

Glacier Flow

Introduction

This example shows how you can set up a glacier flow model in principle. It exemplifies several modeling steps which are important for glacier modeling:

- The creation of the geometry
- The modeling of a non-Newtonian fluid
- A way to investigate and compare different aspects of the model within the same model file

The cryosphere is the part of the climate system that contains frozen water and makes up 80% of our fresh water. Using the COMSOL Multiphysics® software, we can simulate classical ice flow to analyze cryosphere dynamics and assess climate change effects such as shrinking glaciers and rising sea levels.

In 1773, André Bordier, a Swiss naturalist, used the term "fluid" to describe the movement of mountain glaciers for the first time. However, it took more than a century for scientists to agree on a unified description for the dynamics of glaciers.

One of the most confusing aspects of glaciers is the observation that ice exhibits both viscous and plastic behavior, depending on the glacier. British physicist John Glen observed and described this intermediate behavior using a nonlinear relationship between stress and strain. Known as shear thinning, this classical behavior applies to many different fluids (for example, ketchup and blood).

The life of any mountain glacier can be schematically described as follows:

- In the accumulation zone, snow piles up at a high altitude where the temperature is low, and compresses into ice
- The ice starts deforming and flowing down the slope under its own weight
- In the ablation zone at lower altitude, where the temperature is higher, the ice melts away

Figure 1 shows a sketch of a typical mountain glacier with the accumulation zone where the snow piles up and the ablation zone where the ice melts to water.

Glaciologists devide glaciers in different categories, depending on their thermal structure:

• Cold glaciers where the temperature of the ice is below the pressure melting temperature throughout the glacier, except for maybe a thin surface layer.

- Temperate glaciers where the whole glacier is at the pressure melting temperature, except for some seasonal variations and freezing at the surface layer.
- Polythermal glaciers, where some parts of the glacier are cold and some are temperate. The cold parts are usually the highest accumulation area as well as the upper part of an ice column, whereas the surface and the base are temperate. In polythermal glaciers, cold and temperate ice is separated by the cold-temperate transition surface (CTS).



Figure 1: Sketch of a typical mountain glacier.

Most of the alpine glaciers are temperate, but at higher altitudes, also polythermal glaciers can be found. Cold glaciers can typically be found in polar regions like Greenland and Antarctica. Polythermal glaciers are common at high latitudes and high altitudes (like the Scandinavian Mountains, European Alps, Himalaya).

In this example a realistic geometry - a 2D cross section inspired by the Arolla glacier in the Pennine alps in Switzerland - is used to simulate the nonisothermal flow of the ice mass downslope, under its own weight and subject to basal sliding. Two versions of the glacier model are investigated: A cold glacier version and a temperate glacier version.

Model Definition

In this example the geometry is inspired by the Haut glacier d'Arolla in the Swiss Alps, which is 5 kilometers long and up to 200 meters thick with an average slope of 15%. Figure 2 shows a photograph of the Arolla glacier.



Figure 2: Aerial photo of the Arolla glacier in the Pennine Alps in Switzerland.

The model is built in 2D as a cross section through the flow line of the glacier. It is constructed from two datasets, one for the ice surface and one for the bedrock surface. Figure 3 shows the model geometry, colored by the ice thickness.



Figure 3: A 2D cross section of the Arolla glacier is constructed as model geometry. Here it is colored by the ice thickness and the y-axis is stretched compared to the x-axis to have a better view of the vertical differences.

The ice flow is simulated using the Stokes equations describing the so-called creeping flow:

$$\rho \frac{\partial \mathbf{u}}{\partial t} = \nabla \cdot \left[-p\mathbf{I} + \mu(\nabla \mathbf{u} + \nabla \mathbf{u}^T)\right] + \rho \mathbf{g}$$
(1)

$$\nabla \cdot \mathbf{u} = 0 \tag{2}$$

where ρ is the density, **u** is the velocity vector, *p* is the pressure, **g** is the acceleration of gravity, and μ is the dynamic viscosity.

Using Glen's flow law, the viscosity µ can be described as

$$\mu = \frac{1}{2}A^{-\frac{1}{n}}\dot{\gamma}^{n-1}$$
(3)

where γ is the shear rate and is classically defined as the norm of the strain rate tensor

$$\gamma(\mathbf{u}) = \left\| \frac{1}{2} (\nabla \mathbf{u} + \nabla \mathbf{u}^T) \right\|.$$
(4)

To calculate the flow rate factor *A* in Equation 3 an Arrhenius law can be used:

$$A(T,p) = A_0 e^{\left(\frac{Q}{RT}\right)}$$
(5)

with A_0 being the flow rate constant, Q the activation energy, and R the universal gas constant. According to the literature, A_0 and Q are a matter of debate. In this case we use,

$$A_0 = \begin{pmatrix} 3.985e^{-13}; \text{ for } T <= -10^{\circ}C \\ 1.916e^3; \text{ for } T >-10^{\circ}C \end{pmatrix}$$
 and (6)

$$Q = \begin{pmatrix} 60e^3; \text{ for } T <= -10^{\circ}C \\ 139e^3; \text{ for } T > -10^{\circ}C \end{pmatrix}$$
(7)

To calculate the temperature distribution in the model, the energy balance equation is solved:

$$\rho c_p \left(\frac{\partial T}{\partial t} + \mathbf{u} \cdot \nabla T \right) - \nabla (k \cdot \nabla T) = Q$$
(8)

where c_p is the heat capacity and k is the thermal conductivity of ice. Both are functions of temperature and are described using the following numerical value equations (see, for example, Ref. 4):

$$c_p(T) \left[\frac{J}{kgK} \right] = 146.3 + 7.253T[K] \text{ and}$$
 (9)

$$k(T) \left[\frac{W}{mK} \right] = 9.828 e^{-0.0057 T[K]}.$$
 (10)

In terms of fluid, the inflow and outflow boundary conditions are the normal constraints, corresponding to the applied pressure of the ice, which is not included in the domain. It simply corresponds to an assigned hydrostatic (or cryostatic) pressure. The upstream boundary weighs on the domain, thus contributing to a streamwise velocity, while the downstream boundary resists to the flow. The surface of the glacier is a free surface.

If the temperature at the ice-bed contact is at the pressure melting temperature $T_{\rm m}$ — which is the case if the glacier is temperate — the glacier can slide over the base. If the temperature is below $T_{\rm m}$ a no slip condition would be appropriate. In case of a temperate glacier, a slip length of 50 m is defined at the lower boundary.

In terms of heat transfer, the surface is influenced by the ambient temperature and is subject of convective heat exchange and radiative heat exchange with the environment. For a cold glacier, the boundary in contact with the bedrock is subject to a geothermal heat flux, which could be modeled as a boundary condition. Typical geothermal heat fluxes are of the order of 40–120 mW/m². In this case a geothermal heat flux of 120 mW/m² is chosen.

In case the glacier is temperate, the temperature at the bedrock can be assumed to be at pressure melting point temperature, which is

$$T_m = T_{\rm tp} - \beta_{\rm CC} (p - p_{\rm tp}) \tag{11}$$

with $T_{\rm tp}$ and $p_{\rm tp}$ being the triple point temperature and pressure of water (see Ref. 2). Heat is allowed to leave and enter the domain at the inflow and outflow boundaries.

A mapped mesh is used that is consistent with the aspect ratio of the geometry.

The external weather conditions are an important input data for geophysical simulations. Accessing the ASHRAE 2017 database, we can import the average external temperature and wind velocities at a given time of the year for more than 6000 weather stations all over the world. Here, we use the data from the Grand Saint Bernard station in the Swiss Alps, located at about 25 km of the Arolla glacier on the first of February at noon. The ambient temperature is imposed at the glacier surface and the wind velocities are used to simulate a convective heat flux at the surface.

Results and Discussion

The results are first evaluated after 10 years, when the flow has reached a stationary state. Figure 4 shows the velocity for the "cold glacier" conditions. At the bedrock the velocity is zero and there is hardly any in- and outflow at the upper and lower boundaries. However, there is some uncertainty regarding basal sliding which is not present in this case: Depending on the ice thickness and the geothermal heat flux, even for cold glacier conditions it is possible that a water layer builds up at the bedrock as the heat can only be transported upwards very slowly.



Figure 4: Velocity magnitude after 10 years of simulated time for a given heat flux at the bottom (cold glacier model).

The temperature after 10 years of simulation time (Figure 5) shows that the main heat source is the external temperature being in exchange with the glacier surface. Here the highest temperatures occur during summer and the lowest during winter season. The ablation zone of the glacier is colder on average than the accumulation zone. The temperature at the bedrock is higher than in the middle of the glacier due to the geothermal heat flux, however, it is still well below pressure melting temperature.



Figure 5: Temperature distribution after 10 years of simulated time for a given heat flux at the bottom (cold glacier model).

The next figures show the results for the temperate glacier conditions. Here the temperature at the bedrock is set to pressure melting point temperature and therefore it can be assumed that the ice can slide over the bedrock. The velocity field which is displayed in Figure 6 shows this as the velocity is non-zero at the bottom of the glacier. In general the velocities are higher in this case.



Figure 6: Velocity magnitude after 10 years of simulated time for the bottom temperature being at pressure melting point (temperate glacier model).

The temperature distribution after 10 years of simulation time is shown in Figure 7. Again the ablation zone is colder on average than the accumulation zone and the temperature field shows a line structure which is due to a combination of the seasonal heating and cooling from the surface and the influence of the mesh and time step size. With refined mesh the structures still appear on a smaller scale.



Figure 7: Temperature distribution after 10 years of simulated time for the bottom temperature being at pressure melting point temperature (temperate glacier model).

Figure 8 shows the tangential velocity component along the glacier surface for both the cold and the temperate glacier scenario. As already mentioned the velocities are much bigger for the temperate scenario.



Figure 8: Tangential velocity component along the glacier surface after 10 years of simulated time.

References

1. A. Aschwanden and H. Blatter "Mathematical modeling and numerical simulation of polythermal glaciers," *J. Geophys. Res.*, vol. 114 (F1), p. F01027, 2008. (10.1029/2008JF001028.)

2. A. Aschwanden, "Thermodynamics of Glaciers", McCarthy Summer School, 2010. (https://glaciers.gi.alaska.edu/sites/default/files/mccarthy/ Notes_thermodyn_Aschwanden.pdf)

3. R. Greve, and H. Blatter, Dynamics of Ice Sheets and Glaciers, Springer, 2009.

4. C. Ritz, "Time dependent boundary conditions for calculation of temperature fields in ice sheets," *The Physical Basis of Ice Sheet Modelling*, vol. 170, pp. 207–216, 1987.

Application Library path: Subsurface_Flow_Module/Heat_Transfer/ glacier_flow_2d

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click 🔗 Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click 9 2D.
- 2 In the Select Physics tree, select Fluid Flow>Nonisothermal Flow>Laminar Flow.
- 3 Click Add.
- 4 Click \bigcirc Study.
- 5 In the Select Study tree, select General Studies>Time Dependent.
- 6 Click 🗹 Done.

GLOBAL DEFINITIONS

Parameters I

I In the Model Builder window, under Global Definitions click Parameters I.

Start by setting the parameters defining the material properties of ice and the constants needed to calculate the ice flow. You can either import them from the file "glacier_flow_2d_parameters.txt" from the model's Application Librabries folder or enter them as follows:

- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
rho_ice	910[kg/m^3]	910 kg/m³	Density of ice
mu_ice	5e12[Pa*s]	5E12 Pa·s	Dynamic viscosity of ice
LSlip	50[m]	50 m	Slip length
T_init	-10[degC]	263.15 K	Initial temperature

Name	Expression	Value	Description
betaCC	9.8e-8[K/Pa]	9.8E-8 m·s²·K/kg	Clapeyron constant
n_ice	3	3	Rheological exponent for ice
T_tp	0.01[degC]	273.16 K	Temperature at triple point of water
p_tp	611.657[Pa]	611.66 Pa	Pressure at triple point of water
q_geo	120[mW/m^2]	0.12 W/m ²	Geothermal heat flux

Glacier Base

Now import the data to specify the glacier geometry and define the functions to calculate the flow viscosity and the pressure melting temperature.

- I In the Home toolbar, click f(X) Functions and choose Global>Interpolation.
- 2 In the Settings window for Interpolation, locate the Definition section.
- 3 From the Data source list, choose File.
- 4 Click 📂 Browse.
- 5 Browse to the model's Application Libraries folder and double-click the file glacier_flow_2d_arolla01.txt.
- 6 Click **[F-** Import.
- 7 In the Label text field, type Glacier Base.
- 8 Locate the Units section. In the Function table, enter the following settings:

Function	Unit
intl	m

9 In the Argument table, enter the following settings:

Argument	Unit
t	m

Glacier Surface

- I In the Home toolbar, click f(X) Functions and choose Global>Interpolation.
- 2 In the Settings window for Interpolation, locate the Definition section.
- 3 From the Data source list, choose File.
- 4 Click 📂 Browse.

- 5 Browse to the model's Application Libraries folder and double-click the file glacier_flow_2d_arolla02.txt.
- 6 Click **[I-]** Import.
- 7 In the Label text field, type Glacier Surface.

8 Locate the Units section. In the Function table, enter the following settings:

Function	Unit
int2	m

9 In the Argument table, enter the following settings:

Argument	Unit
t	m

Now define the flow rate constant A_0 and the activation energy Q to calculate the flow rate factor (Equation 5).

Α0

- I In the Home toolbar, click f(X) Functions and choose Global>Step.
- 2 In the Settings window for Step, type A0 in the Label text field.
- **3** In the **Function name** text field, type A0.
- 4 Locate the Parameters section. In the Location text field, type 263.15.
- 5 In the From text field, type 3.985e-13.
- 6 In the To text field, type 1.916e3.
- 7 Click to expand the Smoothing section. Clear the Size of transition zone check box.

Q

- I Right-click **A0** and choose **Duplicate**.
- 2 In the Settings window for Step, type Q in the Label text field.
- 3 In the Function name text field, type Q.
- 4 Locate the **Parameters** section. In the **From** text field, type 60e3.
- 5 In the To text field, type 139e3.

DEFINITIONS

Define the thermal conductivity, the heat capacity, and the viscosity of ice as variables depending on the temperature T. As T is calculated in **Component I**, the variables have to be defined locally, that is, in **Component I**, too.

Variables I

- I In the Model Builder window, expand the Component I (compl)>Definitions node.
- 2 Right-click **Definitions** and choose **Variables**.
- 3 In the Settings window for Variables, locate the Variables section.
- **4** In the table, enter the following settings:

Name	Expression	Unit	Description
k_ice	9.828[W/(m*K)]*exp(- 0.0057[1/K]*T)	W/(m·K)	Conductivity of ice
cp_ice	146.3[J/(kg*K)]+ 7.253[J/(kg*K^2)]*T	J/(kg·K)	Heat capacity of ice

m_ice

- I In the Home toolbar, click f(X) Functions and choose Local>Analytic.
- 2 In the Settings window for Analytic, type m_ice in the Label text field.
- 3 In the Function name text field, type m_ice.
- 4 Locate the Definition section. In the Expression text field, type abs(AO(T)*exp(-Q(T)/ (R_const*T)))^(-1/3)*0.5 according to Equation 5.
- **5** In the **Arguments** text field, type T.
- 6 Locate the Units section. In the Function text field, type Pa*s.
- 7 In the table, enter the following settings:

Argument	Unit
Т	К

8 Locate the Plot Parameters section. In the table, enter the following settings:

Argument	Lower limit	Upper limit	Unit
Т	260	280	К



9 Click **I** Plot to plot the function and compare with the figure below.

Specify the pressure melting point temperature T_m according to Equation 11.

T_m

I In the Home toolbar, click f(x) Functions and choose Local>Analytic.

2 In the Settings window for Analytic, type T_m in the Label text field.

3 In the **Function name** text field, type T_m.

4 Locate the **Definition** section. In the **Expression** text field, type T_tp-betaCC*(p-p_tp).

5 In the Arguments text field, type p.

6 Locate the Units section. In the Function text field, type K.

7 In the table, enter the following settings:

Argument	Unit
Ρ	Ра

8 Locate the Plot Parameters section. In the table, enter the following settings:

Argument	Lower limit	Upper limit	Unit
Ρ	0	120000	Pa

9 Click 💽 Plot.

Ambient Properties 1 (ampr1)

Now define the ambient properties. As there is no data for the Arolla glacier directly, select a station where similar weather conditions can be expected.

- I In the Physics toolbar, click **=** Shared Properties and choose Ambient Properties.
- 2 In the Settings window for Ambient Properties, locate the Ambient Settings section.
- 3 From the Ambient data list, choose Meteorological data (ASHRAE 2017).
- 4 Locate the Location section. Click Set Weather Station.
- 5 In the Weather Station dialog box, select Europe>Switzerland> COL DU GRAND ST BERNARD (067170) in the tree.
- 6 Click OK.
- 7 In the Settings window for Ambient Properties, locate the Time section.

8 Find the Date subsection. In the table, enter the following settings:

01 01	

9 Find the Local time subsection. In the table, enter the following settings:

Hour	Minute	Second
00	00	00

IO Locate the Ambient Conditions section. From the Temperature list, choose Low.

View I

Use automatic scaling of the axes to get a better view of the vertical changes within the glacier.

Axis

- I In the Model Builder window, expand the Component I (compl)>Definitions>View I node, then click Axis.
- 2 In the Settings window for Axis, locate the Axis section.
- 3 From the View scale list, choose Automatic.
- 4 Click 🍈 Update.

GEOMETRY I

Build the geometry using the interpolation functions defined above.

Parametric Curve 1 (pc1)

- I In the Model Builder window, expand the Component I (compl)>Geometry I node.
- 2 Right-click Geometry I and choose More Primitives>Parametric Curve.
- 3 In the Settings window for Parametric Curve, locate the Parameter section.
- 4 In the Maximum text field, type 5000.
- 5 Locate the **Expressions** section. In the **x** text field, type **s**.
- 6 In the y text field, type int1(s).
- 7 Click 틤 Build Selected.

Parametric Curve 2 (pc2)

- I In the Geometry toolbar, click 😕 More Primitives and choose Parametric Curve.
- 2 In the Settings window for Parametric Curve, locate the Parameter section.
- **3** In the **Maximum** text field, type 5000.
- **4** Locate the **Expressions** section. In the **x** text field, type **s**.
- 5 In the y text field, type int2(s).
- 6 Click 틤 Build Selected.

Line Segment I (IsI)

- I In the Geometry toolbar, click 😕 More Primitives and choose Line Segment.
- 2 On the object **pc2**, select Point 1 only.
- 3 In the Settings window for Line Segment, locate the Endpoint section.
- 4 Find the End vertex subsection. Click to select the 💷 Activate Selection toggle button.
- **5** On the object **pc1**, select Point 1 only.
- 6 Click 📄 Build Selected.

Line Segment 2 (Is2)

- I In the Geometry toolbar, click 🚧 More Primitives and choose Line Segment.
- 2 On the object **pc2**, select Point 2 only.
- 3 In the Settings window for Line Segment, locate the Endpoint section.
- 4 Find the End vertex subsection. Click to select the 🔲 Activate Selection toggle button.
- 5 On the object **pc1**, select Point 2 only.
- 6 Click 틤 Build Selected.

Convert to Solid 1 (csol1)

I In the Geometry toolbar, click 🙀 Conversions and choose Convert to Solid.

- 2 Select the object **pc2** only.
- 3 Click the **Select All** button in the **Graphics** toolbar.
- 4 In the Settings window for Convert to Solid, click 📳 Build Selected.

Form Union (fin)

In the **Geometry** toolbar, click 📗 Build All.

MATERIALS

Define the material ice in the next step. Introduce it as empty material node, first. As soon as the physics has been defined, the material node menu will show you which properties are needed for the simulation.

Ice

- I In the Model Builder window, under Component I (compl) right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type Ice in the Label text field.

LAMINAR FLOW (SPF)

Now define the flow properties.

- I In the Model Builder window, under Component I (compl) click Laminar Flow (spf).
- 2 In the Settings window for Laminar Flow, locate the Physical Model section.
- 3 Select the Neglect inertial term (Stokes flow) check box.
- 4 Select the Include gravity check box.
- **5** In the p_{ref} text field, type ampr1.p_amb.
- **6** Specify the \mathbf{r}_{ref} vector as.

x x int2(x) y

This guarantees that the pressure at the ice surface is equal to zero or the ambient pressure, respectively.

Fluid Properties 1

- I In the Model Builder window, under Component I (compl)>Creeping Flow (spf) click Fluid Properties I.
- 2 In the Settings window for Fluid Properties, locate the Fluid Properties section.

3 Find the **Constitutive relation** subsection. From the list, choose **Inelastic non-Newtonian**. For the **Lower shear rate limit** enter 1e-15 [1/s].

Wall 2

- I In the **Physics** toolbar, click **Boundaries** and choose **Wall**.
- 2 Select Boundary 3 only.
- 3 In the Settings window for Wall, locate the Boundary Condition section.
- 4 From the Wall condition list, choose Slip velocity.
- 5 Select the Use viscous slip check box.
- 6 In the L_s text field, type LSlip. This boundary condition is needed for the temperate glacier model. For the cold glacier flow it has to be disabled.

Open Boundary I

- I In the Physics toolbar, click Boundaries and choose Open Boundary.
- 2 Select Boundary 4 only.
- 3 In the Settings window for Open Boundary, locate the Boundary Condition section.
- 4 Clear the Compensate for hydrostatic pressure approximation check box.

Open Boundary 2

- I In the Physics toolbar, click Boundaries and choose Open Boundary.
- 2 Select Boundaries 1 and 2 only.

Pressure Point Constraint I

- I In the Physics toolbar, click 💭 Points and choose Pressure Point Constraint.
- 2 Select Point 2 only.
- **3** In the **Settings** window for **Pressure Point Constraint**, locate the **Pressure Constraint** section.
- 4 Clear the Compensate for hydrostatic pressure approximation check box.

HEAT TRANSFER IN FLUIDS (HT)

- I In the Model Builder window, under Component I (comp1) click Heat Transfer in Fluids (ht).
- 2 In the Settings window for Heat Transfer in Fluids, locate the Physical Model section.
- **3** In the d_z text field, type 500[m].

Initial Values 1

- I In the Model Builder window, under Component I (compl)>Heat Transfer in Fluids (ht) click Initial Values I.
- 2 In the Settings window for Initial Values, locate the Initial Values section.
- **3** In the *T* text field, type T_init.

Heat Flux 1

- I In the Physics toolbar, click Boundaries and choose Heat Flux.
- 2 Select Boundary 3 only.
- 3 In the Settings window for Heat Flux, locate the Heat Flux section.
- **4** In the q_0 text field, type q_geo.

Open Boundary I

- I In the Physics toolbar, click Boundaries and choose Open Boundary.
- **2** Select Boundaries 1, 2, and 4 only.
- 3 In the Settings window for Open Boundary, locate the Upstream Properties section.
- 4 From the T_{ustr} list, choose Ambient temperature (amprl).

Heat Flux 2

- I In the Physics toolbar, click Boundaries and choose Heat Flux.
- **2** Select Boundary 4 only.
- 3 In the Settings window for Heat Flux, locate the Heat Flux section.
- 4 From the Flux type list, choose Convective heat flux.
- 5 From the Heat transfer coefficient list, choose External forced convection.
- **6** In the L text field, type 5000.
- 7 From the U list, choose Wind speed (amprl).
- **8** From the p_A list, choose **Ambient absolute pressure (amprl)**.
- 9 From the $T_{\rm ext}$ list, choose Ambient temperature (amprl).

Surface-to-Ambient Radiation 1

- I In the Physics toolbar, click Boundaries and choose Surface-to-Ambient Radiation.
- 2 Select Boundary 4 only.
- 3 In the Settings window for Surface-to-Ambient Radiation, locate the Surface-to-Ambient Radiation section.
- **4** From the ε list, choose **User defined**. In the associated text field, type **0.97**.
- **5** From the T_{amb} list, choose **Ambient temperature (amprl)**.

Temperature I

- I In the Physics toolbar, click Boundaries and choose Temperature.
- 2 Select Boundary 3 only.
- 3 In the Settings window for Temperature, locate the Temperature section.
- 4 In the T₀ text field, type T_m(p). This boundary condition is needed for the temperate glacier model. For the cold glacier flow it has to be disabled.

MATERIALS

Having defined the physics, now fill in the empty expressions in the Materials node.

lce (mat1)

- I In the Model Builder window, under Component I (compl)>Materials click Ice (matl).
- 2 In the Settings window for Material, locate the Material Contents section.
- **3** In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Fluid consistency coefficient	m_pow	m_ice(T)	Pa·s	Power law
Flow behavior index	n_pow	1/n_ice	1	Power law
Thermal conductivity	k_iso ; kii = k_iso, kij = 0	k_ice	W/(m·K)	Basic
Density	rho	rho_ice	kg/m³	Basic
Heat capacity at constant pressure	Ср	cp_ice	J/(kg·K)	Basic

MESH I

Mapped I

In the Mesh toolbar, click Mapped.

Distribution I

- I Right-click Mapped I and choose Distribution.
- **2** Select Boundary 1 only.
- **3** In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 20.

Distribution 2

I In the Model Builder window, right-click Mapped I and choose Distribution.

- 2 Select Boundary 4 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 100.
- 5 Click 📗 Build All.

STUDY I

Now the flow field and the temperature distribution within the glacier is calculated. Start with a stationary velocity field, first. Therefore, a stationary study step is introduced.

Stationary

- I In the Study toolbar, click 🔁 Study Steps and choose Stationary>Stationary.
- 2 Right-click Study I>Step 2: Stationary and choose Move Up.
- 3 In the Settings window for Stationary, locate the Physics and Variables Selection section.
- 4 In the table, clear the Solve for check box for Heat Transfer in Fluids (ht).
- 5 Select the Modify model configuration for study step check box.
- 6 In the tree, select Component I (Compl)>Creeping Flow (Spf)>Wall 2.
- 7 Right-click and choose **Disable** to deactivate the slip boundary condition which is only needed for the temperate glacier simulation.
- 8 Right-click Study I>Step 2: Stationary and choose Compute Selected Step.

STUDY I

The next step is to start the time-dependent fully coupled simulation. To catch seasonal variations, force the time-step to be small enough.

Step 2: Time Dependent

- I In the Model Builder window, expand the Study I>Solver Configurations node, then click Study I>Step 2: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- **3** From the **Time unit** list, choose **a**.
- **4** In the **Output times** text field, type range(0,0.1,10).
- 5 Locate the Physics and Variables Selection section. Select theModify model configuration for study step check box to deactivate the boundary conditions that are not needed for the cold glacier simulation.
- 6 In the tree, select Component I (Compl)>Creeping Flow (Spf)>Wall 2.
- 7 Right-click and choose **Disable**.
- 8 In the tree, select Component I (Compl)>Heat Transfer in Fluids (Ht)>Temperature I.

9 Right-click and choose Disable.

Solution 1 (soll)

I In the Study toolbar, click **The Show Default Solver**.

Surface plots of velocity, pressure, and temperature are created automatically. As an example for an additional plot, the outward mass flow rate, averaged over the glacier surface and the lower end of the glacier are plotted here as follows.

- 2 In the Model Builder window, expand the Solution I (soll) node, then click Time-Dependent Solver I.
- **3** In the **Settings** window for **Time-Dependent Solver**, click to expand the **Time Stepping** section.
- 4 From the Steps taken by solver list, choose Strict.

Step 2: Time Dependent

In the Model Builder window, under Study I right-click Step 2: Time Dependent and choose Compute Selected Step.

RESULTS

Surface

- I In the Model Builder window, expand the Velocity (spf) node, then click Surface.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the **Unit** field, type m/yr.
- 4 In the Velocity (spf) toolbar, click 💿 Plot.

Line Average 1

- I In the Results toolbar, click ^{8.85}_{e-12} More Derived Values and choose Average>Line Average.
- **2** Select Boundaries 1, 2, and 4 only.
- 3 In the Settings window for Line Average, click Replace Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (compl)> Creeping Flow>Auxiliary variables>spf.openl.massFlowRate Outward mass flow rate across feature selection kg/s.
- 4 Click **= Evaluate**.

TABLE

- I Go to the Table window.
- 2 Click Table Graph in the window toolbar.

RESULTS

Outward Mass Flow Rate

- I In the Model Builder window, under Results click ID Plot Group 5.
- 2 In the Settings window for ID Plot Group, type Outward Mass Flow Rate in the Label text field.

Temperate Glacier

ROOT

So far, we have modeled an example of a cold glacier. Now add a second study and modify the boundary conditions to match the conditions for a temperate glacier. Start again with a stationary velocity field.

ADD STUDY

- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies> Time Dependent.
- 4 Right-click and choose Add Study.
- 5 In the Home toolbar, click $\stackrel{\sim}{\sim}_1$ Add Study to close the Add Study window.

STUDY 2

Step 1: Time Dependent

- I In the Settings window for Time Dependent, locate the Study Settings section.
- 2 From the Time unit list, choose a.
- 3 In the **Output times** text field, type range(0,0.1,10).

Stationary

- I In the Study toolbar, click 🔁 Study Steps and choose Stationary>Stationary.
- 2 Right-click Study 2>Step 2: Stationary and choose Move Up.
- 3 In the Settings window for Stationary, locate the Physics and Variables Selection section.
- 4 In the table, clear the Solve for check box for Heat Transfer in Fluids (ht).

Step 2: Time Dependent

I In the Model Builder window, click Step 2: Time Dependent.

- 2 In the Settings window for Time Dependent, locate the Physics and Variables Selection section.
- **3** Select the **Modify model configuration for study step** check box.
- 4 In the tree, select Component I (Compl)>Heat Transfer in Fluids (Ht)>Heat Flux I.
- **5** Click **O Disable** to deactivate the heat flux boundary condition that is only needed for the cold glacier simulation, not the temperate glacier simulation.

Solution 3 (sol3)

- I In the Study toolbar, click The Show Default Solver.
- 2 In the Model Builder window, expand the Solution 3 (sol3) node, then click Time-Dependent Solver I.
- 3 In the Settings window for Time-Dependent Solver, locate the Time Stepping section.
- 4 From the Steps taken by solver list, choose Strict.

Step 1: Stationary

In the Model Builder window, under Study 2 right-click Step 1: Stationary and choose Compute Selected Step.

Step 2: Time Dependent

In the Model Builder window, under Study 2 right-click Step 2: Time Dependent and choose Compute Selected Step.

RESULTS

Surface

Again, velocity, pressure, and temperature are plotted by default. Change the default unit of the velocity magnitude to (m/yr).

- I In the Model Builder window, expand the Velocity (spf) I node, then click Surface.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the **Unit** field, type m/yr.
- 4 In the Velocity (spf) I toolbar, click 💿 Plot.
- **5** Click to expand the **Range** section.

Temperature (ht) 1

The plots of the "cold glacier" scenario and the "temperate glacier" scenario can each be grouped together.

I In the Model Builder window, expand the Results>Datasets node.

Isothermal Contours (ht), Outward Mass Flow Rate, Pressure (spf), Temperature (ht), Velocity (spf)

- I In the Model Builder window, under Results, Ctrl-click to select Velocity (spf), Pressure (spf), Temperature (ht), Isothermal Contours (ht), and Outward Mass Flow Rate.
- 2 Right-click and choose Group.

Cold Glacier

In the Settings window for Group, type Cold Glacier in the Label text field.

Isothermal Contours (ht) I, Outward Mass Flow Rate I, Pressure (spf) I, Temperature (ht) I, Velocity (spf) I

- In the Model Builder window, under Results, Ctrl-click to select Velocity (spf) I, Pressure (spf) I, Temperature (ht) I, Isothermal Contours (ht) I, and Outward Mass Flow Rate I.
- 2 Right-click and choose Group.

Temperate Glacier

In the Settings window for Group, type Temperate Glacier in the Label text field.

ID Plot Group 12

To compare the tangential velocities along the glacier surface as displayed in Figure 8, follow the steps below.

In the Home toolbar, click 🚛 Add Plot Group and choose ID Plot Group.

Line Graph I

- I Right-click ID Plot Group 12 and choose Line Graph.
- **2** Select Boundary 4 only.
- 3 In the Settings window for Line Graph, locate the y-Axis Data section.
- **4** In the **Expression** text field, type u*tx+v*ty.
- 5 In the **Unit** field, type m/yr.
- 6 Click to expand the Legends section. Select the Show legends check box.
- 7 From the Legends list, choose Manual.
- **8** In the table, enter the following settings:

Legends

Cold glacier

ID Plot Group 12

I In the Model Builder window, click ID Plot Group 12.

- 2 In the Settings window for ID Plot Group, locate the Data section.
- **3** From the **Time selection** list, choose **Last**.

Line Graph 2

- I Right-click ID Plot Group 12 and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the Data section.
- **3** From the **Dataset** list, choose **Study 2/Solution 3 (sol3)**.
- **4** From the **Time selection** list, choose **Last**.
- **5** Select Boundary 4 only.
- 6 Locate the y-Axis Data section. In the Expression text field, type u*tx+v*ty.
- 7 In the **Unit** field, type m/yr.
- 8 Locate the Legends section. Select the Show legends check box.
- 9 From the Legends list, choose Manual.
- **IO** In the table, enter the following settings:

Legends

Temperate glacier

Tangential Velocity along Glacier Surface

- I In the Model Builder window, under Results click ID Plot Group 12.
- 2 In the Settings window for ID Plot Group, type Tangential Velocity along Glacier Surface in the Label text field.
- 3 In the Tangential Velocity along Glacier Surface toolbar, click 💽 Plot.
- 4 Locate the Plot Settings section. Select the x-axis label check box.
- **5** In the associated text field, type Surface length (m).
- 6 Select the **y-axis label** check box.
- 7 In the associated text field, type Tangential velocity (m/yr).

Line Graph 2

- I In the Model Builder window, click Line Graph 2.
- 2 In the Settings window for Line Graph, click to expand the Title section.
- **3** From the **Title type** list, choose **None**.

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