

# Cascaded Rectangular Cavity Filter

# Introduction

A cascaded cavity filter provides much better bandpass filter performance compared to a single cavity filter. Here, three rectangular cavity filters are coupled via slots and provide excellent out-of-band rejection.



Figure 1: A cascaded rectangular cavity filter consisting of three cavities, coupling slots, and microstrip lines feeds.

# Model Definition

The resonant frequencies of a rectangular cavity are given by

$$f_{nml} = \frac{c}{2\pi \sqrt{\varepsilon_{\rm r} \mu_{\rm r}}} \sqrt{\left(\frac{m\pi}{a}\right)^2 + \left(\frac{n\pi}{b}\right)^2 + \left(\frac{l\pi}{d}\right)^2}$$

where *a* and *b* are the dimension of the aperture of a waveguide and *d* is the length of the waveguide cavity. The size of a single cavity used in this example is 50 mm, 50 mm, 100 mm in depth, height, and width, respectively. The resonant frequency at the dominant mode  $TE_{101}$  is 3.354 GHz. In this example, three such cavities are coupled through slots. The dimensions and locations of the slots can be adjusted to improve input matching properties as well as power transfer between in and output ports. Two shorted microstrip

lines, fed by a lumped port, couple into the first and last cavities of the structure. The air box around the microstrip lines is enclosed by metallic walls, representing the packaging.

# Results and Discussion

Solving the model over a range of frequencies reveals that the resonant frequency of the cascaded filter is 3.354 GHz, as expected. The out-of-band rejection at  $\pm 90$  MHz is better than -60 dB.



Figure 2: A plot of the electric field shows the dominant  $TE_{101}$  mode in each cavity.



Figure 3: Frequency response of the cascaded rectangular cavity filter shows good bandpass characteristics.

# Notes About the COMSOL Implementation

This example also uses the Frequency Domain Modal study step combined with an Eigenfrequency analysis to evaluate the frequency response of the filter circuit. This approach is faster than a regular frequency sweep performed in a Frequency Domain study, but its usage is limited to only high-Q devices or circuits presenting bandpass frequency properties excited by lumped ports. Since an Eigenfrequency analysis is computationally intensive, it may require more than 8 GB of RAM.

# Reference

1. D.M. Pozar, Microwave Engineering, John Wiley & Sons, 1998.

Application Library path: RF\_Module/Filters/cascaded\_cavity\_filter

# Modeling Instructions

From the File menu, choose New.

## NEW

In the New window, click 🔗 Model Wizard.

## MODEL WIZARD

- I In the Model Wizard window, click 间 3D.
- 2 In the Select Physics tree, select Radio Frequency>Electromagnetic Waves, Frequency Domain (emw).
- 3 Click Add.
- 4 Click 🔿 Study.
- 5 In the Select Study tree, select General Studies>Frequency Domain.
- 6 Click **M** Done.

## STUDY I

## Step 1: Frequency Domain

- I In the Model Builder window, under Study I click Step I: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- 3 In the Frequencies text field, type range(3.3[GHz],2.5[MHz],3.38[GHz]).

## **GLOBAL DEFINITIONS**

## Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click 📂 Load from File.
- **4** Browse to the model's Application Libraries folder and double-click the file cascaded\_cavity\_filter\_parameters.txt.

Here mil refers to the unit milliinch, that is 1 mil = 0.0254 mm.

## GEOMETRY I

- I In the Model Builder window, under Component I (compl) click Geometry I.
- 2 In the Settings window for Geometry, locate the Units section.
- 3 From the Length unit list, choose mm.

Create a cavity at the input port.

## Cavity I

- I In the **Geometry** toolbar, click 🗍 Block.
- 2 In the Settings window for Block, type Cavity1 in the Label text field.
- 3 Locate the Size and Shape section. In the Width text field, type w\_cavity.
- 4 In the **Depth** text field, type d\_cavity.
- 5 In the **Height** text field, type d\_cavity.
- 6 Locate the Position section. From the Base list, choose Center.
- 7 In the x text field, type -w\_cavity/2-w\_cavity/8.
- 8 In the z text field, type d\_cavity.
- 9 Click 틤 Build Selected.

Create a substrate at the input port.

#### Substrate

- I In the **Geometry** toolbar, click 🗍 Block.
- 2 In the Settings window for Block, type Substrate in the Label text field.
- 3 Locate the Size and Shape section. In the Width text field, type w\_cavity/3.
- 4 In the **Depth** text field, type d\_cavity.
- **5** In the **Height** text field, type d.
- 6 Locate the Position section. In the x text field, type -w\_cavity-w\_cavity/8.
- 7 In the y text field, type -w\_cavity/4.
- 8 In the z text field, type d\_cavity\*1.5.
- 9 Click 틤 Build Selected.

Create a microstrip line at the input port.

## Feed

- I In the **Geometry** toolbar, click **[]** Block.
- 2 In the Settings window for Block, type Feed in the Label text field.
- 3 Locate the Size and Shape section. In the Width text field, type l\_feed+w\_slot.
- 4 In the **Depth** text field, type **3.2**[mm].
- 5 In the Height text field, type d.
- 6 Locate the Position section. From the Base list, choose Center.
- 7 In the x text field, type -w\_cavity/2-w\_cavity/8-x\_slot-1\_feed/2.

#### 6 | CASCADED RECTANGULAR CAVITY FILTER

- 8 In the z text field, type d\_cavity\*1.5+d/2.
- 9 Click 틤 Build Selected.

To see the interior, you can choose wireframe rendering:

**IO** Click the **Wireframe Rendering** button in the **Graphics** toolbar.

Create a box enclosing the input port.

## FeedBoxBlock

- I In the **Geometry** toolbar, click 🗍 **Block**.
- 2 In the Settings window for Block, type FeedBoxBlock in the Label text field.
- 3 Locate the Size and Shape section. In the Width text field, type w\_cavity/3.
- 4 In the **Depth** text field, type d\_cavity.
- 5 In the Height text field, type h\_feed.
- 6 Locate the Position section. From the Base list, choose Center.
- 7 In the x text field, type -w\_cavity-w\_cavity/8+w\_cavity/6.
- 8 In the z text field, type d\_cavity\*1.5+h\_feed/2.
- 9 Click 틤 Build Selected.

Create coupling slots between the cavities.

## Work Plane I (wp1)

- I In the Geometry toolbar, click <del>·</del> Work Plane.
- 2 In the Settings window for Work Plane, locate the Plane Definition section.
- **3** In the **z-coordinate** text field, type 25[mm].
- 4 Click 📥 Show Work Plane.

Work Plane I (wp1)>Rectangle I (r1)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- **3** In the **Width** text field, type **3.5**[mm].
- 4 In the **Height** text field, type 26.4[mm].
- 5 Locate the Position section. From the Base list, choose Center.
- 6 In the xw text field, type -28.5[mm].
- 7 Click 📄 Build Selected.

Create coupling slots between the microstrip line feed and the cavity linked to the feed as well.

## Work Plane 2 (wp2)

- I In the Model Builder window, right-click Geometry I and choose Work Plane.
- 2 In the Settings window for Work Plane, locate the Plane Definition section.
- 3 In the **z-coordinate** text field, type 75[mm].
- 4 Click 📥 Show Work Plane.

# Work Plane 2 (wp2)>Rectangle 1 (r1)

- I In the Work Plane toolbar, click 📃 Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- **3** In the **Width** text field, type w\_slot.
- 4 In the **Height** text field, type 45[mm].
- 5 Locate the Position section. From the Base list, choose Center.
- 6 In the xw text field, type -w\_cavity/2-w\_cavity/8-x\_slot.
- 7 Right-click Geometry I and choose Build All.



Generate the second cavity by mirroring the first one.

## Mirror I (mirl)

- I In the **Geometry** toolbar, click 💭 **Transforms** and choose **Mirror**.
- 2 Click in the Graphics window and then press Ctrl+A to select all objects.
- 3 In the Settings window for Mirror, locate the Normal Vector to Plane of Reflection section.

- 4 In the **x** text field, type 1.
- **5** In the **z** text field, type **0**.
- 6 Locate the Input section. Select the Keep input objects check box.
- 7 Click 🟢 Build All Objects.
- 8 Click the |+| Zoom Extents button in the Graphics toolbar.

Cavity I.1 (blk5)

- I In the Model Builder window, under Component I (compl)>Geometry I right-click Cavity1 (blk1) and choose Duplicate.
- 2 In the Settings window for Block, locate the Position section.
- **3** In the **x** text field, type **0**.
- **4** In the **z** text field, type **0**.
- 5 Click 🟢 Build All Objects.



## ELECTROMAGNETIC WAVES, FREQUENCY DOMAIN (EMW)

The default boundary condition is perfect electric conductor, which is applied to all exterior boundaries. Assign perfect electric conductor to interior boundaries on the cavity walls and microstrip lines.

## Perfect Electric Conductor 2

- I In the Model Builder window, under Component I (comp1) right-click Electromagnetic Waves, Frequency Domain (emw) and choose Perfect Electric Conductor.
- **2** Select Boundaries 6, 16, 17, 22, 29, 36, 44, 52, 55, and 58 only.



Assign a lumped port with port excitation at the end of one microstrip line.

## Lumped Port I

- I In the Physics toolbar, click 🔚 Boundaries and choose Lumped Port.
- 2 Select Boundary 14 only.

For the first port, wave excitation is **on** by default.

Assign a lumped port at the end of the other microstrip line.

#### Lumped Port 2

- I In the Physics toolbar, click 📄 Boundaries and choose Lumped Port.
- 2 Select Boundary 59 only.

## ADD MATERIAL

- I In the Home toolbar, click 🙀 Add Material to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Built-in>Air.
- 4 Click Add to Component in the window toolbar.

5 In the Home toolbar, click 🙀 Add Material to close the Add Material window.

# MATERIALS

Create a dielectric material for the substrates.

Material 2 (mat2)

- I In the Model Builder window, under Component I (compl) right-click Materials and choose Blank Material.
- 2 Select Domains 2, 4, 7, and 9 only.



- 3 In the Settings window for Material, locate the Material Contents section.
- **4** In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Relative permittivity	epsilonr_iso ; epsilonrii = epsilonr_iso, epsilonrij = 0	3.38	I	Basic

Property	Variable	Value	Unit	Property group
Relative permeability	mur_iso ; murii = mur_iso, murij = 0	1	1	Basic
Electrical conductivity	sigma_iso ; sigmaii = sigma_iso, sigmaij = 0	0	S/m	Basic

# MESH I

- I In the Model Builder window, under Component I (comp1) click Mesh I.
- 2 In the Settings window for Mesh, locate the Physics-Controlled Mesh section.
- **3** From the **Element size** list, choose **Fine**.
- 4 Click 📗 Build All.



**STUDY I** In the **Home** toolbar, click **= Compute**.

## RESULTS

## Electric Field (emw)

The default plot shows the norm of the electric field for the highest frequency. Follow the instructions to reproduce Figure 2.

- I In the Settings window for 3D Plot Group, locate the Data section.
- 2 From the Parameter value (freq (GHz)) list, choose 3.34.

#### Multislice

- I In the Model Builder window, expand the Electric Field (emw) node, then click Multislice.
- 2 In the Settings window for Multislice, locate the Multiplane Data section.
- 3 Find the X-planes subsection. In the Planes text field, type 0.
- 4 Find the Z-planes subsection. From the Entry method list, choose Coordinates.
- 5 In the **Coordinates** text field, type -d\_cavity/2+0.1,d\_cavity/2+0.1,d\_cavity/2\* 3-0.1.
- 6 Click to expand the Range section. Select the Manual color range check box.
- 7 In the Maximum text field, type 800.
- 8 In the Electric Field (emw) toolbar, click 💿 Plot.

#### S-parameter (emw)

- I In the Model Builder window, under Results click S-parameter (emw).
- 2 In the Settings window for ID Plot Group, locate the Legend section.



**3** From the **Position** list, choose **Lower right**.

# Smith Plot (emw)



# 3D Plot Group 4

- I In the Home toolbar, click 🚛 Add Plot Group and choose 3D Plot Group.
- 2 In the Settings window for 3D Plot Group, locate the Data section.
- 3 From the Parameter value (freq (GHz)) list, choose 3.34.

## Isosurface I

- I Right-click **3D Plot Group 4** and choose Isosurface.
- 2 In the Settings window for Isosurface, locate the Levels section.
- 3 In the Total levels text field, type 20.
- 4 Locate the Coloring and Style section. From the Color table list, choose AuroraBorealis.

#### Filter I

- I Right-click Isosurface I and choose Filter.
- 2 In the Settings window for Filter, locate the Element Selection section.
- **3** In the Logical expression for inclusion text field, type y>0.

## 4 In the **3D Plot Group 4** toolbar, click **I** Plot.



Analyze the same model with a Frequency Domain Modal method. When a device presents resonances, the Frequency Domain Modal method combined with an Eigenfrequency analysis provides a faster solution time.

## ELECTROMAGNETIC WAVES, FREQUENCY DOMAIN (EMW)

Lumped Port I

- In the Model Builder window, under Component I (compl)>Electromagnetic Waves, Frequency Domain (emw) click Lumped Port I.
- 2 In the Settings window for Lumped Port, locate the Boundary Selection section.
- 3 Click here are a create Selection.
- 4 In the **Create Selection** dialog box, Create a set of selections for use in the study settings.
- 5 type Lumped port 1 in the Selection name text field.
- 6 Click OK.

Lumped Port 2

- I In the Model Builder window, click Lumped Port 2.
- 2 In the Settings window for Lumped Port, locate the Boundary Selection section.

# 3 Click har Create Selection.

4 In the Create Selection dialog box, type Lumped port 2 in the Selection name text field.

5 Click OK.

#### ADD STUDY

- I In the Home toolbar, click  $\sim$  Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- **3** Find the **Studies** subsection. In the **Select Study** tree, select

# Preset Studies for Selected Physics Interfaces>Frequency Domain, Modal.

- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

## STUDY 2

#### Step 1: Eigenfrequency

- I In the Settings window for Eigenfrequency, locate the Study Settings section.
- 2 In the Search for eigenfrequencies around text field, type 3.3[GHz].

## Step 2: Frequency Domain, Modal

- I In the Model Builder window, click Step 2: Frequency Domain, Modal.
- 2 In the Settings window for Frequency Domain, Modal, locate the Study Settings section.
- 3 In the Frequencies text field, type range(3.3[GHz],2.5[MHz]/50,3.38[GHz]).

With a 50 times finer frequency step, the solutions will increase the file size tremendously when it is saved. When only S-parameters are of interest, a common theme in most passive RF and microwave device designs, it is not necessary to store all of the field solutions. By selecting the **Store fields in output** check box in the **Values of Dependent Variables** section, we can control the part of the model on which the computed solution is saved. We only add the selection containing these boundaries where the S-parameters are calculated. The lumped port size is typically very small compared to the entire modeling domain, and the saved file size with the finer frequency step is more or less that of the regular discrete frequency sweep model when only the solutions on the port boundaries are stored.

- **4** Click to expand the **Values of Dependent Variables** section. Find the **Store fields in output** subsection. From the **Settings** list, choose **For selections**.
- **5** Under **Selections**, click + **Add**.
- 6 In the Add dialog box, in the Selections list, choose Lumped port I and Lumped port 2.

7 Click OK.

8 In the **Home** toolbar, click **= Compute**.

## RESULTS

## Electric Field (emw) 1

Since the results are stored only on the lumped port boundaries, this default E-field norm plot does not provide useful information.

## I Right-click Results>Electric Field (emw) I and choose Delete.

Generate all S-parameters from each analysis on the same plot and compare them to each other.

S-parameter (emw) I

- I In the Model Builder window, under Results click S-parameter (emw) I.
- 2 In the Settings window for ID Plot Group, click to expand the Title section.
- 3 From the Title type list, choose Manual.
- **4** In the **Title** text area, type S-parameter Comparison between Frequency Domain Modal and Discrete Sweep.
- 5 Locate the Legend section. From the Position list, choose Lower right.

## Global 2

- I In the Model Builder window, expand the S-parameter (emw) I node.
- 2 Right-click Results>S-parameter (emw) I>Global I and choose Duplicate.
- 3 In the Settings window for Global, locate the Data section.
- 4 From the Dataset list, choose Study I/Solution I (soll).
- 5 Click to expand the Coloring and Style section. Find the Line style subsection. From the Line list, choose Dotted.
- 6 Find the Line markers subsection. From the Marker list, choose Cycle.
- 7 From the Positioning list, choose In data points.

## Global I

- I In the Model Builder window, click Global I.
- 2 In the Settings window for Global, locate the y-Axis Data section.

**3** In the table, enter the following settings:

Expression	Unit	Description
emw.S11dB	1	S11, FD Modal
emw.S21dB	1	S21, FD Modal

4 In the S-parameter (emw) I toolbar, click 💿 Plot.

See Figure 3 for S-parameter plot.

Smith Plot (emw) I



Compare the solution time between two studies.

# 20 | CASCADED RECTANGULAR CAVITY FILTER