression of the form

$$\dot{X} = \xi_0^{\text{d}} f(X) \quad (3-17)$$

where the relative phase fraction  $X$  has been used. Note that at a fixed temperature, the equilibrium phase fraction  $\xi_{\text{eq}}^{\text{d}}$  is constant, and it can therefore be included in the rate term  $\dot{X}$  in Equation 3-17. The reference rate  $\xi_0^{\text{d}}$  is temperature dependent (and dependent on chemical composition and grain size, in the original Kirkaldy–Venugopalan formulation). At a fixed temperature,  $t_1$  is the time to reach the destination phase fraction  $\xi_1^{\text{d}}$  (or alternatively, to reach the relative phase fraction  $X_1$ ), see Figure 3-3. This is expressed as

$$\xi_1^d = \xi^d(t_1) \quad (3-18)$$

$$X_1 = \frac{\xi_1^d}{\xi_{eq}^d} \quad (3-19)$$

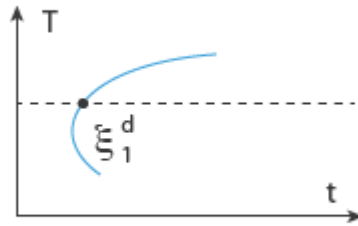


Figure 3-3: Constant phase fraction curve in a TTT diagram

Using Equation 3-17, the rate coefficient is expressed as

$$\xi_0^d = \frac{1}{t_1} \int_0^{X_1} \frac{dg}{f(g)} = \frac{1}{t_1} \int_0^{X_1} \frac{\exp(C_r g^2)}{\frac{2(1-g)^2}{3} (1-g)^3} dg \quad (3-20)$$

Note that if the retardation coefficient  $C_r$  is known, the integral can be computed *a priori* for a fixed  $X_1$ . The rate coefficient is therefore inversely proportional to the time it takes to reach the relative phase fraction  $X_1$ . The time  $t_1$  generally depends on temperature.

#### Parameterized TTT Diagram

The Kirkaldy-Venugopalan model can use a parameterized TTT diagram as input, in which a single TTT curve is used to identify the rate coefficient. See [Parameterized TTT Diagram](#).

### THE KOISTINEN–MARBURGER MODEL

This phase transformation model was developed by Koistinen and Marburger (Ref. 2) to model the diffusionless (displacive) austenite-martensite transformation in iron-carbon alloys and carbon steels. The onset of the transformation, which only occurs on cooling, is characterized by a critical start temperature — the martensite start temperature  $M_s$ . Above this temperature, no transformation from austenite (the source phase) to martensite (the destination phase) occurs. Below  $M_s$ , the amount of formed martensite is proportional to the undercooling below  $M_s$ , given by  $M_s - T$ . On rate form, the Koistinen–Marburger equation can be written

$$\dot{\xi}^d = -\xi^s \beta \dot{T} \quad (3-21)$$

where  $\beta$  is the Koistinen–Marburger coefficient. Note that the transformation of austenite into martensite only occurs below  $M_s$  and only during cooling (that is, when  $\dot{T} < 0$ ). To make the onset of martensitic transformation numerically smooth, a parameter  $\Delta M_s$  is used. The smoothing parameter defines a smoothed Heaviside function that makes the onset of martensitic transformation gradual. The parameter should be chosen small enough that the start temperature characteristic is retained. Assuming a constant cooling rate and that the phase fraction of austenite at  $M_s$  is  $\xi_0^s$ , the rate equation can be integrated to

$$\xi^d = \xi_0^s (1 - \exp(-\beta(M_s - T))) \quad (3-22)$$

This integrated form is commonly found in the literature. Instead of defining the Koistinen-Marburger coefficient directly, a martensite finish temperature,  $M_{90}$ , can be defined, corresponding to reaching a phase fraction of 90% using Equation 3-22, and assuming 100% initial source phase fraction. The Koistinen-Marburger coefficient  $\beta$  is then given by

$$\beta = -\frac{\ln 0.1}{M_s - M_{90}}$$

The rate form of Equation 3-21 is more general, and from a computational standpoint it is more suitable for implementation. The rate form is therefore used in the phase transformation interfaces.

### USER DEFINED

Using this option, other types of phase transformations can be defined. A user-defined phase transformation assumes that a source phase decomposes into a destination phase according to Equation 3-1.

### Parameterized TTT Diagram

A curve in a TTT diagram represents the time it takes to form a certain relative phase fraction of a metallurgical phase, under isothermal conditions. Using experimental TTT diagram data, one can extract transformations times across a range of temperatures and thereby characterize temperature dependent phase transformations. This is what you typically need to do for the TTT Diagram Data formulations of the Leblond-Devaux, the JMAK, and the Kirkaldy-Venugopalan phase transformation models. In some situations, it may be sufficient to approximate the shape of a TTT curve using analytical functions. COMSOL Multiphysics provides a functionality to enter three characteristic time-temperature points on a TTT curve, and together with two shape parameters, construct an approximate a TTT curve. The three points that are used to define the TTT curve in this way are:

- A point on the upper part of the curve
- A point on the lower part of the curve
- The point defining the “nose” of the curve

The points are designated U (upper), L (lower), and N (nose), see [Figure 3-4](#).

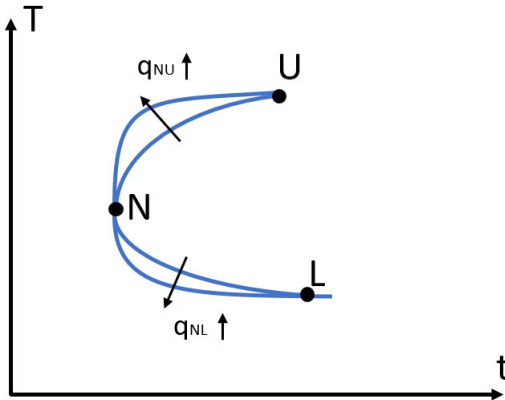


Figure 3-4: A parameterized TTT curve.

The parameterized TTT curve is defined by two analytical functions that meet at the nose. They are:

$$\log\left(\frac{t}{t_N}\right) = \log\left(\frac{t_L}{t_N}\right) \left(\frac{T - T_N}{T_L - T_N}\right)^{q_{NL}}, \quad T < T_N$$

$$\log\left(\frac{t}{t_N}\right) = \log\left(\frac{t_U}{t_N}\right) \left(\frac{T - T_N}{T_U - T_N}\right)^{q_{NU}}, \quad T \geq T_N$$

The shape parameters  $q_{NL}$  and  $q_{NU}$  are used to control the shape of the curve below the nose (NL) and above the nose (NU), and the effect of increasing them is schematically shown in [Figure 3-4](#). A shape parameter value of two produces a quadratic function in the log time - temperature space, and so on. When you parameterize the curves in a TTT diagram in this way, COMSOL Multiphysics will internally use the TTT curves in the same way as if you had used the TTT Diagram Data formulations.

# Compound Material Properties

The material consists of a mixture of metallurgical phases, each with a phase fraction that is evolving during the analysis. When the Metal Processing Module is used together with the Heat Transfer in Solids and Solid Mechanics interfaces, it is of interest to compute effective material properties so that a compound material can be defined and used by these physics interfaces. This chapter describes how various thermal and mechanical properties are averaged in terms of the phase fractions of the material.

## *Heat Transfer Properties*

---

The thermal conductivity and mass density of the compound material are computed using linear weighting by the phase fractions. The properties are given by

$$k = \sum_{i=1}^N \xi^i k^i$$

$$\rho = \sum_{i=1}^N \xi^i \rho^i$$

The thermal conductivity of the compound material uses a full tensor description. The heat capacity at constant pressure is computed by using a linear weighting of the volumetric heat capacity  $\rho C_p$ , having already computed  $\rho$ :

$$C_p = \frac{1}{\rho} \sum_{i=1}^N \xi^i \rho^i C_p^i$$



If geometric nonlinearity is used,  $k$  and  $\rho C_p$  are convected to the spatial frame in the Heat Transfer in Solids physics interface.

---

## *Electromagnetic Properties*

---

The relative permeability, the electrical conductivity, and the relative permittivity for the compound material are computed using a linear weighting by the phase fractions. The properties are given by

$$\mu_r = \sum_{i=1}^N \xi^i \mu_r^i \quad (3-23)$$

$$\sigma = \sum_{i=1}^N \xi^i \sigma^i \quad (3-24)$$

$$\epsilon_r = \sum_{i=1}^N \xi^i \epsilon_r^i \quad (3-25)$$

The electromagnetic properties for the compound material use a full tensor description.

## *Mechanical Properties*

---

The mechanical properties for the compound material are generally computed using linear weighting by the phase fractions. The exception is in the case where phase plasticity is modeled, where other types of weighting schemes can be used for the initial yield strength of the compound material.

### **ELASTICITY**

The elastic behavior of the compound material is assumed to be isotropic and defined by a linear weighting of the Young's moduli and Poisson's ratios of the phases. This is reasonable because the elastic properties for the different phases are similar at a given temperature.

$$E = \sum_{i=1}^N \xi^i E^i$$

$$v = \sum_{i=1}^N \xi^i v^i$$

### PLASTICITY

It is not obvious what weighting scheme should be used to define an effective initial yield strength because the initial yield strengths of the phases will differ. The following weighting scheme is used:

$$\sigma_{ys0} = \sum_{i=1}^N g_i(\xi^i) \sigma_{ys0}^i$$

The simplest model for the initial yield strength of the compound material uses a linear weighting

$$g_i(\xi^i) = \xi^i$$

This scheme is reasonable when the initial yield strengths are similar. However, it is well known that the yield strength of some metallurgical phases can differ significantly. Most notably, martensite is typically an order of magnitude harder than austenite, and a linear mixture rule is unsuitable. Geijselaers (Ref. 7) developed a weighting scheme that is suitable in this situation. In this model, it is assumed that the hardest phase is considerably harder than the softest phase. Assuming that the hard phase is  $m$  and the soft phase is  $\gamma$ , the Geijselaers weighting scheme is given by

$$g_i(\xi^i) = \begin{cases} \xi^i, & i \neq m \\ f_i(\xi^i), & i = m \end{cases}$$

with

$$f_m(\xi^m) = \xi^m (C + 2(1-C)\xi^m - (1-C)(\xi^m)^2)$$

$$C = 1.383 \frac{\sigma_{ys0}^\gamma}{\sigma_{ys0}^m}$$

The hardening function for the compound material is defined using the linear weighting



$$\sigma_h = \sum_{i=1}^N \xi^i \sigma_h^i(\epsilon_{pe}^i) \quad (3-26)$$

where  $\epsilon_{pe}^i$  is the equivalent plastic strain of the phase.

### EQUIVALENT PLASTIC STRAINS

In Equation 3-26, the hardening function for each individual phase depends on equivalent plastic strain. If we denote the equivalent plastic strain of the compound material  $\epsilon_{pe}$ , we must define how the equivalent of each phase  $\epsilon_{pe}^i$  evolves with this strain. The simplest assumption is to use the evolution equation

$$\dot{\epsilon}_{pe}^i = \dot{\epsilon}_{pe}$$

which is to say that the equivalent plastic strain of phase  $i$  follows that of the compound material. If phase transformation and mechanical straining occur simultaneously, the equivalent plastic strain of the diminishing source phase of the phase transformation can be taken to follow that of the compound material, and this is the behavior in the phase transformation physics interfaces. However, for a phase which is increasing in fraction during plastic straining, this assumption is questionable. Leblond (Ref. 6) derived an evolution equation for the equivalent plastic strain, which is suitable for the forming destination phase. The evolution equations for the source and destination phases are

$$\dot{\epsilon}_{pe}^s = \dot{\epsilon}_{pe}$$

$$\dot{\epsilon}_{pe}^d = \dot{\epsilon}_{pe} - \frac{\xi^d}{\xi^d} (\dot{\epsilon}_{pe}^d - \Theta_{s \rightarrow d} \dot{\epsilon}_{pe}^s)$$

where the plasticity memory coefficient  $\Theta_{s \rightarrow d}$  was introduced to model that some plastic straining present in the source phase at the instant of transformation will be carried over to the forming destination phase. A zero plasticity memory coefficient means that no plastic straining will be remembered.

# Phase Transformation Strains

We consider two types of strains that appear during a thermal transient involving metallurgical phase transformations. These strains originate from:

- Thermal expansion
- Transformation induced plasticity (TRIP)

Other inelastic strains may also be present during a thermal transient, such as plastic strains or creep strains.

## *Thermal Expansion*

---

Thermal expansion for the compound material is given by a phase fraction weighted sum of the thermal expansion of each phase:

$$\epsilon_{\text{th}} = \sum_{i=1}^N \xi^i \epsilon_{\text{th}}^i$$

It is well known that different metallurgical phases occupy different volumes at a given temperature. For example, when austenite transforms into martensite, the thermal contraction due to cooling is accompanied by a volumetric expansion when the martensite begins to form. Consider a simple case where phase I transforms into phase II. In 1D, and using a secant definition of the thermal expansion coefficient, the thermal strain is

$$\epsilon_{\text{th}} = \xi^I \alpha^I(T)(T - T_{\text{ref}}^I) + \xi^{II} \alpha^{II}(T)(T - T_{\text{ref}}^{II})$$

where  $\alpha(T)$  and  $T_{\text{ref}}$  are the secant coefficient of thermal expansion and strain volume reference temperature, for the respective phases I and II. Figure 3-5 shows the thermal strain. For simplicity, the coefficients of thermal expansion for the two phases in the figure are constant (but different). In the figure, a fictitious phase transformation has been used to illustrate when phase I transforms completely into phase II as the temperature is lowered. No separate volumetric term is required to model this type of phase transformation strain, as it is included in the definition of the thermal expansion itself.

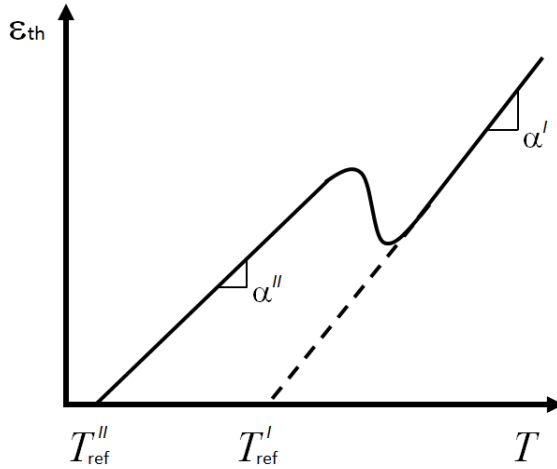


Figure 3-5: Thermal strain during phase transformation.

### Transformation-Induced Plasticity

Plastic strains in metals result from deviatoric stresses that exceed the yield strength of the material. However, during phase transformations, inelastic strains may appear already at very small stress levels. This transformation-induced plasticity (TRIP) is therefore different from classical plasticity in that it does not involve a yield criterion and that it appears at stress levels that would otherwise be insufficient to cause plastic straining even in the softest of the phases. A description of TRIP strain rate, common in the literature (see, for example, Ref. 3), is

$$\dot{\varepsilon}_{\text{tp, s} \rightarrow \text{d}} = \frac{3}{2} K_{\text{s} \rightarrow \text{d}}^{\text{TRIP}} \cdot \frac{\text{d}\Phi(\xi^{\text{d}})}{\text{d}\xi^{\text{d}}} \dot{\xi}^{\text{d}} \cdot \text{dev}(S)$$

where the strain rate is proportional to the deviatoric part of the second Piola–Kirchhoff stress tensor  $S$  through the transformation induced plasticity parameter  $K_{\text{s} \rightarrow \text{d}}^{\text{TRIP}}$ , the derivative of the saturation function  $\Phi(\xi^{\text{d}})$ , and the rate of the destination phase  $\dot{\xi}^{\text{d}}$ . Values for the transformation-induced plasticity parameter  $K_{\text{s} \rightarrow \text{d}}^{\text{TRIP}}$  will depend on the type of phase transformation. It can depend on, for example, carbon content and temperature (see Ref. 4). Several propositions exist for the saturation

functions; see [Table 3-1](#) and [Ref. 9](#). Through the user-defined option, you can define the derivative of the saturation function.

TABLE 3-1: SATURATION FUNCTIONS FOR THE TRIP STRAIN RATE

TYPE	EXPRESSION
Abrassart	$\xi^d (3 - 2\sqrt{\xi^d})$
Desalos	$\xi^d (2 - \xi^d)$
Leblond	$\xi^d (1 - \ln \xi^d)$ for $\xi^d > 0.03$ , zero otherwise
Tanaka	$\xi^d$

The total TRIP strain rate is given by

$$\dot{\epsilon}_{tp} = \sum_{s \rightarrow d} \dot{\epsilon}_{tp, s \rightarrow d}$$

### *Total Strain Contribution*

When thermal and TRIP strains are computed, they can be used in a Solid Mechanics interface as an inelastic strain contribution. The contributions from thermal and TRIP strains are added to form a total strain contribution. In the Solid Mechanics interface, this contribution is used additively in the case of an additive strain definition or used to form an inelastic-deformation-gradient contribution in the case of geometric nonlinearity with nonlinear strains; see [Inelastic Strain Contributions](#). In the latter case, the contribution is used multiplicatively.

# Phase Transformation Latent Heat

The heat rate  $Q_0$  that is released during a phase transformation is characterized by the enthalpy per unit volume  $\Delta H_{s \rightarrow d}$  (see [Ref. 4](#)). The heat rate that is associated with the transformation of a source phase into a destination phase can be expressed as

$$Q_0 = \Delta H_{s \rightarrow d} \dot{\xi}^d \quad (3-27)$$

The heat rates that result from each phase transformation are added, and they can be used as a heat source when solving the heat equation. A weak contribution is added to the weak form of the heat equation:

$$\hat{Q}_0 \delta(T)$$

where  $\hat{Q}_0$  is the sum of the contributions  $Q_0$  from each phase transformation ([Equation 3-27](#)), and  $T$  is the temperature degree of freedom used in the Heat Transfer in Solids interface.

# Carburization

Carburization is a heat treatment process where a component is placed in a carbon rich atmosphere, at an elevated temperature. During the process, carbon diffuses into the surface of the component, and the carbon concentration in the component changes with time as carbon continues to diffuse to the interior. The process of carburization is modeled using Fick's second law of diffusion. The carbon concentration  $c$  during carburization depends on position and time as  $c = c(\mathbf{X}, t)$ , where  $\mathbf{X}$  denotes material coordinates, and  $t$  is time. The carbon concentration represents the mass fraction of carbon, and it is thus dimensionless. The carbon concentration is governed by the following equation:

$$\frac{\partial c}{\partial t} + \nabla \cdot (-D\nabla c) = 0$$

where  $D$  is the diffusion coefficient, or diffusivity. The diffusivity can be specified directly, or it can be modeled using an Arrhenius expression of the form

$$D = D_0 \exp\left(-\frac{Q_D}{RT}\right)$$

where  $D_0$  is a pre-exponential factor,  $Q_D$  is an activation energy, and  $R$  is the gas constant.

## *Carbon Potential Model*

---

During carburization, the carbon rich atmosphere can be changed over time to produce a desired carbon profile near the surface of the component. In COMSOL Multiphysics, you can specify the carbon potential  $c_{\text{pot}}$  of the surrounding atmosphere as a function of time, or you can use a boost-diffuse cycle (Figure 3-6). For the Boost-diffuse cycle, the carbon potential is defined by

$$c_{\text{pot}} = \begin{cases} c_{\text{boost}} & , \quad t \leq t_{\text{boost}} \\ c_{\text{diffuse}} & , \quad t > t_{\text{boost}} \end{cases}$$

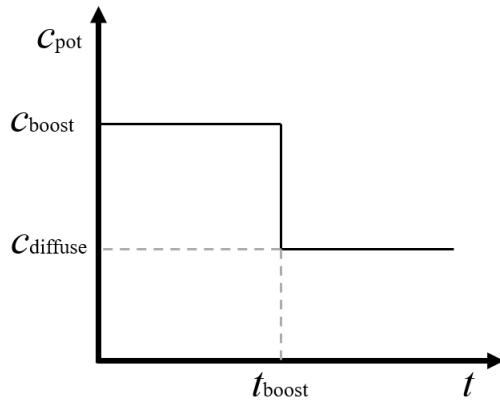


Figure 3-6: The Boost-diffuse cycle.

### Boundary Conditions

When a component is subjected to an environment of different carbon concentration, carbon can diffuse into or out from its surface. This mass transfer can be modeled in two ways:

- A prescribed carbon flux (a Neumann condition): Carbon mass transfer is modeled using a convection boundary condition
- A prescribed carbon concentration (a Dirichlet condition): Carbon mass transfer is enabled by means of a prescribed value on the surface

A special case of prescribed carbon flux is the case of zero carbon flux.

#### PRESCRIBED CARBON FLUX

The convective mass transfer of carbon from the environment into a surface with outward normal  $\mathbf{n}$  is given by

$$-\mathbf{n} \cdot (-D\nabla c) = b \cdot (c_{\text{ext}} - c)$$

where  $b$  is the mass transfer coefficient, and  $c_{\text{ext}}$  is the carbon concentration of the exterior. A natural way to define the carbon concentration of the exterior is to take it as equal to the carbon potential  $c_{\text{pot}}$  of the surrounding carburizing atmosphere. The mass transfer coefficient can be specified directly, or defined as thermally activated

$$b = b_0 \exp\left(-\frac{Q_b}{RT}\right)$$

where  $b_0$  is a pre-exponential factor and  $Q_b$  is an activation energy. In a given situation, these quantities would have to be estimated or measured experimentally.

#### **PRESCRIBED CARBON CONCENTRATION**

A simple way to model the carbon exchange is to simply prescribe the carbon concentration at the surface of the component to be equal to the carbon concentration of the exterior. This modeling approach avoids having to characterize the carbon mass transfer, but it may instead exaggerate it because the surface will be saturated.





# References

1. J.B. Leblond and J.C. Devaux, "A new kinetic model for anisothermal metallurgical phase transformations in steels including effect of austenite grain size," *Acta Metall.*, vol. 32, no. 1, pp. 137–146, 1984.
2. D.P. Koistinen and R.E. Marburger, "A general equation prescribing the extent of the austenite-martensite transformation in pure iron-carbon alloys and plain carbon steels," *Acta Metall.*, vol. 7, no. 1, pp. 59–60, 1959.
3. J.B. Leblond, G. Mottet, J. Devaux, and J.C. Devaux, "Mathematical models of anisothermal phase transformations in steels, and predicted plastic behaviour," *Mat. Sci. Tech.*, vol. 1, no. 10, pp. 815–822, 1985.
4. B. Liscic, H.M. Tensi, L.C.F. Canale, and G.E. Totten (Eds.), *Quenching theory and technology*, CRC Press, Taylor & Francis Group, 2010.
5. J.B. Leblond, J. Devaux, and J.C. Devaux, "Mathematical modelling of transformation plasticity in steels I: Case of ideal-plastic phases," *Int. J. Plast.*, vol. 5, pp. 551–572, 1989.
6. J.B. Leblond, "Mathematical modelling of transformation plasticity in steels II: Coupling with strain hardening phenomena," *Int. J. Plast.*, vol. 5, pp. 573–591, 1989.
7. H.J.M. Geijselaers, *Numerical simulation of stresses due to solid state transformations: The simulation of laser hardening*, doctoral dissertation, Univ. of Twente, Enschede, 2003.
8. J. Gyhlestén Back, *Modelling and characterisation of the martensite formation in low-alloyed carbon steels*, licentiate thesis, Luleå Univ. of Technology, Luleå, 2017.
9. S. Boettcher, M. Böhm, and M. Wolff, *A comprehensive model of thermo-elasto-plasticity with phase transitions in steel*, Zentrum für Technomathematik, Universität Bremen, 2013.
10. J.S. Kirkaldy and D. Venugopalan, *Phase Transformations in Ferrous Alloys*, Am, Inst. Min. Engg., Philadelphia, Pa 1984.



# Metal Phase Transformation

This chapter describes the Metal Phase Transformation Interface () and its functionality. It is found under the **Heat Transfer>Metal Processing** branch () when adding a physics interface.

# The Metal Phase Transformation Interface



The **Metal Phase Transformation** interface () is found under the **Heat Transfer>Metal Processing** () branch when adding a physics interface. The physics interface is intended for studying metallurgical phase transformations. You can use this interface to study diffusional, displacive, and user-defined (solid state) phase transformations. Physical phenomena, such as latent heat of phase transformation and transformation strains, can be computed and used in Heat Transfer in Solids and Solid Mechanics. With the Nonlinear Structural Materials Module or the Geomechanics Module, plastic strains and hardening behavior of each metallurgical phase can be used in Solid Mechanics. Different sections of the **Settings** panel will be active depending on the space dimension that the interface is used in, see [Table 4-1](#).

TABLE 4-1: PHYSICS INTERFACE SECTIONS.

SECTION	AVAILABILITY
Material Properties	1D, 1D axisymmetric, 2D, 2D axisymmetric, 3D
Heat Transfer	1D, 1D axisymmetric, 2D, 2D axisymmetric, 3D
Temperature	0D
Solid Mechanics	1D, 1D axisymmetric, 2D, 2D axisymmetric, 3D
Discretization	1D, 1D axisymmetric, 2D, 2D axisymmetric, 3D

When the Metal Phase Transformation interface is added, three nodes are also added to the **Model Builder** — two **Metallurgical Phase** nodes and one **Phase Transformation** node. The phase transformation node will be set to use the two metallurgical phases as source and destination phases, respectively. From the **Physics** toolbar, you can add additional metallurgical phases and phase transformations. You can also right-click **Metal Phase Transformation** to select physics features from the context menu.

## SETTINGS

The **Label** is the default physics interface name.

The **Name** is used primarily as a scope prefix for variables defined by the physics interface. Refer to such physics interface variables in expressions using the pattern `<name>.<variable_name>`. In order to distinguish between variables belonging to different physics interfaces, the `name` string must be unique. Only letters, numbers, and underscores (`_`) are permitted in the **Name** field. The first character must be a letter.

The default **Name** (for the first physics interface in the model) is `metp`.

### MATERIAL PROPERTIES

You have the option of letting the physics interface compute effective thermal, electromagnetic, and mechanical material properties, based on the corresponding properties and fractions of the individual metallurgical phases. Select the **Compute effective thermal properties** check box to let the physics interface compute effective thermal properties. Select the **Compute effective electromagnetic properties** check box to let the physics interface compute effective electromagnetic properties. Select the **Compute effective mechanical properties** check box to let the physics interface compute effective mechanical properties. You can use the computed effective material properties to create a compound material that can be used in other physics interfaces as a domain material. Select the **Create Compound Material** to create a compound material. This material is created at the component level.



A compound material that is generated from an Austenite Decomposition interface (`audc`) will be given the tag `audcmat`.

---

### HEAT TRANSFER

Phase transformations are inherently temperature dependent. Select the temperature field to use from the **Temperature** list. If you want to consider the release or absorption of latent heat during phase transformations, select the **Enable phase transformation latent heat** check box. You can then define values for the latent heat at each of the phase transformation nodes. By default, the check box is not selected.

### TEMPERATURE

Phase transformations are inherently temperature dependent. Enter an expression for the temperature to use.



The two sections Heat Transfer and Temperature are mutually exclusive, and which one is active is determined by the space dimension.

---

### SOLID MECHANICS

This section contains settings that affect various strains that accompany phase transformations. Select the **Enable transformation-induced plasticity** check box if you want to include this type of transformation strain in your analysis. The **Enable thermal strains** and **Enable phase plasticity** check boxes are visible only if you have selected the

**Compute effective mechanical properties** check box in the **Material Properties** section. Select **Enable thermal strains** if you want to include thermal strains in your analysis. Note that the thermal strains will include both pure thermal strains as well as strains that arise from volumetric differences between different metallurgical phases. Select the **Enable phase plasticity** check box if you want to allow for plasticity in the individual phases. By default, none of the three check boxes in this section are selected.

#### DISCRETIZATION

The discretizations for phase fractions and displacements can be set independently using the **Discretization for phase fractions** and **Discretization for displacements** lists. In general, the **Discretization for displacements** setting should match the discretization order used for the displacement field in the Solid Mechanics interface. By default, **Linear** is selected for phase fractions and **Quadratic** for displacements.



Note that when you set the **Discretization for phase fractions** to Gauss point data, spatial gradients of the phase fractions will not be available. This can be relevant in other physics interfaces, should the gradients of phase fractions be required.

### *Metallurgical Phase*

The **Metallurgical Phase** node defines a phase. Depending on the settings at the physics interface level and the space dimension where the physics interface is used, the phase node will contain different sections, see [Table 4-2](#).

TABLE 4-2: METALLURGICAL PHASE SECTIONS.

SECTION	AVAILABILITY
Model Input	1D, 1D axisymmetric, 2D, 2D axisymmetric, 3D
Initial Phase Fraction	0D, 1D, 1D axisymmetric, 2D, 2D axisymmetric, 3D
Transformation Times	0D
Phase Material	1D, 1D axisymmetric, 2D, 2D axisymmetric, 3D
Heat Transfer Properties	1D, 1D axisymmetric, 2D, 2D axisymmetric, 3D
Electromagnetic Properties	2D, 2D axisymmetric, 3D
Mechanical Properties	1D, 1D axisymmetric, 2D, 2D axisymmetric, 3D

## MODEL INPUT

Provide the **Volume reference temperature**  $T_{\text{ref}}$  for the phase. This is the temperature at which the thermal strain is zero for the phase.

## INITIAL PHASE FRACTION

Define the **Initial phase fraction** for the phase. This fraction should be a value between zero and one, and you have to ensure that the initial phase fractions for all the phases in your analysis sum to one.



- The initial fractions for the metallurgical phases are named `metp.phase1.xi0`, `metp.phase2.xi0`, and so on.
- The current phase fractions are correspondingly named `metp.phase1.xi` and `metp.phase2.xi`.

## TRANSFORMATION TIMES

If you select **Compute transformation times**, you can store the times  $\hat{t}$  and temperatures  $T$  during an analysis, corresponding to reaching specified target phase fractions. Enter a list of **Target phase fractions**  $\hat{\xi}$  in the table. Whether transformation times and temperatures are recorded depends on if the phase fraction is increasing or decreasing during the analysis. Select **Decreasing phase fraction** if the phase fraction is expected to reach the specified target values when it is decreasing. With **Compute transformation times** selected, and in the case a phase fraction is increasing over time, you can select **Compute time to completion**. Enter the **Completion rate**, that is, a rate of phase formation low enough that the formation of the phase can be considered complete.



If the second Target phase fraction in the table is reached for a Metallurgical Phase (`phase4`) in an Austenite Decomposition interface (`audc`), the corresponding transformation time and temperature will be `audc.phase4.time_2` and `audc.phase4.temperature_2`.

## PHASE MATERIAL

From the **Phase material** list, you select the material that defines the material properties for the phase. This section is visible only if at least one of the **Compute effective thermal properties** or the **Compute effective mechanical properties** check boxes has been selected at the physics interface level. You can create a material at the component level by using

**Create Phase Material.** When you define material properties for the phase, **From material** will refer to the material that you have selected from the **Phase material** list.



A phase material that is generated from a Metallurgical Phase (phase2) in an Austenite Decomposition interface (audc) will be given the tag audcphase2mat.

#### HEAT TRANSFER PROPERTIES

If the **Compute effective thermal properties** has been selected at the physics interface level, you must define the thermal properties for the phase. The default **Thermal conductivity**  $k$ , **Density**  $\rho$ , and **Heat Capacity at constant pressure**  $C_p$ , use values **From material**. The **From material** option refers to the selected material from the **Phase Material** list. For **User defined**, enter values or expressions for these properties.

#### ELECTROMAGNETIC PROPERTIES

If the **Compute effective electromagnetic properties** has been selected at the physics interface level, you must define electromagnetic properties for the phase. The default **Relative permeability**  $\mu_r$ , **Electrical conductivity**  $\sigma$ , and **Relative permittivity**  $\epsilon_r$ , use values **From material**. The **From material** option refers to the selected material from the **Phase Material** list. For **User defined**, enter values or expressions for these properties.

#### MECHANICAL PROPERTIES

If the **Compute effective mechanical properties** has been selected at the physics interface level, you must define mechanical properties for the phase. The default Young's modulus  $E$  and Poisson's ratio  $\nu$  use values **From material**. For **User defined**, enter values or expressions for these properties.

If **Enable thermal strains** has been selected at the physics interface level, you have to define the **Secant coefficient of thermal expansion**  $\alpha$  for the phase. By default, the value is taken **From material**. For **User defined**, enter a value or expression.

If **Enable phase plasticity** has been selected at the physics interface level, you have to define the plastic behavior of the phase. The default **Initial yield stress**  $\sigma_{ys0}$  uses a value **From material**. For **User defined**, enter another value or expression for initial yield stress. Initial yield stresses for phases can be weighted differently. This is useful when initial yield stresses for the phases in the model are very different. Select a **Weight factor for yield stress** — **Linear**, **Geijselaers**, or **User defined**. If **Geijselaers** is selected, you also need to specify a **Soft phase**, which is considered plastically soft in comparison to this phase.



You should typically use this to give a stronger weight to martensite (hard) in relation to austenite (soft).

Select the **Isotropic hardening model** — **Perfectly plastic**, **Linear**, or **User defined** to define the hardening behavior of the phase.

#### *Linear*

Specify the **Isotropic hardening modulus**  $E_{T_{iso}}$ . The default value is taken **From material**.

#### *User defined*

For **User defined**, enter another value or expression for the modulus. If a **User defined** isotropic hardening modulus is selected, you have to select the **Hardening function**. By default, the value is taken **From material**.

For **User defined**, enter a value or expression for the **hardening function**. The expression can depend, for example, on the equivalent plastic strain in the phase.



In a phase (**phase4**) of an Austenite Decomposition interface (**audc**), the equivalent plastic strain is **audc.phase4.epe**.

---

### *Phase Transformation*

---

Depending on the settings at the physics interface level and the space dimension where the physics interface is used, the phase transformation node will contain different sections.

#### **PHASE TRANSFORMATION**

The phase transformation defines how one phase forms (the destination phase) at the expense of another (the source phase). Select **Source phase**  $\xi^s$  and **Destination phase**  $\xi^d$  from the list of defined phases. Select a **Phase transformation model** — **Leblond–Devaux**, **Johnson–Mehl–Avrami–Kolmogorov**, **Kirkaldy–Venugopalan**, **Koistinen–Marburger**, **Hyperbolic rate**, or **User defined**.

#### *Leblond–Devaux*

Select a **Formulation** — **Time and equilibrium**, **General coefficients**, **TTT diagram data**, or **Parameterized TTT diagram**.

- For **Time and equilibrium**, specify the **Equilibrium phase fraction**  $\xi_{eq}^d$  and **Time constant**  $\tau_{s \rightarrow d}$ .

- For **General coefficients**, specify the expressions for  $K_{s \rightarrow d}$  and  $L_{s \rightarrow d}$ . For **TTT diagram data**, specify the **Equilibrium phase fraction**  $\xi_{eq}^d$ , the **Relative phase fraction**  $X_1$ , and the **Transformation time**  $t_1$ .
- For **Parameterized TTT diagram**, specify the **Equilibrium phase fraction**  $\xi_{eq}^d$  and the **Relative phase fraction**  $X_1$ . In the **TTT Curve 1** section, specify the transformation times  $t_L$ ,  $t_N$ , and  $t_U$  corresponding to points on the lower part, the “nose”, and the upper part of the TTT curve at the relative phase fraction  $X_1$ . Specify the corresponding transformation temperatures  $T_L$ ,  $T_N$ , and  $T_U$ , and the TTT curve shape parameters  $q_{NL}$  and  $q_{NU}$ .

If applicable, select **Define temperature limits**, and specify the **Lower temperature limit**  $T_l$  and the **Upper temperature limit**  $T_u$ .

#### *Johnson–Mehl–Avrami–Kolmogorov*

Select a **Formulation — Time, equilibrium and exponent, TTT diagram data, TTT diagram data, fixed exponent, Parameterized TTT diagram, or Parameterized TTT diagram, fixed exponent.**

- For **Time, equilibrium and exponent**, specify the **Equilibrium phase fraction**  $\xi_{eq}^d$ , the **Time constant**  $\tau_{s \rightarrow d}$ , and the **Avrami exponent**  $n_{s \rightarrow d}$ .
- For **TTT diagram data**, specify the **Equilibrium phase fraction**  $\xi_{eq}^d$ , the **Relative phase fraction**  $X_1$ , the **Transformation time**  $t_1$ , the **Relative phase fraction**  $X_2$ , and the **Transformation time**  $t_2$ .
- For **TTT diagram data, fixed exponent**, specify the **Equilibrium phase fraction**  $\xi_{eq}^d$ , the **Avrami exponent**  $n_{s \rightarrow d}$ , the **Relative phase fraction**  $X_1$ , and the **Transformation time**  $t_1$ .
- For **Parameterized TTT diagram**, specify the **Equilibrium phase fraction**  $\xi_{eq}^d$ , the **Relative phase fraction**  $X_1$ , and the **Relative phase fraction**  $X_2$ . In the **TTT Curve 1** section, specify the transformation times  $t_L$ ,  $t_N$ , and  $t_U$  corresponding to points on the lower part, the “nose”, and the upper part of the TTT curve at the **Relative phase fraction**  $X_1$ . Specify the corresponding transformation temperatures  $T_L$ ,  $T_N$ , and  $T_U$ , and the TTT curve shape parameters  $q_{NL}$  and  $q_{NU}$ . In the **TTT Curve 2** section, specify the parameters for the TTT curve at the **Relative phase fraction**  $X_2$ .
- For **Parameterized TTT diagram, fixed exponent**, specify the **Equilibrium phase fraction**  $\xi_{eq}^d$ , the **Avrami exponent**  $n_{s \rightarrow d}$ , and the **Relative phase fraction**  $X_1$ . In the **TTT Curve 1** section, specify the transformation times  $t_L$ ,  $t_N$ , and  $t_U$  corresponding to points on the lower part, the “nose”, and the upper part of the TTT curve at the **Relative phase fraction**  $X_1$ . Specify the corresponding transformation temperatures  $T_L$ ,  $T_N$ , and  $T_U$ , and the TTT curve shape parameters  $q_{NL}$  and  $q_{NU}$ .

If the rate term in the phase transformation model is to account for a non-zero initial phase fraction of the source phase, select **Include effect of initial phase fraction**. If applicable, select **Define temperature limits**, and specify the **Lower temperature limit**  $T_l$  and the **Upper temperature limit**  $T_u$ .

#### *Kirkaldy–Venugopalan*

Select a **Formulation** — **Rate coefficient**, **TTT diagram data**, or **Parameterized TTT diagram**.

- For **Rate coefficient**, specify the **Equilibrium phase fraction**  $\xi_{eq}^d$  and the **Reference rate**  $\xi_0^d$ .
- For **TTT diagram data**, specify the **Equilibrium phase fraction**  $\xi_{eq}^d$ , the **Relative phase fraction**  $X_1$ , and the **Transformation time**  $t_1$ .
- For **Parameterized TTT diagram**, specify the **Equilibrium phase fraction**  $\xi_{eq}^d$  and the **Relative phase fraction**  $X_1$ . In the **TTT Curve I** section, specify the transformation times  $t_L$ ,  $t_N$ , and  $t_U$  corresponding to points on the lower part, the “nose”, and the upper part of the TTT curve at the relative phase fraction  $X_1$ . Specify the corresponding transformation temperatures  $T_L$ ,  $T_N$ , and  $T_U$ , and the TTT curve shape parameters  $q_{NL}$  and  $q_{NU}$ .

The rate term can be modified from its original form. If applicable, select **Include retardation term**, and specify the **Retardation coefficient**  $C_r$ . If applicable, select **Define temperature limits**, and specify the **Lower temperature limit**  $T_l$  and the **Upper temperature limit**  $T_u$ .

#### *Koistinen–Marburger*

Select a **Formulation** — **Koistinen-Marburger coefficient** or **Martensite finish temperature**.

- For **Koistinen-Marburger coefficient**, specify the **Martensite start temperature**  $M_s$  and the **Koistinen-Marburger coefficient**  $\beta$ .
- For **Martensite finish temperature**, specify the **Martensite start temperature**  $M_s$  and the **Martensite finish temperature**  $M_{90}$ .

#### *Hyperbolic rate*

Specify the **Hyperbolic rate constant**  $P_{s \rightarrow d}$  and the **Equilibrium phase fraction**  $\xi_{eq}^d$ . If applicable, select **Define temperature limits**, and specify the **Lower temperature limit**  $T_l$  and the **Upper temperature limit**  $T_u$ .

#### *User defined*

Specify the **Phase transformation contribution**  $A_{s \rightarrow d}$ . The expression defines the rate at which the destination phase forms, at the expense of the source phase.

If applicable, select **Define temperature limits**, and specify the **Lower temperature limit**  $T_l$  and the **Upper temperature limit**  $T_u$ .

#### PHASE TRANSFORMATION LATENT HEAT

This section is active if you have selected **Enable phase transformation latent heat** at the physics interface level. You can specify the latent heat  $\Delta H_{s \rightarrow d}$  that is released during the phase transformation.

#### PHASE TRANSFORMATION STRAIN

The **Transformation induced plasticity** check box is available if you have selected **Enable transformation induced plasticity** at the physics interface level. In case of transformation induced plasticity, specify the **Transformation induced plasticity parameter**  $K_{s \rightarrow d}^{\text{TRIP}}$  and the **Saturation function**  $\Phi$ .

The **Plastic recovery for destination phase** check box is available if the **Enable thermal strains** has been selected at the physics interface level. If you have selected **Plastic recovery** for destination phase, you can specify the **Plastic memory coefficient**  $\Theta_{s \rightarrow d}$ . The default value is zero, which means that no plastic straining in the source phase will be carried over to the destination phase.



If you have selected **Parameterized TTT Diagram** or **Parameterized TTT Diagram, Fixed Exponent**, you can visualize the TTT curve corresponding to the entered parameters in the **TTT curve 1** or **TTT Curve 2** sections.

- Make a preview plot by selecting **TTT curve preview**.
- Generate a plot by selecting **Create TTT curve plot**.

#### ADVANCED

Numerical smoothing can be applied at temperatures that correspond to a sudden activation or deactivation of the phase transformation. If you select **Advanced Physics Options**, the **Advanced** section is used to assign smoothing:

- **Transformation temperature smoothing**,  $\Delta T$ , in case you have used **Define temperature limits**.
- **Martensite start temperature smoothing**,  $\Delta M_s$ , in the case of the **Koistinen-Marburger** phase transformation model.

The smoothing parameters  $\Delta T$  and  $\Delta M_s$  each defines a temperature span across which the phase transformation rate term is smoothly ramped. In the limit of a zero smoothing parameter value, the ramping reduces to a Heaviside step function.

## *Transformation Condition*

---

One or several **Transformation Condition** subnodes can be added to a **Phase Transformation node**. In the **Transformation Condition** subnode, specify a Boolean expression  $c$  that has to be satisfied for the **Phase Transformation** to take place. For example, if you have reason to prevent a phase transformation from occurring unless the temperature rate is negative, the expression could look like:

```
metp.Tt<0[K/s]
```

If several **Transformation Condition** subnodes are used, each separate condition has to be satisfied for the **Phase Transformation** to take place.



In some situations, a Boolean expression  $c$  may be numerically challenging. It can be beneficial to use smoothed transformation condition. For example, a general Boolean expression  $a > b$  can be replaced by a smoothed Heaviside function as

$$f_{1c1hs}(2*(a-b)/h, 1)$$

causing  $c$  to increase smoothly from zero to one, across an interval of length  $h$ , centered at  $a = b$ .

---



## *Additional Source Phase*

---



One or several **Additional Source Phase** subnodes can be added to a **Phase Transformation node**. In the **Additional Source Phase** subnode, select a metallurgical phase that contributes to the formation of the **Destination phase** defined in the **Phase Transformation node**.



# Austenite Decomposition

This chapter describes the Austenite Decomposition Interface () and its functionality. It is found under the **Heat Transfer>Metal Processing** branch () when adding a physics interface.

# The Austenite Decomposition Interface

The **Austenite Decomposition** interface () is found under the **Heat Transfer>Metal Processing** () branch when adding a physics interface. The physics interface is intended for studying metallurgical phase transformations. You can use this interface to study diffusional, displacive, and user-defined (solid-solid) phase transformations. Physical phenomena, such as latent heat of phase transformation and transformation strains can be computed and used in Heat Transfer in Solids and Solid Mechanics. With the Nonlinear Structural Materials Module or the Geomechanics Module, plastic strains and hardening behavior of each metallurgical phase can be used in Solid Mechanics.

This interface is based on the Metal Phase Transformation interface. This chapter will only describe the nodes and settings that set the Austenite Decomposition interface apart from the Metal Phase Transformation interface. With regard to other settings at the physics interface level and feature level, see [The Metal Phase Transformation Interface](#).

When the Austenite Decomposition interface is added, nine nodes are added to the **Model Builder** — five [Metallurgical Phase](#) nodes and four [Phase Transformation](#) nodes. The interface is tailored specifically to the decomposition of austenite into a combination of ferrite, pearlite, bainite, and martensite. The phase nodes are given names to reflect this:

- Austenite
- Ferrite
- Pearlite
- Bainite
- Martensite

The **Initial Phase Fraction** is set to one in the **Austenite** node, and zero in the other metallurgical phase nodes. Four **Phase Transformation** nodes are also created to define the relevant phase transformations:

- Austenite to Ferrite
- Austenite to Pearlite



- Austenite to Bainite
- Austenite to Martensite

The source and destination phases in each phase transformation are set to the corresponding phases that have been created. The **Phase transformation model** is set to **Leblond–Devaux** with **General coefficients**, except in **Austenite to Martensite**, where it is set to **Koistinen–Marburger**.



A **Parameters** node is automatically created under **Global Definitions**. This node contains parameters for certain user inputs of the physics interface nodes.

---

From the **Physics** toolbar, you can delete or disable metallurgical phases and phase transformations that are irrelevant in a given situation, and you can add additional metallurgical phases and phase transformations. You can also right-click **Austenite Decomposition** to select physics features from the context menu.

## SETTINGS



The **Label** is the default physics interface name.

The **Name** is used primarily as a scope prefix for variables defined by the physics interface. Refer to such physics interface variables in expressions using the pattern `<name>.<variable_name>`. In order to distinguish between variables belonging to different physics interfaces, the `name` string must be unique. Only letters, numbers, and underscores (`_`) are permitted in the **Name** field. The first character must be a letter.



The default **Name** (for the first physics interface in the model) is `audc`.



# Alpha-Beta Phase Transformation

This chapter describes the Alpha-Beta Phase Transformation Interface () and its functionality. It is found under the **Heat Transfer>Metal Processing** branch () when adding a physics interface.

# The Alpha-Beta Phase Transformation Interface

The **Alpha-Beta Phase Transformation** interface () is found under the **Heat Transfer>Metal Processing** () branch when adding a physics interface. The physics interface is intended for studying metallurgical phase transformations in  $\alpha$ - $\beta$  titanium alloys. You can use this interface to study diffusional, displacive, and user-defined (solid-solid) phase transformations. Physical phenomena, such as latent heat of phase transformation and transformation strains can be computed and used in Heat Transfer in Solids and Solid Mechanics. With the Nonlinear Structural Materials Module or the Geomechanics Module, plastic strains and hardening behavior of each metallurgical phase can be used in Solid Mechanics.

This interface is based on the Metal Phase Transformation interface. This chapter will only describe the nodes and settings that set the Alpha-Beta Phase Transformation interface apart from the Metal Phase Transformation interface. With regard to other settings at the physics interface level and feature level, see [The Metal Phase Transformation Interface](#).

When the Alpha-Beta Phase Transformation interface is added, several nodes are added to the **Model Builder** — three [Metallurgical Phase](#) nodes and seven [Phase Transformation](#) nodes. The interface is tailored specifically to the phase transformations that can take place in  $\alpha$ - $\beta$  titanium alloys like Ti-6Al-4V. The Alpha-Beta Phase Transformation interface defines three major phases, whose node names are:

- Beta
- Widmanstätten Alpha
- Martensitic Alpha



---

Phase transformation modeling of  $\alpha$ - $\beta$  titanium alloys sometimes includes an alpha phase that forms at the beta grain boundaries. This alpha phase is omitted here, as it often exists in small fractions. Should this level of modeling detail be warranted, additional metallurgical phase and phase transformation nodes can be added to the interface.

---

The **Initial Phase Fraction** is set to 0.11 in the **Beta** node, and 0.89 in the **Widmanstätten Alpha** node. These initial phase fractions are approximate values corresponding to an  $\alpha$ - $\beta$  titanium alloy like Ti-6Al-4V, at room temperature. Seven **Phase Transformation** nodes are also created to define the relevant phase transformations:

- Beta to Widmanstätten Alpha. This phase transformation is active under isothermal or cooling conditions, and it is active provided that the fraction of beta phase exceeds its equilibrium value.
- Beta to Martensitic Alpha (Fast). This phase transformation is active under cooling conditions, when the cooling rate exceeds a certain threshold rate, and below the **Martensite start temperature**.
- Beta to Martensitic Alpha (Slow). This phase transformation is active under cooling conditions, when the cooling rate is lower than the threshold rate mentioned above, and below the **Martensite start temperature**. Under these conditions, the maximum fraction of formed Martensitic alpha is limited by the equilibrium value of beta phase.
- Alpha to Beta. This phase transformation is used to model the dissolution of Widmanstätten and Martensitic alpha, into beta phase. It is active under heating conditions, and when the temperature exceeds the so-called beta start temperature.
- Martensitic Alpha to Beta. This phase transformation represents the dissolution of Martensitic alpha into beta phase. It is active at temperatures above the martensite dissolution temperature. In this phase transformation, the beta phase strives toward its equilibrium value.
- Martensitic Alpha to Widmanstätten Alpha. This phase transformation represents the dissolution of Martensitic alpha into Widmanstätten alpha phase. It is active at temperatures above the martensite dissolution temperature. In this phase transformation, the Widmanstätten alpha phase strives toward its equilibrium value.
- Beta Re-Formation. This phase transformation represents a simplified description of complete dissolution of alpha phase. It is active when the temperature exceeds the beta transus.



A **Parameters** node is automatically created under **Global Definitions**. This node contains parameters for certain user inputs of the physics interface nodes. Generated parameters include default values for characteristic transformation temperatures, for the Martensitic alpha rate threshold, etc.

---

From the **Physics** toolbar, you can delete or disable metallurgical phases and phase transformations that are irrelevant in a given situation, and you can add additional metallurgical phases and phase transformations. You can also right-click **Alpha-Beta Phase Transformation** to select physics features from the context menu.



For an example how to model phase transformation that occur during welding of a titanium plate, see *Welding of a Titanium Plate*:

Application Library path

**Metal\_Processing\_Module/Titanium\_Phase\_Transformations/welding\_of\_a\_titanium\_plate.**

---



## SETTINGS

The **Label** is the default physics interface name.



The **Name** is used primarily as a scope prefix for variables defined by the physics interface. Refer to such physics interface variables in expressions using the pattern `<name>.<variable_name>`. In order to distinguish between variables belonging to different physics interfaces, the `name` string must be unique. Only letters, numbers, and underscores (`_`) are permitted in the **Name** field. The first character must be a letter.

The default **Name** (for the first physics interface in the model) is `abp`.

## Carburization

This chapter describes the Carburization interface () and its functionality. It is found under the **Heat Transfer>Metal Processing** branch () when adding a physics interface.

# The Carburization Interface

The **Carburization** interface () is found under the **Heat Transfer>Metal Processing** () branch when adding a physics interface. The physics interface is intended for modeling carburization processes during heat treatment. The carburization process is based on diffusion, and it is used to compute the evolving mass fraction of carbon when a component is exposed to a carbon rich atmosphere.

When the Carburization interface is added, three default nodes are added to the **Model Builder** — a **Carburization** node, an **Initial Values** node, and a **Zero Carbon Flux** node.

## SETTINGS

The **Label** is the default physics interface name.

The **Name** is used primarily as a scope prefix for variables defined by the physics interface. Refer to such physics interface variables in expressions using the pattern `<name>.<variable_name>`. In order to distinguish between variables belonging to different physics interfaces, the `name` string must be unique. Only letters, numbers, and underscores (`_`) are permitted in the **Name** field. The first character must be a letter.

The default **Name** (for the first physics interface in the model) is `carb`.

## TEMPERATURE

Carbon diffusion is inherently temperature dependent. Select the temperature field to use from the **Temperature** list.

## CARBURIZING CYCLE

This section contains settings for the carburization process. Select the carbon potential model to use from the **Carbon potential model** list. Select **Boost-diffuse cycle** if you want to model a two-stage carburization process, where a boost stage is followed by a diffuse stage. Define the **Boost carbon potential**  $c_{\text{boost}}$ , the **Diffuse carbon potential**  $c_{\text{diffuse}}$ , and the **Boost period**  $t_{\text{boost}}$ . Select **User defined** if you want to use your own expression for the carbon potential of the carburization process. Define the **Carbon potential**  $c_{\text{pot}}$ .

## *Carburization*

---

The Carburization node defines the carbon diffusion inside the domain.



## CARBON DIFFUSION

From the **Diffusion coefficient** list you select the diffusion coefficient that is used in the diffusion equation. Select **Arrhenius** to define a thermally activated diffusion coefficient. Define the **Pre-exponential factor**  $D_0$  and the **Activation energy**  $Q_D$ . Select **User defined** to define the **Diffusion coefficient**  $D$  directly.

### *Carbon Flux*

---

The Carbon Flux node is used to define the carbon exchange with the surrounding carbon atmosphere (the exterior).

## CARBON MASS TRANSFER

From the **Carbon potential list**, select the carbon potential of the exterior  $c_{\text{ext}}$ . Select **Carbon potential** to use the carbon potential defined at the physics interface level. Select **User defined** to define the carbon potential directly. From the **Mass transfer coefficient** list, select the mass transfer coefficient to be used to define the carbon flux. Select **Arrhenius** to define a thermally activated mass transfer coefficient. Define the **Pre-exponential factor**  $b_0$  and the **Activation energy**  $Q_b$ . Select **User defined** to define the **Mass transfer coefficient**  $b$  directly.

### *Zero Carbon Flux*

---

The Zero Carbon Flux node is used to define boundaries where no carbon exchange takes place with the exterior.

### *Carbon Concentration*

---

The Carbon Concentration node is used to specify the carbon concentration at an exterior domain boundary.

## CARBON CONCENTRATION

From the list, select the carbon concentration  $c_0$ . Select **Carbon potential** to use the carbon potential defined at the physics interface level. Select **User defined** to specify the carbon concentration  $c_0$  directly.


### *Initial Values*

---

The Initial Values node is used to specify the initial carbon concentration  $c$ .




# Multiphysics Interfaces and Couplings

The Metal Processing Module contains predefined multiphysics interfaces to facilitate the coupling to Heat Transfer in Solids and Solid Mechanics interfaces. The physics interfaces are found under the **Heat Transfer>Metal Processing** branch () when adding a physics interface — **Heat Transfer with Phase Transformations** and **Steel Quenching**. Two multiphysics coupling features — **Phase Transformation Latent Heat** and **Phase Transformation Strain**, can be added to facilitate the coupling to Heat Transfer in Solids and Solid Mechanics.

In this chapter:

- [Heat Transfer with Phase Transformations](#)
- [Steel Quenching](#)
- [Phase Transformation Latent Heat Multiphysics Coupling](#)
- [Phase Transformation Strain Multiphysics Coupling](#)

# Heat Transfer with Phase Transformations

The **Heat Transfer with Phase Transformations** multiphysics interface () combines a Heat Transfer in Solids interface with a Metal Phase Transformation interface. When the Heat Transfer with Phase Transformations multiphysics interface is added, the multiphysics coupling **Phase Transformation Latent Heat** is included.

## *On the Constituent Physics Interfaces*


---

- The Heat Transfer in Solids interface is described in [The Heat Transfer in Solids Interface](#) of the Heat Transfer Module User's Guide.
- The Metal Phase Transformation interface is described in [The Metal Phase Transformation Interface](#) chapter.

### **SETTINGS FOR PHYSICS INTERFACES AND COUPLING FEATURES**

The **Enable phase transformation latent heat** check box is selected in the Metal Phase Transformation interface.

# Steel Quenching

The **Steel Quenching** multiphysics interface () combines a Heat Transfer in Solids interface with an Austenite Decomposition interface and a Solid Mechanics interface. When the Steel Quenching multiphysics interface is added, the **Phase Transformation Latent Heat** and **Phase Transformation Strain** multiphysics couplings are included.

## *On the Constituent Physics Interfaces*

---

- The Heat Transfer in Solids interface is described in [The Heat Transfer in Solids Interface](#).
- The Austenite Decomposition interface is described in [The Austenite Decomposition Interface](#) chapter.
- The Solid Mechanics interface is described in [The Solid Mechanics Interface](#) of the *Structural Mechanics Module User's Guide*.


### **SETTINGS FOR PHYSICS INTERFACES AND COUPLING FEATURES**

The following check boxes are selected in the Austenite Decomposition interface:

- Compute effective thermal properties
- Compute effective mechanical properties
- Enable phase transformation latent heat
- Enable transformation induced plasticity
- Enable thermal strains

The discretization for the temperature field in the Heat Transfer in Solids interface is set to Linear, because thermal strains are typically linear in the Solid Mechanics interface.

# Phase Transformation Latent Heat Multiphysics Coupling

The **Phase Transformation Latent Heat** multiphysics coupling () is used to add the latent heat that is produced by a phase transformation physics interface as a heat source term in the heat equation of the coupled Heat Transfer in Solids interface. When the coupling is used, no separate Heat Source feature in the Heat Transfer interface is required.



When the **Phase Transformation Latent Heat** multiphysics coupling is used, the effect of latent heat should not be added as a **Heat Source** in the Heat Transfer in Solids interface, as this incorrectly amounts to adding the latent heat contribution twice.

---

## SETTINGS

The **Label** is the default multiphysics coupling feature name.

The **Name** is used primarily as a scope prefix for variables defined by the coupling node. Refer to such variables in expressions using the pattern `<name>.<variable_name>`. In order to distinguish between variables belonging to different coupling nodes or physics interfaces, the `name` string must be unique. Only letters, numbers, and underscores (`_`) are permitted in the **Name** field. The first character must be a letter.

The default **Name** (for the first multiphysics coupling feature in the model) is `1ht1`.

## DOMAIN SELECTION

When the coupling is added, selected entities in the coupled Heat Transfer in Solids and Metal Phase Transformation interfaces are included by default.

## COUPLED INTERFACES

This section defines the physics involved in the multiphysics coupling. The **Metal Phase Transformation** and **Heat Transfer** lists include all applicable physics interfaces.

The default values depend on how the coupling node is created.


- If the node is added from the **Physics** ribbon (Windows users), **Physics** contextual toolbar (Mac and Linux users), or context menu (all users), then the first physics interface of each type in the component is selected as the default.
- If it the node added automatically when a multiphysics interface is selected in the **Model Wizard** or **Add Physics** window, then the two participating physics interfaces are selected.



See also the Theory for [Phase Transformation Latent Heat](#)

---

# Phase Transformation Strain Multiphysics Coupling

The Phase Transformation Strain multiphysics coupling () is used to include phase transformation strains that are produced by a phase transformation physics interface as an inelastic strain contribution to the total strain in the Solid Mechanics interface.



---

Note that if **Enable thermal strains** has been selected at the **Metal Phase Transformation** interface level, thermal strain effects are included in the phase transformation strains. In this situation no **Thermal Expansion** coupling should be used between Solid Mechanics and Heat Transfer in Solids.

---

## SETTINGS

The **Label** is the default multiphysics coupling feature name.

The **Name** is used primarily as a scope prefix for variables defined by the coupling node. Refer to such variables in expressions using the pattern `<name>.<variable_name>`. In order to distinguish between variables belonging to different coupling nodes or physics interfaces, the `name` string must be unique. Only letters, numbers, and underscores (`_`) are permitted in the **Name** field. The first character must be a letter.

The default **Name** (for the first multiphysics coupling feature in the model) is `ptstr1`.

## DOMAIN SELECTION

When the coupling is added, selected entities in the coupled Solid Mechanics and Metal Phase Transformation interfaces are included by default.

## COUPLED INTERFACES

This section defines the physics involved in the multiphysics coupling. The **Metal Phase Transformation** and **Solid Mechanics** lists include all applicable physics interfaces.



The default values depend on how the coupling node is created.

- If the node is added from the **Physics** ribbon (Windows users), **Physics** contextual toolbar (macOS and Linux users), or context menu (all users), then the first physics interface of each type in the component is selected as the default.
- If it the node added automatically when a multiphysics interface is selected in the **Model Wizard** or **Add Physics** window, then the two participating physics interfaces are selected.



See also the Theory for [Phase Transformation Strains](#)

---



# I n d e x

- A** additional source phases 53
  - alpha-beta phase transformation interface 17
  - Application Libraries window 10
  - application library examples
    - carburization and quenching of a steel gear 29
    - phase transformations in a round bar 23
    - transformation diagram computation 27, 86
  - austenite decomposition interface 17
- C** calibration of phase transformation models 23
  - continuous cooling transformation diagram 23
  - time-temperature transformation diagram 23
  - carbon concentration (node) 89
  - carbon flux (node) 89
  - carburization (node) 88
  - carburization interface 18
  - compute effective electromagnetic properties 69
  - compute effective mechanical properties 69
  - compute effective thermal properties 69
  - create compound material 32, 69
- D** documentation 9
- E** emailing COMSOL 10
  - enable phase plasticity 69
  - enable phase transformation latent heat 69
  - enable thermal strains 69–70
  - enable transformation induced plasticity 69
- H** heat transfer properties 54
  - heat transfer with phase transformations interface 28
- I** importing material properties 33
  - initial phase fraction 80, 85
  - initial values (node) 89
  - internet resources 9
- J** Johnson-Mehl-Avrami-Kolmogorov model 21, 45
  - parameterized ttt diagram 21
  - parameterized ttt diagram, fixed exponent 21
  - time, equilibrium and exponent 21
  - ttt diagram data 21
  - ttt diagram data, fixed exponent 21
- K** Kirkaldy-Venugopalan model 22, 48
  - parameterized ttt diagram 22
  - rate coefficient 22
  - ttt diagram data 22
  - knowledge base, COMSOL 11
  - Koistinen-Marburger model 22, 51
    - Koistinen-Marburger coefficient 22
    - martensite finish temperature 22
    - martensite start temperature 22
- L** Leblond-Devaux model 21, 43
  - general coefficients 21
  - parameterized ttt diagram 21
  - time and equilibrium 21
  - ttt diagram data 21
- M** mechanical properties 55
  - elasticity 55
  - equivalent plastic strains 57
  - plasticity 56

- metal phase transformation interface 16, 68
- metallurgical phase (node) 68, 70
- Metallurgical phases 20
- MPH-files 10
- P**
  - parameterized ttt diagram 52
  - phase fraction
    - initial phase fraction 80, 85
  - phase transformation (node) 68, 73
  - phase transformation latent heat 30, 94
  - phase transformation latent heat multiphysics coupling 94
  - phase transformation strain 30
  - phase transformation strain multiphysics coupling 96
  - phase transformations 20
- S**
  - selecting discretizations 31
    - discretizations for displacements 31
    - discretizations for phase fractions 31
  - steel quenching interface 29
- T**
  - technical support, COMSOL 10
  - thermal expansion 58
  - transformation condition (node) 77
    - phase transformation 77
  - transformation induced plasticity 59
- W**
  - websites, COMSOL 11
- Z**
  - zero carbon flux (node) 89