

Polarized Circular Ports

Introduction

This example of a circular waveguide demonstrates how to excite and terminate ports with degenerate port modes. In particular it shows how to model and excite the TE11 mode of circular waveguides in 3D.

Model Definition

A straight piece of circular waveguide with perfect metallic walls is excited by a linearly polarized TE_{11} mode at one end and ideally terminated at the other end.

The TE₁₁ mode of a circular waveguide is degenerate, meaning that there is an infinite number of possible variants of the TE₁₁ mode that only differ in polarization. Any type of polarization (for example circular polarization) of the TE₁₁ mode can be constructed by or decomposed into two linearly polarized modes. The direction of polarization of the first one can be chosen freely and the second one is obtained from the first one by a rotation of 90 degrees around the waveguide axis.

As a general structure may change the polarization of the incident field as it is transmitted or reflected, ideal termination means that any circular waveguide port that operates in the TE_{11} mode need to have two port features which are tuned to mutually orthogonal, linear polarizations of the TE_{11} mode respectively. The reference directions for the two port features are subject to a manual choice but must differ by a rotation of 90 degrees around the waveguide axis.

The Port subfeature, Circular Port Reference Axis is used to determine the reference direction for the polarization of each mode/port by means of selecting two vertices (points) on the port circumference. In this example, extra vertices that are equally distributed along the port edge are added to the geometry to allow for the definition of the desired reference directions.

With the stipulated excitation using the two mutually orthogonal TE_{11} ports as boundary conditions, the following equation is solved for the electric field vector **E** inside the waveguide:

$$\nabla \times (\mu_{\rm r}^{-1} \nabla \times \mathbf{E}) - k_0^2 \left(\varepsilon_{\rm r} - \frac{j\sigma}{\omega \varepsilon_0} \right) \mathbf{E} = 0$$



The first TE_{11} mode of the inport is shown in Figure 1.

Figure 1: The first TE_{11} mode of the inport

Note: Depending on the details of the mesh, which in turn may depend on the origin of the CAD geometry, a mode that is rotated 180 degrees may be found.



The first TE_{11} mode of the outport is shown in Figure 2.

Figure 2: The first TE_{11} mode of the outport.

Note: Depending on the details of the mesh, which in turn may depend on the origin of the CAD geometry, a mode that is rotated 180 degrees may be found.



The transmission coefficients between the inport and outport modes are shown in Figure 3.

Figure 3: The transmission coefficients between inport modes and outport modes are plotted as a function of frequency. As the port modes are misaligned by 45 degrees the transmission coefficients approach the -3dB level.

Application Library path: RF_Module/Tutorials/polarized_circular_ports

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click 🔗 Model Wizard.

MODEL WIZARD

I In the Model Wizard window, click 间 3D.

- 2 In the Select Physics tree, select Radio Frequency>Electromagnetic Waves, Frequency Domain (emw).
- 3 Click Add.
- 4 Click \bigcirc Study.
- 5 In the Select Study tree, select General Studies>Frequency Domain.
- 6 Click 🗹 Done.

GLOBAL DEFINITIONS

Add a parameter for the operating frequency.

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.

3 In the table, enter the following settings:

Name	Expression	Value	Description
frq	c_const/0.03[m]	9.9931E9 1/s	Operating frequency

STUDY I

Step 1: Frequency Domain

- I In the Model Builder window, under Study I click Step I: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- 3 In the Frequencies text field, type range(0.9*frq,(1.5*frq-(0.9*frq))/10,1.5* frq).

GEOMETRY I

The geometry is essentially a cylinder.

Cylinder I (cyl1)

- I In the **Geometry** toolbar, click **D** Cylinder.
- 2 In the Settings window for Cylinder, locate the Size and Shape section.
- 3 In the Radius text field, type 0.01.
- 4 In the **Height** text field, type 0.1.

5 Click 틤 Build Selected.



6 Click the 🔁 Wireframe Rendering button in the Graphics toolbar.

You need to add a reference direction for the port polarization. Add a couple of lines on the cylinder end to generate extra vertices. This is done in a work plane.

Work Plane I (wp1)

- I In the Geometry toolbar, click 📥 Work Plane.
- 2 In the Settings window for Work Plane, locate the Plane Definition section.
- **3** In the **z-coordinate** text field, type **0.1**.

Work Plane I (wpI)>Plane Geometry

In the Model Builder window, click Plane Geometry.

Work Plane I (wp1)>Line Segment I (ls1)

- I In the Work Plane toolbar, click 🚧 More Primitives and choose Line Segment.
- 2 In the Settings window for Line Segment, locate the Starting Point section.
- 3 From the Specify list, choose Coordinates.
- 4 Locate the Endpoint section. From the Specify list, choose Coordinates.
- 5 Locate the Starting Point section. In the yw text field, type 0.01.
- 6 Locate the Endpoint section. In the yw text field, type -0.01.

Work Plane I (wp1)>Rotate I (rot1)

I In the Work Plane toolbar, click 💭 Transforms and choose Rotate.

- 2 Select the object IsI only.
- 3 In the Settings window for Rotate, locate the Rotation section.
- 4 In the Angle text field, type 45 135.



5 Click 틤 Build Selected.

Ignore Edges 1 (ige1)

I In the Model Builder window, right-click Geometry I and choose Virtual Operations> Ignore Edges.

2 On the object fin, select Edges 7, 8, 13, and 14 only.



- 3 In the Settings window for Ignore Edges, locate the Input section.
- 4 Clear the **Ignore adjacent vertices** check box.
- 5 In the Geometry toolbar, click 📗 Build All.

MATERIALS

Next, add a material for the interior (air) of the waveguide.

Material I (mat1)

- I In the Model Builder window, under Component I (compl) right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, locate the Material Contents section.

3 In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Relative permittivity	epsilonr_iso; epsilonrii = epsilonr_iso, epsilonrij = 0	1	I	Basic
Relative permeability	mur_iso ; murii = mur_iso, murij = 0	1	1	Basic
Electrical conductivity	sigma_iso ; sigmaii = sigma_iso, sigmaij = 0	0	S/m	Basic

ELECTROMAGNETIC WAVES, FREQUENCY DOMAIN (EMW)

Set up one inport and three outports.

Port I

- I In the Model Builder window, under Component I (compl) right-click Electromagnetic Waves, Frequency Domain (emw) and choose Port.
- 2 Select Boundary 3 only.

It might be easier to select the correct boundary by using the **Selection List** window. To open this window, in the **Home** toolbar click **Windows** and choose **Selection List**. (If you are running the cross-platform desktop, you find **Windows** in the main menu.)

- 3 In the Settings window for Port, locate the Port Properties section.
- **4** From the **Type of port** list, choose **Circular**.

Circular Port Reference Axis 1

- I In the Physics toolbar, click 📃 Attributes and choose Circular Port Reference Axis.
- 2 In the Settings window for Circular Port Reference Axis, locate the Point Selection section.
- 3 Click Clear Selection.

4 Select Points 5 and 8 only.



Port 2

- I In the Physics toolbar, click 🔚 Boundaries and choose Port.
- **2** Select Boundary **3** only.
- 3 In the Settings window for Port, locate the Port Properties section.
- 4 From the Type of port list, choose Circular.

Circular Port Reference Axis I

- I In the Physics toolbar, click 层 Attributes and choose Circular Port Reference Axis.
- 2 In the Settings window for Circular Port Reference Axis, locate the Point Selection section.
- 3 Click Telear Selection.

4 Select Points 1 and 12 only.



Port 3

- I In the Physics toolbar, click 🔚 Boundaries and choose Port.
- **2** Select Boundary 4 only.
- 3 In the Settings window for Port, locate the Port Properties section.
- **4** From the **Type of port** list, choose **Circular**.

Circular Port Reference Axis I

- I In the Physics toolbar, click 层 Attributes and choose Circular Port Reference Axis.
- 2 In the Settings window for Circular Port Reference Axis, locate the Point Selection section.
- 3 Click Telear Selection.

4 Select Points 4 and 10 only.



Port 4

- I In the Physics toolbar, click 🔚 Boundaries and choose Port.
- **2** Select Boundary 4 only.
- 3 In the Settings window for Port, locate the Port Properties section.
- **4** From the **Type of port** list, choose **Circular**.

Circular Port Reference Axis I

- I In the Physics toolbar, click 层 Attributes and choose Circular Port Reference Axis.
- 2 In the Settings window for Circular Port Reference Axis, locate the Point Selection section.
- 3 Click Clear Selection.

4 Select Points **3** and **11** only.



y z x

MESH I

In the Model Builder window, under Component I (compl) right-click Mesh I and choose Build All.





STUDY I

Step 1: Frequency Domain In the Home toolbar, click **= Compute**.

RESULTS

Electric Field (emw)

Inspect the electric field norm.



Next, inspect the S-parameters representing transmission.

S-parameter (emw)

As expected, the transmitted energy is evenly divided between the outport modes (Figure 3).

Smith Plot (emw)



Port I

- I In the Home toolbar, click 🚛 Add Plot Group and choose 3D Plot Group.
- 2 In the Settings window for 3D Plot Group, type Port 1 in the Label text field.

Surface 1

- I Right-click Port I and choose Surface.
- In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>
 Electromagnetic Waves, Frequency Domain>Ports>emw.normtEmode_I Port tangential electric mode field norm V/m.

- I In the Model Builder window, right-click Port I and choose Arrow Surface.
- 2 In the Settings window for Arrow Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)> Electromagnetic Waves, Frequency Domain>Ports>emw.tEmodex_l,...,emw.tEmodez_l Port tangential electric mode field.
- 3 Locate the Arrow Positioning section. In the Number of arrows text field, type 1000.
- 4 Locate the Coloring and Style section. From the Color list, choose Black.

- 5 In the Port I toolbar, click **Plot**.
- 6 Click 🗿 Plot.

freq(11)=14.99 GHz



Port 2

- I Right-click Port I and choose Duplicate.
- 2 In the Settings window for 3D Plot Group, type Port 2 in the Label text field.

Surface 1

- I In the Model Builder window, expand the Port 2 node, then click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the **Expression** text field, type emw.normtEmode 2.

- I In the Model Builder window, click Arrow Surface I.
- 2 In the Settings window for Arrow Surface, locate the Expression section.
- 3 In the X component text field, type emw.tEmodex_2.
- 4 In the **Y** component text field, type emw.tEmodey 2.
- 5 In the **Z** component text field, type emw.tEmodez_2.

6 In the Port 2 toolbar, click 🗿 Plot.



Port 3

- I In the Model Builder window, right-click Port 2 and choose Duplicate.
- 2 In the Settings window for 3D Plot Group, type Port 3 in the Label text field.

Surface 1

- I In the Model Builder window, expand the Port 3 node, then click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type emw.normtEmode_3.

- I In the Model Builder window, click Arrow Surface I.
- 2 In the Settings window for Arrow Surface, locate the Expression section.
- 3 In the X component text field, type emw.tEmodex_3.
- 4 In the Y component text field, type emw.tEmodey_3.
- 5 In the **Z** component text field, type emw.tEmodez_3.

freq(11)=14.99 GHz Surface: Port tangential electric mode field norm (V/m) Arrow Surface: Port tangential electric mode field ×10⁻³ m 105 $\times 10^{3}$ -5 0.1 2 1.5 0.05 m 1 0.5 5 -10

6 In the Port 3 toolbar, click **Plot**.

Port 4

- I In the Model Builder window, right-click Port 3 and choose Duplicate.
- 2 In the Settings window for 3D Plot Group, type Port 4 in the Label text field.

Surface 1

- I In the Model Builder window, expand the Port 4 node, then click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the **Expression** text field, type emw.normtEmode_4.

- I In the Model Builder window, click Arrow Surface I.
- 2 In the Settings window for Arrow Surface, locate the Expression section.
- 3 In the X component text field, type emw.tEmodex_4.
- 4 In the Y component text field, type emw.tEmodey_4.
- 5 In the **Z** component text field, type emw.tEmodez_4.

6 In the Port 4 toolbar, click 💿 Plot.



Next, display numerical values for the transmission at the highest frequency.

Global Evaluation 1

- I In the **Results** toolbar, click (8.5) **Global Evaluation**.
- 2 In the Settings window for Global Evaluation, locate the Data section.
- **3** From the **Parameter selection (freq)** list, choose **Last**.
- 4 Click Replace Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (compl)>Electromagnetic Waves, Frequency Domain>Ports> S-parameter, dB>emw.S31dB S31.
- 5 Click **=** Evaluate.

Global Evaluation 2

- I In the Results toolbar, click (8.5) Global Evaluation.
- 2 In the Settings window for Global Evaluation, locate the Data section.
- 3 From the Parameter selection (freq) list, choose Last.
- 4 Click Replace Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (compl)>Electromagnetic Waves, Frequency Domain>Ports> S-parameter, dB>emw.S41dB S41.

5 Click **= Evaluate**.

As expected, the result is about -3 dB for both modes.