

# Stationary Analysis of a Biased Resonator — 3D

# Introduction

Silicon micromechanical resonators have long been used for designing sensors and are now becoming increasingly important as oscillators in the consumer electronics market. This sequence of models analyzes in detail a surface micromachined MEMS resonator, designed as part of a micromechanical filter. The resonator is based on that developed in Ref. 1.

This model performs a stationary analysis of the resonator, with an applied DC bias. It serves as a basis for all the subsequent analyses.

# Model Definition

The model consists of a poly-silicon resonator, which is manufactured through a surface micromachining process. Initially, a silicon wafer is coated with 0.75  $\mu$ m of oxide and 0.15  $\mu$ m of silicon nitride to isolate the micromachined parts from the wafer ground plane. Polysilicon electrodes with a thickness of 0.3  $\mu$ m are deposited next. A sacrificial layer of oxide is then deposited to a thickness of 198.5 nm. Note that in Ref. 1 the sacrificial oxide is actually 1.3  $\mu$ m, but the gap thickness was adjusted to this value for the purposes of simulation to account for the depletion layer in the silicon. This model uses the same adjustment to enable the simulations to be directly compared with those presented in the paper. Holes are etched in the sacrificial layer (to provide anchor points for the resonator) and the structural polysilicon is deposited with a thickness of 1.9  $\mu$ m.

The structure has a plane of symmetry, so it is possible to model only half of the geometry explicitly, although care must be taken to mirror the geometry before performing a modal analysis. Figure 1 shows the geometry.



Figure 1: Top: Device geometry. The wafer itself is not shown explicitly, but is represented in the model by a ground plane on the underside of the geometry. Bottom: The model geometry as it appears in COMSOL.

The layers of deposited material from the ground plane up are: silicon oxide, silicon nitride (too thin to see clearly), polysilicon electrodes/air gap (etched sacrificial oxide), polysilicon resonator, and air.

In operation, both the silicon resonator and the underlying wafer are grounded and an electric voltage is applied to the driving electrode, which is bisected by the symmetry plane.

Typically a DC bias of 35 V is applied in normal operation of the device. The assumption is made that the polysilicon is a perfect conductor, so the bias voltage can be applied on the resonator using the Domain Terminal feature, which is much easier than selecting the many boundaries for setting the electric potential on them.

In this model, the deformation of the structure is computed with the applied DC bias. Note that the silicon oxide and nitride are assumed to be rigid for the solid mechanics simulations, so the structure is anchored at the base of its electrode, and these domains are not included in the solid mechanics equations.

## ELECTROMECHANICAL FORCES

Within a vacuum or other medium, forces between charged bodies can be computed on the assumption that a fictitious state of stress exists within the field. The Electromagnetic or Maxwell stress tensor can be used to compute the induced stresses in a material as a result of an electric field as well as surface forces acting on bodies in air or vacuum. In this model, it is assumed that the polysilicon is doped sufficiently heavily that it can be treated as a perfect conductor. The electric field is assumed to be zero inside the resonator, which means that the Maxwell stress tensor is zero inside the material and there are no volumetric electrical forces. The Maxwell stress tensor in the medium surrounding the resonator, where the electric field is nonzero is (Ref. 2)

$$T_{\text{EM},V} = -\frac{1}{2} (\mathbf{E} \cdot \mathbf{D}) I + \mathbf{ED}^{T}$$

A net force on the surface typically results from the discontinuity of the stress tensor at the interface. However, because it is undesirable to apply a stress term throughout the vacuum, the force is only computed on the surface of the resonator, and is applied by the Electromechanical Interface node. The surface force is given by

$$\mathbf{n}_1 T_{\mathrm{EM}, V} = -\left(\frac{1}{2}\mathbf{E}\cdot\mathbf{D}\right)\mathbf{n}_1 + (\mathbf{n}_1\cdot\mathbf{E})\mathbf{D}$$

where  $\mathbf{n}_1$  is the surface normal, pointing out from the mechanical body.

# Results and Discussion

Figure 2 shows the *z* displacement of the structure with an applied DC bias. As expected the structural displacement is maximal on the symmetry plane at the center of the device. The maximum displacement is 13 nm. Electric potential isosurfaces are also shown in Figure 2. As expected, the isobars are uniformly distributed and closest together between the resonator and the electrode. This corresponds to a region of uniform electric field.

Around the electrode the fringing fields can also be seen. Note that the surface of the resonator is assumed to be perfectly grounded. This is a result of the potential boundary condition used and is equivalent to the assumption that the polysilicon is a perfect conductor.



Volume: Displacement field, Z component (µm) Isosurface: Electric potential (V)

Figure 2: The z-displacement of the resonator as a function of position. The maximum displacement occurs in the center of the resonator, immediately over the biasing electrode. Electric potential isosurfaces with values of 10 V (green), 20 V (yellow), and 30 V (red) are also shown.

# References

1. F.D. Bannon III, J.R. Clark, and C.T.-C. Nguyen, "High-Q HF Microelectromechanical Filters", *IEEE Journal of Solid State Circuits*, vol. 35, no. 4, pp. 512–526, 2000.

2. J.A. Stratton, *Electromagnetic Theory*, McGraw-Hill, New York, 1941.

Application Library path: MEMS\_Module/Actuators/biased\_resonator\_3d\_basic

# Modeling Instructions

From the File menu, choose New.

#### NEW

In the New window, click 🔗 Model Wizard.

# MODEL WIZARD

- I In the Model Wizard window, click 间 3D.
- 2 In the Select Physics tree, select Structural Mechanics>Electromagnetics-Structure Interaction>Electromechanics>Electromechanics.
- 3 Click Add.
- 4 Click 🔿 Study.
- 5 In the Select Study tree, select General Studies>Stationary.
- 6 Click **M** Done.

# GEOMETRY I

For convenience, the device geometry is inserted from an existing file. You can read the instructions for creating the geometry in the Appendix — Geometry Modeling Instructions.

- I In the Geometry toolbar, click Insert Sequence and choose Insert Sequence.
- 2 Browse to the model's Application Libraries folder and double-click the file biased\_resonator\_3d\_geom\_sequence.mph.
- **3** In the **Geometry** toolbar, click 🟢 **Build All**.

Add a parameter for the applied DC bias.

#### **GLOBAL DEFINITIONS**

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
Vdc	35[V]	35 V	DC bias voltage

Create selections to facilitate easy setup of the boundary conditions.

#### DEFINITIONS

All domains

- I In the **Definitions** toolbar, click **here Explicit**.
- 2 In the Settings window for Explicit, locate the Input Entities section.
- **3** Select the **All domains** check box.
- 4 Right-click Explicit I and choose Rename.
- 5 In the Rename Explicit dialog box, type All domains in the New label text field.
- 6 Click OK.

Ground Plane

- I In the **Definitions** toolbar, click **Toolbar**.
- 2 In the Settings window for Box, locate the Box Limits section.
- **3** In the **z minimum** text field, type -2.
- 4 In the **z maximum** text field, type -1.
- 5 Locate the Output Entities section. From the Include entity if list, choose Entity inside box.
- 6 Locate the Geometric Entity Level section. From the Level list, choose Boundary.
- 7 Right-click Box I and choose Rename.
- 8 In the Rename Box dialog box, type Ground Plane in the New label text field.
- 9 Click OK.

# Oxide

- I In the **Definitions** toolbar, click **The Box**.
- 2 In the Settings window for Box, locate the Box Limits section.
- **3** In the **z minimum** text field, type -1.
- 4 In the **z maximum** text field, type -0.9.
- 5 Right-click **Box 2** and choose **Rename**.
- 6 In the Rename Box dialog box, type Oxide in the New label text field.
- 7 Click OK.

# Nitride

- I In the **Definitions** toolbar, click **The Box**.
- 2 In the Settings window for Box, locate the Box Limits section.
- **3** In the **z minimum** text field, type -0.4.

- 4 In the **z maximum** text field, type -0.35.
- 5 Right-click **Box 3** and choose **Rename**.
- 6 In the Rename Box dialog box, type Nitride in the New label text field.
- 7 Click OK.

#### Electrode

- I In the **Definitions** toolbar, click **The Box**.
- 2 In the Settings window for Box, locate the Box Limits section.
- **3** In the **x minimum** text field, type -0.1.
- 4 In the **x maximum** text field, type 0.1.
- **5** In the **y minimum** text field, type -4.2.
- 6 In the z minimum text field, type -0.15.
- 7 In the **z maximum** text field, type -0.1.
- 8 Right-click Box 4 and choose Rename.
- 9 In the Rename Box dialog box, type Electrode in the New label text field.

IO Click OK.

- Ball I
- I In the Definitions toolbar, click hall/Disk.
- 2 In the Settings window for Ball, locate the Ball Center section.
- **3** In the **z** text field, type 1.
- 4 Locate the Ball Radius section. In the Radius text field, type 0.1.

#### Box 5

- I In the **Definitions** toolbar, click **The Box**.
- 2 In the Settings window for Box, locate the Box Limits section.
- **3** In the **y maximum** text field, type **4.8**.
- 4 In the **z minimum** text field, type -0.35.
- 5 In the z maximum text field, type 0.05.
- 6 Locate the Output Entities section. From the Include entity if list, choose Entity inside box.

#### Box 6

- I Right-click **Box 5** and choose **Duplicate**.
- 2 In the Settings window for Box, locate the Box Limits section.

- **3** In the **x minimum** text field, type 15.
- 4 In the **x maximum** text field, type 15.

#### Resonator

- I In the **Definitions** toolbar, click **Difference**.
- 2 In the Settings window for Difference, locate the Input Entities section.
- 3 Under Selections to add, click + Add.
- 4 In the Add dialog box, in the Selections to add list, choose Ball I and Box 5.

5 Click OK.

- 6 In the Settings window for Difference, locate the Input Entities section.
- 7 Under Selections to subtract, click + Add.
- 8 In the Add dialog box, select Box 6 in the Selections to subtract list.
- 9 Click OK.
- **IO** Right-click **Difference I** and choose **Rename**.
- II In the Rename Difference dialog box, type Resonator in the New label text field.

I2 Click OK.

PolySi

- I In the **Definitions** toolbar, click 📑 **Union**.
- 2 In the Settings window for Union, locate the Input Entities section.
- **3** Under Selections to add, click + Add.
- 4 In the Add dialog box, in the Selections to add list, choose Electrode and Resonator.

5 Click OK.

- 6 Right-click Union I and choose Rename.
- 7 In the Rename Union dialog box, type PolySi in the New label text field.
- 8 Click OK.

Air

- I In the **Definitions** toolbar, click **Difference**.
- 2 In the Settings window for Difference, locate the Input Entities section.
- 3 Under Selections to add, click + Add.
- 4 In the Add dialog box, select All domains in the Selections to add list.
- 5 Click OK.
- 6 In the Settings window for Difference, locate the Input Entities section.

- 7 Under Selections to subtract, click + Add.
- 8 In the Add dialog box, in the Selections to subtract list, choose Oxide, Nitride, and PolySi.
- 9 Click OK.
- **IO** Right-click **Difference 2** and choose **Rename**.
- II In the Rename Difference dialog box, type Air in the New label text field.

I2 Click OK.

Resonator Boundaries

- I In the Definitions toolbar, click 🗞 Adjacent.
- 2 In the Settings window for Adjacent, locate the Input Entities section.
- 3 Under Input selections, click + Add.
- 4 In the Add dialog box, select Resonator in the Input selections list.
- 5 Click OK.
- 6 Right-click Adjacent I and choose Rename.
- 7 In the **Rename Adjacent** dialog box, type **Resonator Boundaries** in the **New label** text field.
- 8 Click OK.

Electrode Boundaries

- I In the Definitions toolbar, click 🗞 Adjacent.
- 2 In the Settings window for Adjacent, locate the Input Entities section.
- **3** Under **Input selections**, click + **Add**.
- 4 In the Add dialog box, select Electrode in the Input selections list.
- 5 Click OK.
- 6 Right-click Adjacent 2 and choose Rename.
- 7 In the **Rename Adjacent** dialog box, type Electrode Boundaries in the **New label** text field.
- 8 Click OK.

Nitride Boundaries

- I In the **Definitions** toolbar, click **here** Adjacent.
- 2 In the Settings window for Adjacent, locate the Input Entities section.
- **3** Under **Input selections**, click + **Add**.
- 4 In the Add dialog box, select Nitride in the Input selections list.

- 5 Click OK.
- 6 Right-click Adjacent 3 and choose Rename.
- 7 In the **Rename Adjacent** dialog box, type Nitride Boundaries in the **New label** text field.
- 8 Click OK.

# Geometry Exterior Boundaries

- I In the Definitions toolbar, click 🐂 Adjacent.
- 2 In the Settings window for Adjacent, locate the Input Entities section.
- 3 Under Input selections, click + Add.
- 4 In the Add dialog box, select All domains in the Input selections list.
- 5 Click OK.
- 6 Right-click Adjacent 4 and choose Rename.
- 7 In the Rename Adjacent dialog box, type Geometry Exterior Boundaries in the New label text field.
- 8 Click OK.

# Resonator Exterior Boundaries

- I In the **Definitions** toolbar, click **Difference**.
- 2 In the Settings window for Difference, locate the Geometric Entity Level section.
- **3** From the Level list, choose **Boundary**.
- 4 Locate the Input Entities section. Under Selections to add, click + Add.
- 5 In the Add dialog box, select Resonator Boundaries in the Selections to add list.
- 6 Click OK.
- 7 In the Settings window for Difference, locate the Input Entities section.
- 8 Under Selections to subtract, click + Add.
- **9** In the Add dialog box, select Geometry Exterior Boundaries in the Selections to subtract list.
- IO Click OK.
- II Right-click Difference 3 and choose Rename.
- 12 In the Rename Difference dialog box, type Resonator Exterior Boundaries in the New label text field.
- I3 Click OK.

Electrode Exterior Boundaries

- I In the **Definitions** toolbar, click **Difference**.
- 2 In the Settings window for Difference, locate the Geometric Entity Level section.
- **3** From the Level list, choose **Boundary**.
- 4 Locate the Input Entities section. Under Selections to add, click + Add.
- 5 In the Add dialog box, select Electrode Boundaries in the Selections to add list.
- 6 Click OK.
- 7 In the Settings window for Difference, locate the Input Entities section.
- 8 Under Selections to subtract, click + Add.
- **9** In the Add dialog box, select Geometry Exterior Boundaries in the Selections to subtract list.
- IO Click OK.
- II Right-click Difference 4 and choose Rename.
- 12 In the Rename Difference dialog box, type Electrode Exterior Boundaries in the New label text field.
- I3 Click OK.

Fixed Boundaries

- I In the **Definitions** toolbar, click **Intersection**.
- 2 In the Settings window for Intersection, locate the Geometric Entity Level section.
- **3** From the **Level** list, choose **Boundary**.
- 4 Locate the Input Entities section. Under Selections to intersect, click + Add.
- **5** In the Add dialog box, in the Selections to intersect list, choose Resonator Boundaries and Nitride Boundaries.
- 6 Click OK.
- 7 Right-click Intersection I and choose Rename.
- 8 In the **Rename Intersection** dialog box, type Fixed Boundaries in the **New label** text field.
- 9 Click OK.

#### Symmetry Boundaries

- I In the **Definitions** toolbar, click 🌇 **Box**.
- 2 In the Settings window for Box, locate the Geometric Entity Level section.
- **3** From the Level list, choose **Boundary**.

- 4 Locate the **Box Limits** section. In the **x minimum** text field, type -0.1.
- **5** In the **x maximum** text field, type **0.1**.
- 6 Locate the Output Entities section. From the Include entity if list, choose Entity inside box.
- 7 Right-click Box 7 and choose Rename.
- 8 In the Rename Box dialog box, type Symmetry Boundaries in the New label text field.
- 9 Click OK.

# MATERIALS

Add materials to the model.

## ADD MATERIAL

- I In the Home toolbar, click 🙀 Add Material to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select MEMS>Semiconductors>Si Polycrystalline silicon.
- 4 Click Add to Component in the window toolbar.
- 5 In the tree, select MEMS>Insulators>Si3N4 Silicon nitride.
- 6 Click Add to Component in the window toolbar.
- 7 In the tree, select MEMS>Insulators>SiO2 Silicon oxide.
- 8 Click Add to Component in the window toolbar.
- 9 In the tree, select Built-in>Air.
- **IO** Click **Add to Component** in the window toolbar.
- II In the Home toolbar, click 🙀 Add Material to close the Add Material window.

# MATERIALS

- Si Polycrystalline silicon (mat1)
- I In the Model Builder window, under Component I (compl)>Materials click Si -Polycrystalline silicon (matl).
- 2 In the Settings window for Material, locate the Geometric Entity Selection section.
- 3 From the Selection list, choose PolySi.

#### Si3N4 - Silicon nitride (mat2)

- I In the Model Builder window, click Si3N4 Silicon nitride (mat2).
- 2 In the Settings window for Material, locate the Geometric Entity Selection section.

# 3 From the Selection list, choose Nitride.

## SiO2 - Silicon oxide (mat3)

- I In the Model Builder window, click SiO2 Silicon oxide (mat3).
- 2 In the Settings window for Material, locate the Geometric Entity Selection section.
- **3** From the **Selection** list, choose **Oxide**.

## Air (mat4)

- I In the Model Builder window, click Air (mat4).
- 2 In the Settings window for Material, locate the Geometric Entity Selection section.
- 3 From the Selection list, choose Air.

# SOLID MECHANICS (SOLID)

- I In the Model Builder window, under Component I (compl) click Solid Mechanics (solid).
- 2 In the Settings window for Solid Mechanics, locate the Domain Selection section.
- **3** From the **Selection** list, choose **Resonator**.

# Fixed Constraint I

- I In the Physics toolbar, click 🔚 Boundaries and choose Fixed Constraint.
- 2 In the Settings window for Fixed Constraint, locate the Boundary Selection section.
- **3** From the Selection list, choose Fixed Boundaries.

#### Symmetry I

- I In the Physics toolbar, click 📄 Boundaries and choose Symmetry.
- 2 In the Settings window for Symmetry, locate the Boundary Selection section.
- **3** From the Selection list, choose Symmetry Boundaries.

#### MOVING MESH

Deforming Domain 1

- I In the Model Builder window, under Component I (comp1)>Moving Mesh click Deforming Domain I.
- 2 In the Settings window for Deforming Domain, locate the Domain Selection section.
- 3 From the Selection list, choose Air.

#### Symmetry/Roller 1

- I In the Model Builder window, click Symmetry/Roller I.
- 2 In the Settings window for Symmetry/Roller, locate the Boundary Selection section.

#### 3 From the Selection list, choose Symmetry Boundaries.

# ELECTROSTATICS (ES)

The default **Charge Conservation** feature was set to use solid material type. Add one more feature to represent the nonsolid (air) domains.

I In the Model Builder window, under Component I (compl) click Electrostatics (es).

#### Charge Conservation, Air

- I In the Physics toolbar, click 📄 Domains and choose Charge Conservation.
- 2 In the Settings window for Charge Conservation, type Charge Conservation, Air in the Label text field.
- 3 Locate the Domain Selection section. From the Selection list, choose Air.

With the assumption that the silicon material is a good conductor, use the Domain Terminal feature to ground the resonator. Note: The Domain Terminal feature is very handy in this case, where the conducting domain has a complex shape with many exterior surfaces - instead of selecting all the boundaries to set up the Ground, Terminal, or Electric Potential boundary condition, we only need to select the domain to specify the Domain Terminal with the same effect. In addition, the computation load is reduced, because the electrostatic degrees of freedom within the Domain Terminal do not need to be solved for.

#### Terminal I

- I In the Physics toolbar, click 🔚 Domains and choose Terminal.
- 2 In the Settings window for Terminal, locate the Domain Selection section.
- 3 From the Selection list, choose Resonator.
- 4 Locate the Terminal section. From the Terminal type list, choose Voltage.
- **5** In the  $V_0$  text field, type **0**.

#### Ground I

- I In the Physics toolbar, click 🔚 Boundaries and choose Ground.
- 2 In the Settings window for Ground, locate the Boundary Selection section.
- 3 From the Selection list, choose Ground Plane.

Use the Domain Terminal feature to specify a bias voltage for the electrode domain.

#### Terminal 2

- I In the Physics toolbar, click 🔚 Domains and choose Terminal.
- 2 In the Settings window for Terminal, locate the Domain Selection section.
- **3** From the **Selection** list, choose **Electrode**.

- 4 Locate the Terminal section. From the Terminal type list, choose Voltage.
- **5** In the  $V_0$  text field, type Vdc.

# MESH I

# Free Triangular 1

- I In the Mesh toolbar, click  $\bigwedge$  Boundary and choose Free Triangular.
- 2 In the Settings window for Free Triangular, locate the Boundary Selection section.
- 3 From the Selection list, choose Free Triangular Mesh.
- 4 Click 🖷 Build Selected.

# Swept I

- I In the Mesh toolbar, click As Swept.
- 2 In the Settings window for Swept, click 📗 Build Selected.



# **STATIONARY**

- I In the Model Builder window, right-click Study I and choose Rename.
- 2 In the Rename Study dialog box, type Stationary in the New label text field.
- 3 Click OK.

# **STATIONARY**

I In the Model Builder window, click Stationary.

**2** In the **Home** toolbar, click **= Compute**.

# RESULTS

Mirror 3D I

In the **Results** toolbar, click **More Datasets** and choose **Mirror 3D**.

3D Plot Group 4

- I In the Results toolbar, click 间 3D Plot Group.
- 2 In the Settings window for 3D Plot Group, locate the Data section.
- 3 From the Dataset list, choose Mirror 3D I.

Volume 1

- I Right-click **3D Plot Group 4** and choose **Volume**.
- 2 In the Settings window for Volume, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>Solid Mechanics> Displacement>Displacement field - m>w - Displacement field, Z component.
- **3** Locate the Coloring and Style section. From the Color table transformation list, choose Reverse.

Isosurface I

- I In the Model Builder window, right-click 3D Plot Group 4 and choose Isosurface.
- 2 In the Settings window for Isosurface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>Electrostatics> Electric>V Electric potential V.
- 3 Locate the Levels section. From the Entry method list, choose Levels.
- 4 In the Levels text field, type 10 20 30.
- 5 Locate the Coloring and Style section. From the Color table list, choose Traffic.
- 6 Clear the Color legend check box.

Biased Displacement

- I Right-click 3D Plot Group 4 and choose Rename.
- 2 In the Rename 3D Plot Group dialog box, type Biased Displacement in the New label text field.
- 3 Click OK.

Compare the resulting plot with Figure 2.

# Appendix — Geometry Modeling Instructions

From the File menu, choose New.

#### NEW

In the New window, click 🔦 Blank Model.

# ADD COMPONENT

In the Home toolbar, click 🛞 Add Component and choose 3D.

# GEOMETRY I

- I In the Settings window for Geometry, locate the Units section.
- 2 From the Length unit list, choose µm.

#### Block I (blkI)

- I In the **Geometry** toolbar, click 🗍 **Block**.
- 2 In the Settings window for Block, locate the Size and Shape section.
- 3 In the Width text field, type 38.9.
- 4 In the **Depth** text field, type 12.
- 5 In the **Height** text field, type 4.7.
- 6 Locate the Position section. In the x text field, type -38.9.
- 7 In the y text field, type -6.
- 8 In the z text field, type -1.2.
- 9 Click to expand the Layers section. In the table, enter the following settings:

Layer name	Thickness (µm)
Layer 1	1.5
Layer 2	0.5

10 Find the Layer position subsection. Select the Front check box.

II Select the **Back** check box.

**I2** Clear the **Bottom** check box.

Work Plane I (wp1)

- I In the Geometry toolbar, click 🖶 Work Plane.
- 2 In the Settings window for Work Plane, locate the Plane Definition section.
- 3 From the Plane list, choose zx-plane.

4 In the **y-coordinate** text field, type -6.

Work Plane I (wpI)>Plane Geometry

In the Model Builder window, click Plane Geometry.

Work Plane I (wp1)>Rectangle I (r1)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 0.15.
- 4 In the Height text field, type 38.9.
- 5 Locate the Position section. In the xw text field, type -0.45.
- 6 In the yw text field, type -38.9.

# Work Plane 1 (wp1)>Rectangle 2 (r2)

- I In the Work Plane toolbar, click 📃 Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- **3** In the **Width** text field, type **0.2**.
- 4 In the **Height** text field, type 1.5.
- 5 Locate the Position section. In the xw text field, type -0.3.
- 6 In the **yw** text field, type -36.9.

Work Plane 1 (wp1)>Rectangle 3 (r3)

- I In the Work Plane toolbar, click Mectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 1.9.
- 4 In the **Height** text field, type 1.3.
- **5** Locate the **Position** section. In the **xw** text field, type -0.1.
- 6 In the **yw** text field, type -36.9.

Work Plane I (wp1)>Rectangle 4 (r4)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- **3** In the **Width** text field, type **1.9**.
- 4 In the **Height** text field, type 0.7.
- **5** Locate the **Position** section. In the **xw** text field, type **0.2**.
- 6 In the yw text field, type -35.6.

Work Plane 1 (wp1)>Rectangle 5 (r5)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- **3** In the **Width** text field, type **1.9**.
- **4** In the **Height** text field, type 14.
- 5 Locate the Position section. In the yw text field, type -34.9.

Work Plane I (wp1)>Rectangle 6 (r6)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- **3** In the **Width** text field, type **1.9**.
- 4 In the **Height** text field, type 0.7.
- **5** Locate the **Position** section. In the **xw** text field, type **0.2**.
- 6 In the **yw** text field, type -20.9.

Work Plane I (wp1)>Rectangle 7 (r7)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- **3** In the **Width** text field, type **0.2**.
- 4 In the **Height** text field, type 0.7.
- 5 Locate the Position section. In the yw text field, type -20.9.

Work Plane I (wp1)>Rectangle 8 (r8)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- **3** In the **Width** text field, type **1.9**.
- **4** In the **Height** text field, type 10.
- **5** Locate the **Position** section. In the **xw** text field, type -0.1.
- 6 In the yw text field, type -20.2.

Work Plane 1 (wp1)>Rectangle 9 (r9)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- **3** In the **Width** text field, type **0.2**.
- 4 In the **Height** text field, type 10.4.

- **5** Locate the **Position** section. In the **xw** text field, type -0.3.
- 6 In the **yw** text field, type -20.4.

Work Plane I (wpI)>Rectangle IO (rIO)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 0.3.
- 4 In the **Height** text field, type 0.2.
- **5** Locate the **Position** section. In the **xw** text field, type -0.1.
- 6 In the **yw** text field, type -10.2.

Work Plane I (wpl)>Rectangle II (rII)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- **3** In the **Width** text field, type **0.2**.
- **4** In the **Height** text field, type 10.
- **5** Locate the **Position** section. In the **yw** text field, type -10.

Work Plane I (wp1)>Rectangle I2 (r12)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- **3** In the **Width** text field, type **1.9**.
- 4 In the **Height** text field, type 10.2.
- **5** Locate the **Position** section. In the **xw** text field, type **0.2**.
- 6 In the **yw** text field, type -10.2.

Work Plane I (wp1)>Rectangle I3 (r13)

- I In the Work Plane toolbar, click 🔲 Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- **3** In the **Width** text field, type **0.1**.
- 4 In the **Height** text field, type 0.2.
- 5 Locate the Position section. In the xw text field, type -0.1.
- 6 In the **yw** text field, type -20.4.

Work Plane I (wpI)>Rectangle I4 (rI4)

I In the Work Plane toolbar, click Rectangle.

- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 0.3.
- 4 In the **Height** text field, type 0.2.
- 5 Locate the Position section. In the xw text field, type -0.1.
- 6 In the yw text field, type -35.6.

#### Work Plane I (wpI)>Rectangle 15 (r15)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- **3** In the **Width** text field, type **0.2**.
- 4 In the **Height** text field, type 0.5.
- 5 Locate the Position section. In the yw text field, type -35.4.

#### Work Plane I (wp1)>Union I (uni1)

- I In the Work Plane toolbar, click 🔲 Booleans and Partitions and choose Union.
- 2 Select the objects r12, r3, r4, r5, r6, and r8 only.
- 3 In the Settings window for Union, locate the Union section.
- 4 Clear the Keep interior boundaries check box.

# Work Plane I (wp1)>Union 2 (uni2)

- I In the Work Plane toolbar, click 🔲 Booleans and Partitions and choose Union.
- 2 Select the objects r10, r11, r13, r14, r15, r2, r7, and r9 only.
- 3 In the Settings window for Union, locate the Union section.
- 4 Clear the Keep interior boundaries check box.

#### Extrude I (extI)

- In the Model Builder window, under Component I (compl)>Geometry I right-click
  Work Plane I (wpl) and choose Extrude.
- 2 In the Settings window for Extrude, locate the Distances section.
- 3 In the table, enter the following settings:

#### Distances (µm)

#### 12

Form Union (fin)

- I In the Model Builder window, click Form Union (fin).
- 2 In the Settings window for Form Union/Assembly, click 틤 Build Selected.

#### Geometry

- I In the Geometry toolbar, click 👫 Selections and choose Explicit Selection.
- 2 In the Settings window for Explicit Selection, type Geometry in the Label text field.
- **3** Locate the **Entities to Select** section. From the **Geometric entity level** list, choose **Object**.
- **4** Select the object **fin** only.

# Ground Plane

- I In the Geometry toolbar, click 🗞 Selections and choose Box Selection.
- 2 In the Settings window for Box Selection, type Ground Plane in the Label text field.
- 3 Locate the Geometric Entity Level section. From the Level list, choose Boundary.
- 4 Locate the Box Limits section. In the z minimum text field, type -2.
- **5** In the **z maximum** text field, type -1.
- 6 Locate the Output Entities section. From the Include entity if list, choose Entity inside box.

#### Oxide

- I In the Geometry toolbar, click 🛯 Selections and choose Box Selection.
- 2 In the Settings window for Box Selection, type Oxide in the Label text field.
- 3 Locate the Box Limits section. In the z minimum text field, type -1.
- **4** In the **z maximum** text field, type -0.9.

## Nitride

- I In the Geometry toolbar, click 🗞 Selections and choose Box Selection.
- 2 In the Settings window for Box Selection, type Nitride in the Label text field.
- **3** Locate the **Box Limits** section. In the **z minimum** text field, type -0.4.
- **4** In the **z maximum** text field, type -0.35.

# Electrode

- I In the Geometry toolbar, click 🛯 Selections and choose Box Selection.
- 2 In the Settings window for Box Selection, type Electrode in the Label text field.
- **3** Locate the **Box Limits** section. In the **x minimum** text field, type -0.1.
- 4 In the **x maximum** text field, type 0.1.
- **5** In the **y minimum** text field, type -4.2.
- 6 In the **z minimum** text field, type -0.15.
- 7 In the **z maximum** text field, type -0.1.

Ball Selection I (ballsel1)

- I In the Geometry toolbar, click 🔓 Selections and choose Ball Selection.
- 2 In the Settings window for Ball Selection, locate the Ball Center section.
- **3** In the **z** text field, type 1.
- 4 Locate the Ball Radius section. In the Radius text field, type 0.1.

Box Selection 5 (boxsel5)

- I In the Geometry toolbar, click 🗞 Selections and choose Box Selection.
- 2 In the Settings window for Box Selection, locate the Box Limits section.
- 3 In the **y maximum** text field, type 4.8.
- 4 In the z minimum text field, type -0.35.
- 5 In the z maximum text field, type 0.05.
- 6 Locate the Output Entities section. From the Include entity if list, choose Entity inside box.

Box Selection 6 (boxsel6)

- I In the Geometry toolbar, click 🛯 Selections and choose Box Selection.
- 2 In the Settings window for Box Selection, locate the Box Limits section.
- 3 In the x minimum text field, type -15.
- 4 In the **x maximum** text field, type 15.
- 5 In the **y maximum** text field, type 4.8.
- 6 In the z minimum text field, type -0.35.
- 7 In the **z maximum** text field, type 0.05.
- 8 Locate the Output Entities section. From the Include entity if list, choose Entity inside box.

Resonator

- I In the Geometry toolbar, click 🔓 Selections and choose Difference Selection.
- 2 In the Settings window for Difference Selection, locate the Input Entities section.
- 3 Click + Add.
- 4 In the Add dialog box, in the Selections to add list, choose Ball Selection I and Box Selection 5.
- 5 Click OK.
- 6 In the Settings window for Difference Selection, locate the Input Entities section.
- 7 Click + Add.

8 In the Add dialog box, select Box Selection 6 in the Selections to subtract list.

9 Click OK.

IO In the Settings window for Difference Selection, type Resonator in the Label text field.

PolySi

- I In the Geometry toolbar, click 🔓 Selections and choose Union Selection.
- 2 In the Settings window for Union Selection, locate the Input Entities section.
- 3 Click + Add.
- 4 In the Add dialog box, in the Selections to add list, choose Electrode and Resonator.
- 5 Click OK.
- 6 In the Settings window for Union Selection, type PolySi in the Label text field.

Air

- I In the Geometry toolbar, click 🝖 Selections and choose Difference Selection.
- 2 In the Settings window for Difference Selection, type Air in the Label text field.
- **3** Locate the **Input Entities** section. Click + Add.
- 4 In the Add dialog box, select Geometry in the Selections to add list.
- 5 Click OK.
- 6 In the Settings window for Difference Selection, locate the Input Entities section.
- 7 Click + Add.
- 8 In the Add dialog box, in the Selections to subtract list, choose Oxide, Nitride, and PolySi.
- 9 Click OK.

# **Resonator Boundaries**

- I In the Geometry toolbar, click he Selections and choose Adjacent Selection.
- 2 In the Settings window for Adjacent Selection, type Resonator Boundaries in the Label text field.
- 3 Locate the Input Entities section. Click + Add.
- 4 In the Add dialog box, select Resonator in the Input selections list.
- 5 Click OK.

# Electrode Boundaries

- I In the Geometry toolbar, click 🖓 Selections and choose Adjacent Selection.
- 2 In the Settings window for Adjacent Selection, type Electrode Boundaries in the Label text field.

- **3** Locate the **Input Entities** section. Click + **Add**.
- 4 In the Add dialog box, select Electrode in the Input selections list.
- 5 Click OK.

# Nitride Boundaries

- I In the Geometry toolbar, click 😼 Selections and choose Adjacent Selection.
- **2** In the **Settings** window for **Adjacent Selection**, type Nitride Boundaries in the **Label** text field.
- **3** Locate the **Input Entities** section. Click + Add.
- 4 In the Add dialog box, select Nitride in the Input selections list.
- 5 Click OK.

# Geometry Exterior Boundaries

- I In the Geometry toolbar, click 🔓 Selections and choose Adjacent Selection.
- 2 In the Settings window for Adjacent Selection, locate the Input Entities section.
- 3 Click + Add.
- 4 In the Add dialog box, select Geometry in the Input selections list.
- 5 Click OK.
- **6** In the **Settings** window for **Adjacent Selection**, type Geometry Exterior Boundaries in the **Label** text field.

## Resonator Exterior Boundaries

- I In the Geometry toolbar, click 🝖 Selections and choose Difference Selection.
- 2 In the Settings window for Difference Selection, locate the Geometric Entity Level section.
- **3** From the **Level** list, choose **Boundary**.
- 4 In the Label text field, type Resonator Exterior Boundaries.
- 5 Locate the Input Entities section. Click + Add.
- 6 In the Add dialog box, select Resonator Boundaries in the Selections to add list.
- 7 Click OK.
- 8 In the Settings window for Difference Selection, locate the Input Entities section.
- 9 Click + Add.
- **10** In the **Add** dialog box, select **Geometry Exterior Boundaries** in the **Selections to subtract** list.
- II Click OK.

# Electrode Exterior Boundaries

- I In the Geometry toolbar, click 🐚 Selections and choose Difference Selection.
- 2 In the Settings window for Difference Selection, type Electrode Exterior Boundaries in the Label text field.
- 3 Locate the Geometric Entity Level section. From the Level list, choose Boundary.
- 4 Locate the Input Entities section. Click + Add.
- 5 In the Add dialog box, select Electrode Boundaries in the Selections to add list.
- 6 Click OK.
- 7 In the Settings window for Difference Selection, locate the Input Entities section.
- 8 Click + Add.
- **9** In the Add dialog box, select Geometry Exterior Boundaries in the Selections to subtract list.

IO Click OK.

Fixed Boundaries

- I In the Geometry toolbar, click 🔓 Selections and choose Intersection Selection.
- **2** In the **Settings** window for **Intersection Selection**, type Fixed Boundaries in the **Label** text field.
- 3 Locate the Geometric Entity Level section. From the Level list, choose Boundary.
- 4 Locate the Input Entities section. Click + Add.
- 5 In the Add dialog box, in the Selections to intersect list, choose Nitride Boundaries and Resonator Exterior Boundaries.
- 6 Click OK.

Symmetry Boundaries

- I In the Geometry toolbar, click 🗞 Selections and choose Box Selection.
- 2 In the Settings window for Box Selection, type Symmetry Boundaries in the Label text field.
- **3** Locate the **Geometric Entity Level** section. From the **Level** list, choose **Boundary**.
- 4 Locate the Box Limits section. In the x minimum text field, type -0.1.
- **5** In the **x maximum** text field, type **0.1**.
- 6 Locate the Output Entities section. From the Include entity if list, choose Entity inside box.

# Free Triangular Mesh

- I In the Geometry toolbar, click 🛯 🔓 Selections and choose Explicit Selection.
- 2 In the Settings window for Explicit Selection, locate the Entities to Select section.
- **3** From the **Geometric entity level** list, choose **Boundary**.
- **4** Select the **Group by continuous tangent** check box.
- 5 In the Label text field, type Free Triangular Mesh.
- 6 On the object fin, select Boundaries 2, 5, 8, 55, 58, 112, 163, and 254 only.