

Shape Memory Alloy Self-Expanding Stent

This model studies an arterial stent made of shape memory alloy (SMA). The main benefit of SMA stents compared to usual metallic stents is their ability to self-expand, so they do not require the insertion and inflation of a balloon to give them the desired shape.

The SMA stent is manufactured with a diameter higher than the diameter of the destination artery. It is then crimped to the diameter of the artery at low temperature. Due to the low operating temperature, the material partially transforms from austenite to martensite at low stress levels. When the stent is inserted in the artery, its temperature increases to the human body temperature. Then the yield stress increases so the force applied by the stent on the inner wall of the artery increases.

Model Definition

The stent is made of 4 levels of SMA wire. Each level is made of 18 "V" sections (Figure 1). Thanks to symmetry and periodicity, only half of a "V" is modeled; that is, a 10 degrees sector (Figure 2).

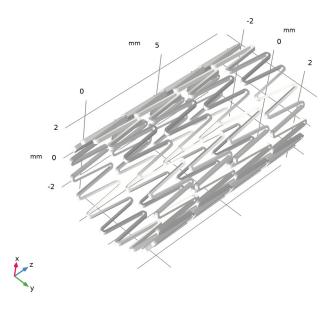


Figure 1: Entire geometry of the stent

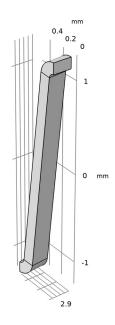




Figure 2: Geometry of the modeled domain of the stent.

The material is nickel-titanium alloy (nitinol), and it is modeled with Lagoudas SMA model. The material properties for each phase are given by:

TABLE I: MATERIAL PROPERTIES OF EACH PHASE.

MATERIAL PROPERTY	AUSTENITE	MARTENSITE
Young's modulus	55 GPa	46 GPa
Poisson's ratio	0.33	0.33
Heat capacity at constant pressure	400 J/(kg.K)	400 J/(kg.K)
Density	6500 kg/m ³	6500 kg/m ³

The phase transformation parameters are:

TABLE 2: PHASE TRANSFORMATION PARAMETERS.

PARAMETER	VALUE
Martensite start temperature	-28 °C
Martensite finish temperature	-43 °C
Austenite start temperature	-3 °C

TABLE 2: PHASE TRANSFORMATION PARAMETERS.

PARAMETER	VALUE
Austenite finish temperature	7 °C
Slope of martensite limit curve	7.4 MPa/K
Slope of austenite limit curve	7.4 MPa/K
Maximum transformation strain	0.056

Results and Discussion

Figure 3 shows that after crimping the stress is concentrated at the inner face of the bend. The locations where the stress is maximal are the locations where the martensite volume fraction is higher as well. Nonzero martensite volume fraction means that transformation occurred, so residual strain remains. Comparison with Figure 4 shows that heating to body temperature has two effects: the maximum stress becomes far higher because the limit stress has increased, and the zone of transformation has reduced, which shows that reverse transformation has partially occurred. Those effects can be noticed on the figures of whole stent as well, see Figure 5 to Figure 8. The development of the martensite during the different steps of the solution is shown in Figure 9, and pressure on the inner wall of the artery during the release of the stent in Figure 10.

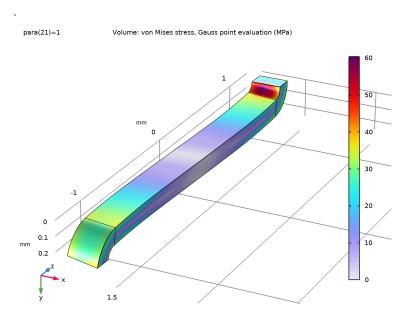


Figure 3: Stress and transformation state of one arm of the stent after crimping.

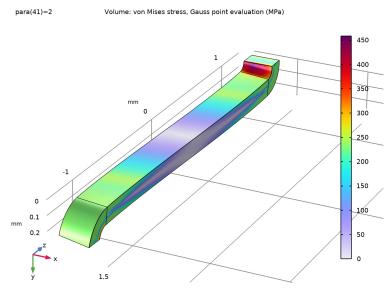


Figure 4: Stress and transformation state of one arm of the stent in the human body.

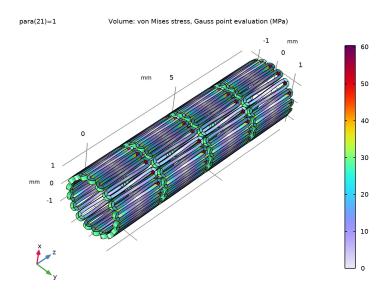


Figure 5: Stress in the stent after crimping.

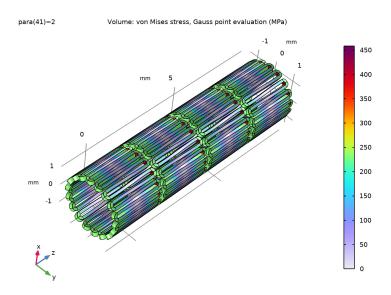


Figure 6: Stress in the stent in the human body.

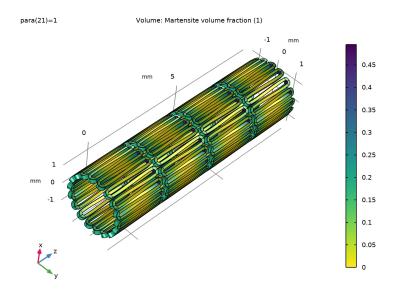


Figure 7: Martensite volume fraction in the stent after crimping.

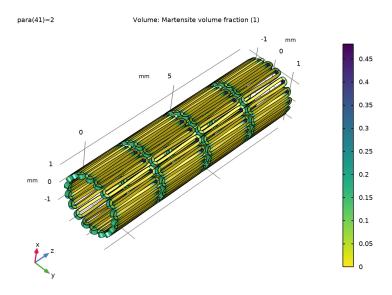


Figure 8: Martensite volume fraction in the stent in human body.

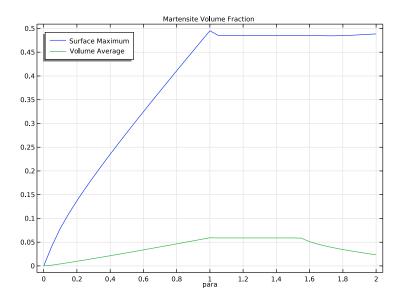


Figure 9: Maximum and average volume fraction history during crimping and release.

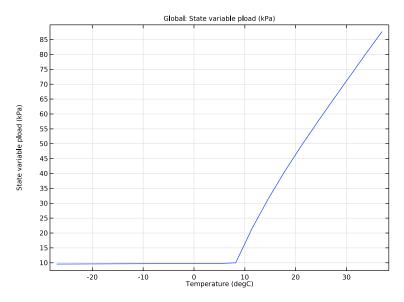


Figure 10: Pressure applied on the inner wall of the artery during stent release.

Notes About the COMSOL Implementation

The stent is crimped and maintained in position with a boundary load condition. The applied pressure is driven by the desired outer radius with a Global Equations feature. It adds the pressure as a DOF and adds a new global equation on the displacement.

The Shape Memory Alloy model requires local computations at each Gauss point during the assembly process which is expensive. By using Reduced Integration, the number of Gauss points are reduced by approximately a factor three for the given displacement shape function order and mesh element type. This setting speed up the computational time significantly.

Reference

1. D.C. Lagoudas, ed., Shape Memory Alloys, Modeling and Engineering Applications, Springer, p. 219, 2008.

Application Library path: Nonlinear Structural Materials Module/ Shape_Memory_Alloys/sma_stent

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

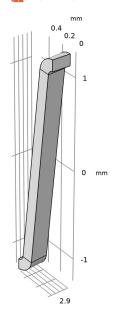
- I In the Model Wizard window, click **3D**.
- 2 In the Select Physics tree, select Structural Mechanics Solid Mechanics (solid).
- 3 Click Add.
- 4 Click 🔵 Study.
- 5 In the Select Study tree, select General Studies>Stationary.
- 6 Click **Done**.

GEOMETRY I

The geometry sequence for the model is available in a file. If you want to create it from scratch yourself, you can follow the instructions in the Appendix — Geometry Modeling Instructions section. Otherwise, insert the geometry sequence as follows:

- I In the Geometry toolbar, click Insert Sequence and choose Insert Sequence.
- 2 Browse to the model's Application Libraries folder and double-click the file sma_stent_geom_sequence.mph.

3 In the Geometry toolbar, click **Build All**.





GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
para	0	0	Sweep parameter
pload	0[N/m^2]	0 N/m ²	Applied pressure

DEFINITIONS

Add functions to prescribe the outer radius and temperature.

Interpolation I (int I)

- I In the Home toolbar, click f(X) Functions and choose Global>Interpolation.
- 2 In the Settings window for Interpolation, locate the Definition section.
- 3 In the Function name text field, type ro.

4 In the table, enter the following settings:

t	f(t)
0	Ro
1	1.4[mm]
2	1.4[mm]

5 Locate the **Units** section. In the **Function** table, enter the following settings:

Function	Unit
ro	m

Interpolation 2 (int2)

- I In the Home toolbar, click f(x) Functions and choose Global>Interpolation.
- 2 In the Settings window for Interpolation, locate the Definition section.
- **3** In the **Function name** text field, type temperature.
- **4** In the table, enter the following settings:

t	f(t)
0	-27
1	-27
2	37

5 Locate the **Units** section. In the **Function** table, enter the following settings:

Function	Unit
temperature	degC

Since the study has two distinct phases, a first one with forward transformation and a second one with reverse transformation, use a function to specify the transformation direction. This will improve the time and robustness of computation.

Piecewise I (pw I)

- I In the Home toolbar, click f(x) Functions and choose Global>Piecewise.
- 2 In the Settings window for Piecewise, locate the Definition section.
- **3** Find the **Intervals** subsection. In the table, enter the following settings:

Start	End	Function
0	1	1
1	2	-1

Create three material nodes: one for each austenite and martensite phase, and one for common properties. For now, just add the material nodes to make them available, the required data will be filled in later.

MATERIALS

General

- I In the Model Builder window, under Component I (compl) right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type General in the Label text field.

Austenite

- I Right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type Austenite in the Label text field.

Martensite

- I Right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type Martensite in the Label text field.

SOLID MECHANICS (SOLID)

Shape Memory Alloy I

- I In the Model Builder window, under Component I (compl) right-click Solid Mechanics (solid) and choose Material Models>Shape Memory Alloy.
- 2 In the Settings window for Shape Memory Alloy, locate the Domain Selection section.
- 3 From the Selection list, choose All domains.
- **4** Locate the **Model Input** section. From the *T* list, choose **User defined**. In the associated text field, type temperature(para).
- 5 Locate the Shape Memory Alloy section. Find the Austenite subsection. From the list, choose Austenite (mat2).
- 6 Find the Martensite subsection. From the list, choose Martensite (mat3).
- 7 Locate the Geometric Nonlinearity section. Select the Geometrically linear formulation check box.
 - The local computations at Gauss points during assembly are expensive for the SMA model. Using a reduced integration scheme will reduce the overall simulation time.
- **8** Locate the **Quadrature Settings** section. Select the **Reduced integration** check box.

Phase Transformation Direction 1

- I In the Model Builder window, expand the Shape Memory Alloy I node, then click Phase Transformation Direction 1.
- 2 In the Settings window for Phase Transformation Direction, locate the Phase Transformation Direction section.
- 3 From the Transformation direction list, choose User defined.
- 4 In the text field, type pw1(para).

Shape Memory Alloy I

In the Model Builder window, click Shape Memory Alloy 1.

Thermal Expansion 1

- I In the Physics toolbar, click 🖳 Attributes and choose Thermal Expansion.
- 2 In the Settings window for Thermal Expansion, locate the Model Input section.
- 3 Click of Go to Source for Volume reference temperature.

GLOBAL DEFINITIONS

Default Model Inputs

- I In the Model Builder window, under Global Definitions click Default Model Inputs.
- 2 In the Settings window for Default Model Inputs, locate the Browse Model Inputs section.
- 3 Find the Expression for remaining selection subsection. In the **Volume reference temperature** text field, type -27[degC].

SOLID MECHANICS (SOLID)

Thermal Expansion 1

- I In the Model Builder window, under Component I (compl)>Solid Mechanics (solid)> Shape Memory Alloy I click Thermal Expansion I.
- 2 In the Settings window for Thermal Expansion, locate the Thermal Expansion Properties section.
- 3 Find the Austenite subsection. From the list, choose Austenite (mat2).
- 4 Find the Martensite subsection. From the list, choose Martensite (mat3).

Symmetry I

- I In the Physics toolbar, click **Boundaries** and choose Symmetry.
- **2** Select Boundaries 2 and 13 only.

Prescribe zero displacement in the z direction on one point to avoid rigid body motion.

Prescribed Displacement I

- I In the Physics toolbar, click Points and choose Prescribed Displacement.
- **2** Select Point 16 only.
- 3 In the Settings window for Prescribed Displacement, locate the Prescribed Displacement section.
- 4 Select the Prescribed in z direction check box.

Boundary Load 1

- I In the Physics toolbar, click **Boundaries** and choose **Boundary Load**.
- **2** Select Boundaries 14–16 only.
- 3 In the Settings window for Boundary Load, locate the Force section.
- 4 From the Load type list, choose Pressure.
- 5 In the p text field, type pload.

DEFINITIONS

Use point integration to make the displacement available in expressions.

Integration I (intobl)

- I In the Definitions toolbar, click Nonlocal Couplings and choose Integration.
- 2 In the Settings window for Integration, locate the Advanced section.
- 3 From the Frame list, choose Material (X, Y, Z).
- 4 Locate the Source Selection section. From the Geometric entity level list, choose Point.
- **5** Select Point 16 only.

SOLID MECHANICS (SOLID)

Now add a global equation for the applied pressure, so that the outer radius equals the prescribed one. For that, you need to show advanced physics options.

- I Click the Show More Options button in the Model Builder toolbar.
- 2 In the Show More Options dialog box, in the tree, select the check box for the node Physics>Equation-Based Contributions.
- 3 Click OK.

Global Equations 1

- I In the Physics toolbar, click **Solution** Global and choose Global Equations.
- 2 In the Settings window for Global Equations, locate the Global Equations section.

3 In the table, enter the following settings:

Name	f(u,ut,utt,t) (1)	Initial value (u_0) (1)	Initial value (u_t0) (1/s)	Description
pload	<pre>intop1(x)- ro(para)</pre>	0	0	

- 4 Locate the Units section. Click Define Dependent Variable Unit.
- 5 In the Dependent variable quantity table, enter the following settings:

Dependent variable quantity	Unit
Custom unit	Pa

- 6 Click Define Source Term Unit.
- 7 In the Source term quantity table, enter the following settings:

Source term quantity	Unit
Custom unit	m

MATERIALS

General (mat I)

- I In the Model Builder window, under Component I (compl)>Materials click General (mat I).
- 2 In the Settings window for Material, locate the Material Contents section.
- **3** In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Shape memory alloy reference temperature	ТО	293.15[K]	K	Lagoudas model
Poisson's ratio	nu	0.33	I	Basic
Martensite start temperature	TMs	-28[degC]	K	Lagoudas model
Martensite finish temperature	TMf	-43[degC]	K	Lagoudas model
Slope of martensite limit curve	CM	7.4e6	Pa/K	Lagoudas model

Property	Variable	Value	Unit	Property group
Austenite start temperature	TAs	-3[degC]	K	Lagoudas model
Austenite finish temperature	TAf	7[degC]	K	Lagoudas model
Slope of austenite limit curve	CA	7.4e6	Pa/K	Lagoudas model
Maximum transformation strain	etrmaxLagoudas	0.056	I	Lagoudas model
Calibration stress level	sigmaStar	0	N/m²	Lagoudas model
Density	rho	6500	kg/m³	Basic

Austenite (mat2)

- I In the Model Builder window, click Austenite (mat2).
- 2 In the Settings window for Material, locate the Material Contents section.
- **3** In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	E_A	55[GPa]	Pa	Austenite phase
Heat capacity at constant pressure	C _P _A	400	J/(kg·K)	Austenite phase
Coefficient of thermal expansion	alpha_A_iso; alpha_Aii = alpha_A_iso, alpha_Aij = 0	22e-6	I/K	Thermal expansion, austenite phase

Martensite (mat3)

- I In the Model Builder window, click Martensite (mat3).
- 2 In the Settings window for Material, locate the Material Contents section.

3 In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	E_M	46[GPa]	Pa	Martensite phase
Heat capacity at constant pressure	C _P _M	400	J/(kg·K)	Martensite phase
Coefficient of thermal expansion	alpha_M_iso ; alpha_Mii = alpha_M_iso, alpha_Mij = 0	22e-6	I/K	Thermal expansion, martensite phase

MESH I

Mapped I

- I In the Mesh toolbar, click A Boundary and choose Mapped.
- 2 Select Boundary 13 only.

Distribution 1

- I Right-click Mapped I and choose Distribution.
- **2** Select Edge 16 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 4.

Distribution 2

- I In the Model Builder window, right-click Mapped I and choose Distribution.
- **2** Select Edge 18 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 3.

Swept I

In the Mesh toolbar, click A Swept.

Distribution I

- I Right-click Swept I and choose Distribution.
- 2 Select Domains 1 and 3 only.
- 3 In the Settings window for Distribution, locate the Distribution section.

4 In the Number of elements text field, type 20.

Distribution 2

- I In the Model Builder window, right-click Swept I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Domain Selection section.
- 3 Click Clear Selection.
- 4 Select Domain 2 only.
- 5 Locate the Distribution section. From the Distribution type list, choose Predefined.
- 6 In the Number of elements text field, type 40.
- 7 In the Element ratio text field, type 8.
- 8 Select the Symmetric distribution check box.
- 9 In the Model Builder window, right-click Mesh I and choose Build All.

Add maximum and average operators that will be used in postprocessing.

DEFINITIONS

Maximum I (maxobl)

- I In the Definitions toolbar, click / Nonlocal Couplings and choose Maximum.
- 2 In the Settings window for Maximum, locate the Source Selection section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 Select Boundary 12 only.

Average I (aveob I)

- I In the Definitions toolbar, click Monlocal Couplings and choose Average.
- 2 In the Settings window for Average, locate the Source Selection section.
- 3 From the Selection list, choose All domains.
- 4 Locate the Advanced section. From the Frame list, choose Material (X, Y, Z).

STUDY I

Step 1: Stationary

- I In the Model Builder window, under Study I click Step I: Stationary.
- 2 In the Settings window for Stationary, locate the Study Settings section.
- 3 Select the Include geometric nonlinearity check box.
- 4 Click to expand the **Study Extensions** section. Select the **Auxiliary sweep** check box.
- 5 Click + Add.

- **6** In the table, click to select the cell at row number 1 and column number 2.
- 7 In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
para (Sweep parameter)		

- 8 Click Range.
- 9 In the Range dialog box, type 0 in the Start text field.
- 10 In the Step text field, type 0.05.
- II In the **Stop** text field, type 2.
- 12 Click Replace.
- 13 In the Home toolbar, click **Compute**.

RESULTS

Stress (solid)

- I In the Settings window for 3D Plot Group, locate the Plot Settings section.
- 2 From the Frame list, choose Spatial (x, y, z).

Volume 1

- I In the Model Builder window, expand the Stress (solid) node, then click Volume I.
- 2 In the Settings window for Volume, locate the Expression section.
- 3 From the Unit list, choose MPa.

Stress (solid)

- I In the Model Builder window, click Stress (solid).
- 2 In the Settings window for 3D Plot Group, locate the Plot Settings section.
- 3 From the View list, choose New view.
- 4 In the Stress (solid) toolbar, click Plot.

Use the mouse and zoom buttons to get similar view as Figure 4.

Now show the results at the end of crimping.

- 5 Locate the Data section. From the Parameter value (para) list, choose 1.
- 6 In the Stress (solid) toolbar, click Plot.
- 7 From the Parameter value (para) list, choose 2.

Reproduce Figure 9 to show the evolution of martensite volume fraction.

Martensite Volume Fraction

- I In the Home toolbar, click **Add Plot Group** and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Martensite Volume Fraction in the **Label** text field.

Global I

- I In the Martensite Volume Fraction toolbar, click (Global.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
maxop1(solid.xi_M)	1	Surface Maximum
aveop1(solid.xi_M)	1	Volume Average

4 In the Martensite Volume Fraction toolbar, click **Plot**.

Martensite Volume Fraction

- I In the Model Builder window, click Martensite Volume Fraction.
- 2 In the Settings window for ID Plot Group, click to expand the Title section.
- 3 From the Title type list, choose Manual.
- 4 In the Title text area, type Martensite Volume Fraction.
- **5** Locate the **Legend** section. From the **Position** list, choose **Upper left**.

Reproduce Figure 10 to show the increase of pressure with temperature.

Pressure vs. Temberature

- I In the Home toolbar, click Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Pressure vs. Temperature in the Label text field.
- 3 Locate the Data section. From the Parameter selection (para) list, choose From list.
- 4 In the Parameter values list, select the solution steps from 1 to 2.

Global I

- I Right-click Pressure vs. Temperature and choose Global.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description	
pload	kPa	State variable pload	

- 4 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- 5 In the **Expression** text field, type temperature(para).
- **6** From the **Unit** list, choose **degC**.
- 7 Select the **Description** check box.
- **8** In the associated text field, type Temperature.

Pressure vs. Temperature

- I In the Model Builder window, click Pressure vs. Temperature.
- 2 In the Settings window for ID Plot Group, locate the Legend section.
- 3 Clear the Show legends check box.
- 4 In the Pressure vs. Temperature toolbar, click **Plot**.

Create new datasets to build the entire geometry of the stent and reproduce Figure 5 to Figure 8.

Sector 3D I

- I In the Results toolbar, click More Datasets and choose Sector 3D.
- 2 In the Settings window for Sector 3D, locate the Symmetry section.
- 3 In the Number of sectors text field, type 2*Ns.
- 4 From the Transformation list, choose Rotation and reflection.

Array 3D I

- I In the Results toolbar, click More Datasets and choose Array 3D.
- 2 In the Settings window for Array 3D, locate the Data section.
- 3 From the Dataset list, choose Sector 3D 1.
- 4 Locate the Array Size section. In the Z size text field, type 4.
- **5** Locate the **Displacement** section. From the **Method** list, choose **Manual**.
- **6** In the **Z** text field, type hs*1.1.

Stress, Whole Stent

- I In the Model Builder window, right-click Stress (solid) and choose Duplicate.
- 2 In the Settings window for 3D Plot Group, type Stress, Whole Stent in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Array 3D 1.
- 4 In the Stress, Whole Stent toolbar, click Plot.
- 5 Locate the Plot Settings section. From the View list, choose New view.

- 6 In the Stress, Whole Stent toolbar, click Plot.
- 7 Click Tolling Plot.
- 8 Locate the Data section. From the Parameter value (para) list, choose 1.
- 9 In the Stress, Whole Stent toolbar, click Plot.
- 10 Click Plot.
- II From the Parameter value (para) list, choose 2.

Transformation, Whole Stent

- I Right-click Stress, Whole Stent and choose Duplicate.
- 2 In the Settings window for 3D Plot Group, type Transformation, Whole Stent in the **Label** text field.

Volume 1

- I In the Model Builder window, expand the Transformation, Whole Stent node, then click Volume 1.
- 2 In the Settings window for Volume, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>Solid Mechanics> Shape memory alloy>solid.xi_M - Martensite volume fraction.
- 3 Locate the Coloring and Style section. From the Color table list, choose Viridis.
- 4 From the Color table transformation list, choose Reverse.

Transformation, Whole Stent

- I In the Model Builder window, click Transformation, Whole Stent.
- 2 In the Transformation, Whole Stent toolbar, click Plot.
- 3 In the Settings window for 3D Plot Group, locate the Data section.
- 4 From the Parameter value (para) list, choose 1.
- 6 Click Plot
- 7 From the Parameter value (para) list, choose 2.

Create animations of the last two plots.

Stress

- I In the Results toolbar, click Animation and choose Player.
- 2 In the Settings window for Animation, type Stress in the Label text field.
- 3 Locate the Scene section. From the Subject list, choose Stress, Whole Stent.
- 4 Locate the Frames section. From the Frame selection list, choose All.

- 5 Locate the Playing section. In the Display each frame for text field, type 0.2.
- **6** Click the Play button in the **Graphics** toolbar.

Transformation

- I Right-click Stress and choose Duplicate.
- 2 In the Settings window for Animation, type Transformation in the Label text field.
- 3 Locate the Scene section. From the Subject list, choose Transformation, Whole Stent.
- 4 Click the Play button in the Graphics toolbar.

Appendix — Geometry Modeling Instructions

From the File menu, choose New.

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click **1** 3D.
- 2 Click **Done**.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
Ro	3[mm]	0.003 m	Outer radius
wr	0.2[mm]	2E-4 m	Width
Ri	Ro-wr	0.0028 m	Inner radius
hs	2.4[mm]	0.0024 m	Height
th	0.12[mm]	1.2E-4 m	Thickness
Ns	18	18	Number of sectors
alpha	2*pi/Ns/2[rad]	0.17453 rad	Sector angle
radius	0.12[mm]	1.2E-4 m	Bent radius

GEOMETRY I

- I In the Model Builder window, under Component I (compl) click Geometry I.
- 2 In the Settings window for Geometry, locate the Units section.
- **3** From the **Length unit** list, choose **mm**.

Work Plane I (wbl)

- I In the Geometry toolbar, click Work Plane.
- 2 In the Settings window for Work Plane, locate the Plane Definition section.
- 3 From the Plane list, choose yz-plane.

Work Plane I (wp I)>Plane Geometry

In the Model Builder window, click Plane Geometry.

Work Plane I (wpl)>Circle I (cl)

- I In the Work Plane toolbar, click Circle.
- 2 In the Settings window for Circle, locate the Object Type section.
- **3** From the **Type** list, choose **Curve**.
- 4 Locate the Size and Shape section. In the Radius text field, type radius-th/2.
- 5 In the Sector angle text field, type 180.
- 6 Locate the Position section. In the xw text field, type -Ri*sin(alpha/2).
- 7 In the yw text field, type hs/2-radius.
- 8 Locate the Rotation Angle section. In the Rotation text field, type 270.
- 9 Locate the Selections of Resulting Entities section. Select the Resulting objects selection check box.
- 10 From the Show in 3D list, choose Off.
- II Find the Cumulative selection subsection. Click New.
- 12 In the New Cumulative Selection dialog box, type union1 in the Name text field.
- I3 Click OK.

Work Plane I (wp I)>Circle 2 (c2)

- I In the Work Plane toolbar, click (Circle.
- 2 In the Settings window for Circle, locate the Object Type section.
- **3** From the **Type** list, choose **Curve**.
- 4 Locate the Size and Shape section. In the Radius text field, type radius+th/2.
- 5 In the Sector angle text field, type 180.

- 6 Locate the **Position** section. In the xw text field, type Ri*sin(alpha/2).
- 7 In the yw text field, type (hs/2-radius).
- **8** Locate the **Rotation Angle** section. In the **Rotation** text field, type 90.
- 9 Locate the Selections of Resulting Entities section. Select the Resulting objects selection check box.
- 10 From the Show in 3D list, choose Off.
- II Find the Cumulative selection subsection. From the Contribute to list, choose union I.
- 12 Click **Build Selected**.
- 13 Click the Zoom Extents button in the Graphics toolbar.

Work Plane I (wpl)>Tangent I (tanl)

- I In the Work Plane toolbar, click \(^{\sqrt{1}}\) Tangent.
- 2 In the Settings window for Tangent, locate the Tangent section.
- 3 From the Edge to tangent list, choose Circle 1.
- 4 From the Second edge to tangent list, choose Circle 2.
- 5 Locate the Selections of Resulting Entities section. Find the Cumulative selection subsection. From the Contribute to list, choose union1.

Work Plane I (wbl)>Union I (unil)

- I In the Work Plane toolbar, click Booleans and Partitions and choose Union.
- 2 In the Settings window for Union, locate the Union section.
- 3 From the Input objects list, choose union1.

Work Plane I (wp I)>Circle I (c1), Work Plane I (wp I)>Circle 2 (c2), Work Plane I (wpl)>Tangent I (tanl), Work Plane I (wpl)>Union I (unil)

- I In the Model Builder window, under Component I (compl)>Geometry I>Work Plane I (wp1)>Plane Geometry, Ctrl-click to select Circle I (c1), Circle 2 (c2), Tangent I (tan1), and Union I (unil).
- 2 Right-click and choose **Duplicate**.

Work Plane 1 (wb1)>Circle 3 (c3)

- I In the Settings window for Circle, locate the Size and Shape section.
- 2 In the Radius text field, type radius+th/2.
- 3 Locate the Selections of Resulting Entities section. Find the Cumulative selection subsection. Click New.
- 4 In the New Cumulative Selection dialog box, type union2 in the Name text field.

5 Click OK.

Work Plane I (wpl)>Circle 4 (c4)

- I In the Model Builder window, click Circle 4 (c4).
- 2 In the Settings window for Circle, locate the Size and Shape section.
- 3 In the Radius text field, type radius-th/2.
- 4 Locate the Selections of Resulting Entities section. Find the Cumulative selection subsection. From the Contribute to list, choose union2.
- 5 Click **Build Selected**.

Work Plane I (wpI)>Tangent 2 (tan2)

- I In the Model Builder window, click Tangent 2 (tan2).
- 2 In the Settings window for Tangent, locate the Tangent section.
- 3 From the Edge to tangent list, choose Circle 3.
- 4 From the Second edge to tangent list, choose Circle 4.
- 5 Locate the Selections of Resulting Entities section. Find the Cumulative selection subsection. From the Contribute to list, choose union2.
- 6 Click **Build Selected**.

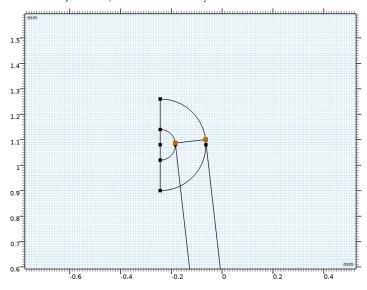
Work Plane I (wp I)>Union 2 (uni2)

- I In the Model Builder window, click Union 2 (uni2).
- 2 In the Settings window for Union, locate the Union section.
- 3 From the Input objects list, choose union2.
- 4 In the Work Plane toolbar, click **Build All**.

Work Plane I (wpI)>Line Segment I (IsI)

- I In the Work Plane toolbar, click * More Primitives and choose Line Segment.
- 2 On the object unil, select Point 4 only.
- 3 In the Settings window for Line Segment, locate the Endpoint section.
- **4** Find the **End vertex** subsection. Click to select the **Activate Selection** toggle button.

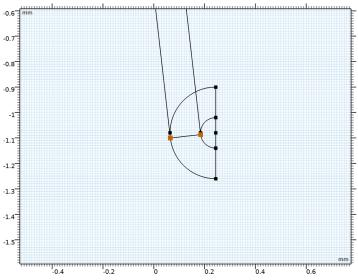
5 On the object uni2, select Point 4 only.



Work Plane I (wp I)>Line Segment 2 (ls2)

- I In the Work Plane toolbar, click * More Primitives and choose Line Segment.
- 2 On the object unil, select Point 7 only.
- 3 In the Settings window for Line Segment, locate the Endpoint section.
- **4** Find the **End vertex** subsection. Click to select the **Activate Selection** toggle button.

5 On the object **uni2**, select Point 7 only.



6 Click **Build Selected**.

Work Plane I (wpl)>Rectangle I (rl)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Object Type section.
- 3 From the Type list, choose Curve.
- 4 Locate the Size and Shape section. In the Width text field, type 0.2.
- 5 In the **Height** text field, type th.
- 6 Locate the Position section. From the Base list, choose Center.
- 7 In the xw text field, type (Ri*sin(alpha/2)+0.1).
- 8 In the yw text field, type hs/2.

Work Plane I (wp I)>Rectangle 2 (r2)

- I Right-click Component I (compl)>Geometry I>Work Plane I (wpl)>Plane Geometry> Rectangle I (rI) and choose Duplicate.
- 2 In the Settings window for Rectangle, locate the Position section.
- 3 In the xw text field, type Ri*sin(alpha/2)+0.1.
- 4 In the yw text field, type -hs/2.

Work Plane I (wbl)>Box Selection I (boxsell)

- I In the Work Plane toolbar, click \(\frac{1}{2} \) Selections and choose Box Selection.
- 2 In the Settings window for Box Selection, locate the Geometric Entity Level section.
- 3 From the Level list, choose Boundary.
- 4 Locate the Box Limits section. In the xw maximum text field, type -Ri*sin(alpha/2)+ 0.001.
- 5 In the yw maximum text field, type hs/2-th.
- 6 Locate the Resulting Selection section. Find the Cumulative selection subsection. Click New.
- 7 In the New Cumulative Selection dialog box, type Delete in the Name text field.
- 8 Click OK.

Work Plane I (wbl)>Box Selection 2 (boxsel2)

- I In the Work Plane toolbar, click 🔓 Selections and choose Box Selection.
- 2 In the Settings window for Box Selection, locate the Geometric Entity Level section.
- 3 From the Level list, choose Boundary.
- 4 Locate the Box Limits section. In the xw minimum text field, type Ri*sin(alpha/2)-0.001.
- 5 In the yw minimum text field, type (hs/2-th).
- 6 Locate the Resulting Selection section. Find the Cumulative selection subsection. From the Contribute to list, choose Delete.

Work Plane I (wbl)>Disk Selection I (disksell)

- I In the Work Plane toolbar, click \(\frac{1}{2} \) Selections and choose Disk Selection.
- 2 In the Settings window for Disk Selection, locate the Geometric Entity Level section.
- 3 From the Level list, choose Boundary.
- 4 Locate the Input Entities section. From the Entities list, choose From selections.
- 5 Click + Add.
- 6 In the Add dialog box, in the Selections list, choose Circle 1 and Circle 3.
- 7 Click OK.
- 8 In the Settings window for Disk Selection, locate the Disk Center section.
- 9 In the xw text field, type -Ri*sin(alpha/2).
- 10 In the yw text field, type hs/2-radius.
- II Locate the Size and Shape section. In the Outer radius text field, type radius+th.

- 12 In the Inner radius text field, type 1e-2.
- 13 In the Start angle text field, type 15.
- 14 In the End angle text field, type 15.
- 15 Locate the Output Entities section. From the Include entity if list, choose Entity inside disk.
- 16 Locate the Input Entities section. In the Selections list, select Circle 3.
- 17 Locate the Resulting Selection section. Clear the Keep selection check box.
- 18 Find the Cumulative selection subsection. From the Contribute to list, choose Delete.

Work Plane I (wp I)>Disk Selection 2 (disksel2)

- I Right-click Component I (compl)>Geometry I>Work Plane I (wpl)>Plane Geometry> Disk Selection I (disksell) and choose Duplicate.
- 2 In the Settings window for Disk Selection, locate the Input Entities section.
- 3 Click Build Preceding State.
- 4 In the Selections list, choose Circle 1 and Circle 3.
- 5 Click Delete.
- 6 Click + Add.
- 7 In the Add dialog box, in the Selections list, choose Circle 2 and Circle 4.
- 8 Click OK.
- 9 In the Settings window for Disk Selection, locate the Disk Center section.
- 10 In the xw text field, type Ri*sin(alpha/2).
- II In the yw text field, type (hs/2-radius).
- 12 Locate the Size and Shape section. In the Start angle text field, type 165.
- 13 In the End angle text field, type 195.
- 14 Click | Build Selected.

Work Plane I (wp I)>Box Selection 3 (boxsel3)

- I In the Work Plane toolbar, click Selections and choose Box Selection.
- 2 In the Settings window for Box Selection, locate the Geometric Entity Level section.
- 3 From the Level list, choose Boundary.
- 4 Locate the Box Limits section. In the xw minimum text field, type -Ri*sin(alpha/2) -0.01.
- 5 In the xw maximum text field, type -Ri*sin(alpha/2)+0.01.

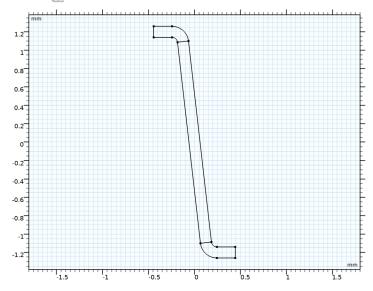
- **6** Locate the **Output Entities** section. From the **Include entity if** list, choose **Entity inside box**.
- 7 Locate the Resulting Selection section. Find the Cumulative selection subsection. From the Contribute to list, choose Delete.
- **8** Clear the **Keep selection** check box.

Work Plane I (wp I)>Box Selection 4 (boxsel4)

- I Right-click Component I (compl)>Geometry I>Work Plane I (wpl)>Plane Geometry> Box Selection 3 (boxsel3) and choose Duplicate.
- 2 In the Settings window for Box Selection, locate the Box Limits section.
- 3 In the xw minimum text field, type Ri*sin(alpha/2)-0.01.
- 4 In the xw maximum text field, type Ri*sin(alpha/2)+0.01.

Work Plane I (wp I)>Delete Entities I (del I)

- I In the Model Builder window, right-click Plane Geometry and choose Delete Entities.
- 2 In the Settings window for Delete Entities, locate the Entities or Objects to Delete section.
- 3 From the Selection list, choose Delete.
- 4 Click Pauld Selected.



Work Plane I (wpl)>Convert to Solid I (csoll)

- I In the Work Plane toolbar, click Conversions and choose Convert to Solid.
- 2 Click in the **Graphics** window and then press Ctrl+A to select all objects.

3 In the Work Plane toolbar, click Build All.

Work Plane I (wbl)

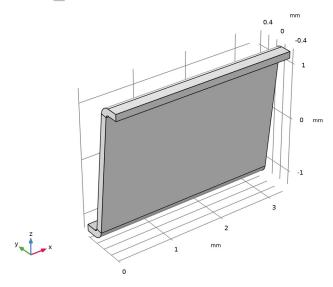
In the Model Builder window, collapse the Component I (compl)>Geometry I> Work Plane I (wpI) node.

Extrude I (extI)

- I In the Model Builder window, right-click Geometry I and choose Extrude.
- 2 In the Settings window for Extrude, locate the Distances section.
- **3** In the table, enter the following settings:

Distances (mm) Ro*1.1

4 Click | Build Selected.



Rotate I (rot1)

- I In the Geometry toolbar, click Transforms and choose Rotate.
- **2** Select the object **ext1** only.
- 3 In the Settings window for Rotate, locate the Rotation section.
- 4 In the Angle text field, type alpha/2.
- 5 Click Pauld Selected.

Work Plane 2 (wp2)

- I In the Geometry toolbar, click Work Plane.
- 2 In the Settings window for Work Plane, locate the Plane Definition section.
- 3 From the Plane list, choose xz-plane.

Work Plane 2 (wp2)>Plane Geometry

In the Model Builder window, click Plane Geometry.

Work Plane 2 (wp2)>Rectangle 1 (r1)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type wr.
- 4 In the Height text field, type hs*1.1.
- **5** Locate the **Position** section. From the **Base** list, choose **Center**.
- 6 In the xw text field, type (Ri+Ro)/2.
- 7 Click | Build Selected.

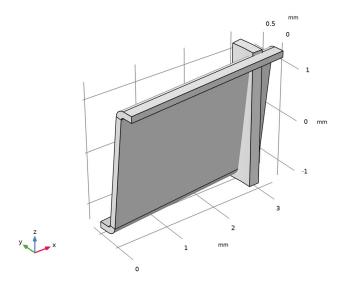
Work Plane 2 (wp2)

In the Model Builder window, collapse the Component I (compl)>Geometry I> Work Plane 2 (wp2) node.

Revolve I (rev I)

- I In the Model Builder window, right-click Geometry I and choose Revolve.
- 2 In the Settings window for Revolve, locate the Revolution Angles section.
- **3** Click the **Angles** button.
- 4 In the End angle text field, type alpha.

5 Click Pauld Selected.



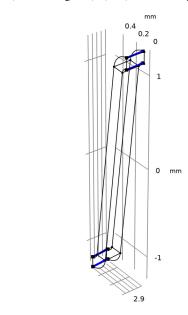
Intersection I (int1)

- I In the Geometry toolbar, click Booleans and Partitions and choose Intersection.
- 2 Click in the **Graphics** window and then press Ctrl+A to select both objects.

Ignore Edges I (ige I)

I In the Geometry toolbar, click 🗠 Virtual Operations and choose Ignore Edges.

2 On the object fin, select Edges 4, 7, 19, and 21 only.



- 3 In the Geometry toolbar, click **Build All**.
- 4 Click the Go to Default View button in the Graphics toolbar.