

Modeling Vibration in an Induction Motor

Introduction

This model simulates the electro-mechanical effects in a three phase induction motor. The assembly consists of stator, rotor and housing. In this example, the eddy currents are induced in the rotor by the time harmonic currents on the stator windings and the rotation of the rotor. The air gap between the rotor and stator is assumed asymmetric and the resulting vibrations in the motor are analyzed.

The electromagnetic simulation of an induction motor is performed in 2D whereas the multibody dynamics simulation is performed in 3D. The rotational torque, when an alternating current is passed through the stator windings, is calculated as a function of time. It is used in the multibody dynamics model in order to compute the angular speed of the rotor.

Note: This model requires the AC/DC Module and the Multibody Dynamics Module.

Model Definition

The three phase induction motor-housing assembly is shown in Figure 1.

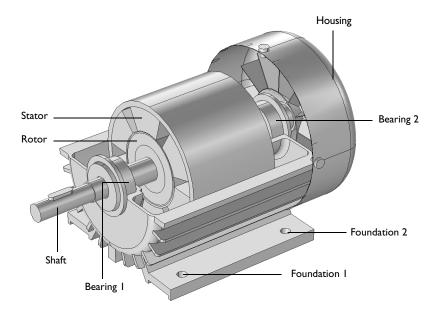


Figure 1: The geometry of a three phase induction motor-housing assembly.

The induction motor modeled in this example has the following parts:

- Stator
- Rotor
- Shaft
- Housing
- Bearings
- Foundation

All parts, except the bearings and foundation, are physically modeled. The latter are modeled as massless springs.

The model uses two different physics interfaces:

- Rotating Machinery interface to simulate the electromagnetic fields in the motor.
- Multibody Dynamics interface to simulate the motion of the rotor and vibration in the housing.

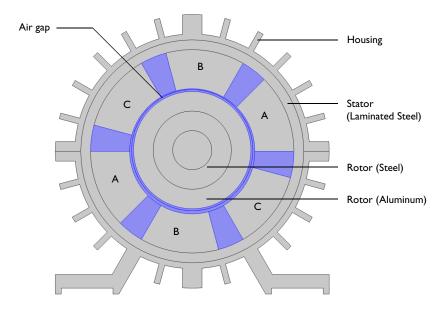


Figure 2: Cross sectional view of three phase induction motor showing stator, rotor, and the housing. The figure shows three different coil regions A, B, and C in the stator representing three phases of the motor. The air gap between the stator and rotor is also highlighted.

ELECTROMAGNETIC MODEL DESCRIPTION

The electromagnetic field equations are solved in a transverse section of the induction motor as shown in Figure 2. In the electromagnetic simulation, only the following parts are considered:

- Stator
- Rotor
- Air gap

The stator is made of steel. The stator steel is laminated and its conductivity is zero. The inner part of the rotor is made of steel and outer part is made of aluminum and they have the conductivity of $1.6 \cdot 10^6$ S/m and $3.74 \cdot 10^7$ S/m respectively. There exists a slight misalignment between the rotor and stator, making the air gap asymmetric.

Each of the three phases of the stator winding spans 45 degrees and they are separated by 120 electrical degrees. The alternating current (60 Hz) through the stator windings is applied using a homogenized multiturn coil feature with 2045 turns. The geometrical

dimensions for this model are obtained from Ref. 1. More details about the electromagnetic model can be found in Ref. 2.

MULTIBODY DYNAMICS MODEL DESCRIPTION

In the multibody dynamics model, the stator, rotor, and shaft are considered to be rigid. The rotor is rigidly mounted on the shaft. The bearings are modeled by elastic hinge joints between the rotor and housing. The bearings are responsible for supporting the rotor and in turn transmitting the forces to the housing. The housing is assumed elastic and made of structural steel. The housing is supported on the foundation using elastic fixed joints. The bearing and foundation stiffness parameters are given the table below.

TABLE I: BEARING AND FOUNDATION PARAMETERS

PARAMETER	VALUE
Bearing translational stiffness (kb)	$1\cdot10^6$ N/m
Bearing rotational stiffness (kbr)	$1\cdot10^4$ Nm/rad
Foundation translational stiffness (kf)	$1\cdot10^6$ N/m
Foundation rotational stiffness (kfr)	$1\cdot10^4$ Nm/rad

ELECTROMAGNETIC-MULTIBODY DYNAMICS COUPLING

Electromagnetic Torque

The electromagnetic torque calculated in the Rotating Machinery interface is applied on the rotor as well as on the stator in the Multibody Dynamics interface. As the rotor is free to rotate about its own axis, it starts accelerating by overcoming the inertial resistance. The reaction torque on the stator bends the motor-housing assembly in the direction opposite to the rotor rotation.

Rotor Speed

The rotor speed calculated using the angular motion of the hinge joint in the Multibody Dynamics interface is transferred to the Rotating Machinery interface.

Electromagnetic Forces

In addition to the above, the misalignment between the stator and rotor also causes nonzero resultant electromagnetic forces. These forces calculated in the Rotating Machinery interface are also applied to the rotor and stator in the Multibody Dynamics interface. Since these forces are oscillating in nature, the cause vibrations in the motor.

A transient analysis is performed to calculate the torque, speed, and vibration in an induction motor. The magnetic flux density norm in the rotor and stator coils at a particular instant is shown in Figure 3.

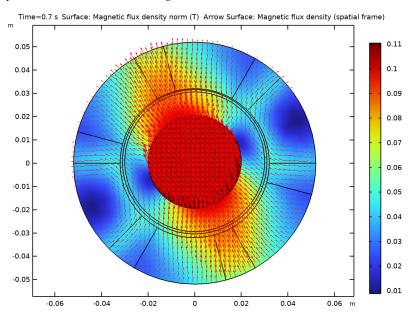


Figure 3: Magnetic flux density in the rotor and stator at t = 0.7 s.

The von Mises stress distribution in the housing together with the velocity of the rotor is shown in Figure 4. It can be seen that the stress values are higher near the bearing and at the connection between the housing and the foundation.

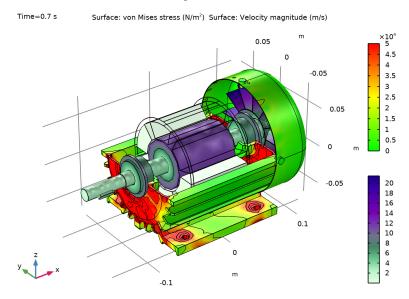


Figure 4: von Mises stress distribution in the housing and the rotor velocity profile at t = 0.7 s.

Figure 5 illustrates the electromagnetic torque as a function of time. It can be seen that in the absence of any loading torque on the shaft, the electromagnetic torque goes to zero as the rotor achieves the speed equal to the stator electrical frequency (60 Hz).

The angular speed of the rotor as a function of time is shown in Figure 6. It can be seen that it takes 0.7 seconds for the rotor to reach the steady state speed. The time delay for the rotor speed to reach the stator electrical frequency depends on the inertia of the rotor.

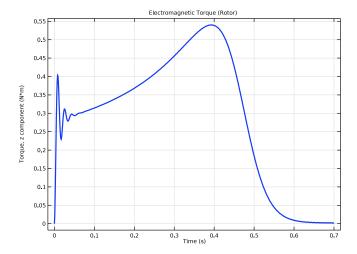


Figure 5: Electromagnetic torque in the rotor as a function of time.

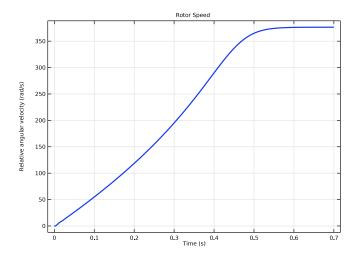


Figure 6: Rotor angular speed as a function of time.

Figure 7 shows the electromagnetic forces experienced by the rotor as a function of time. These vibrating forces in the transverse direction of the rotor are caused by the misalignment between the stator and rotor.

The frequency spectrum of electromagnetic forces can be seen in Figure 8. It is clear that the frequency of these forces is 120 Hz which is twice the stator electrical frequency.

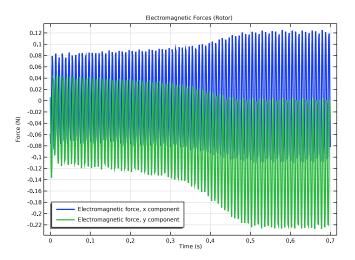


Figure 7: Electromagnetic forces in the rotor in transverse and axial directions.

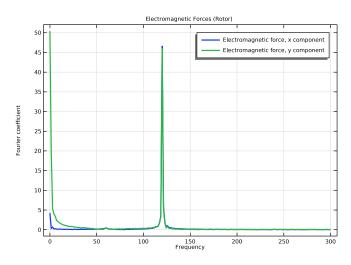


Figure 8: Frequency spectrum of electromagnetic forces in the rotor.

The forces experienced by the bearings on both sides as a function of time are shown in Figure 9 and Figure 10. These forces are transmitted to the foundation through elastic housing. The foundation forces as a function of time at one of the locations are shown in Figure 11. The frequency spectrum of the same forces can be seen in Figure 12.

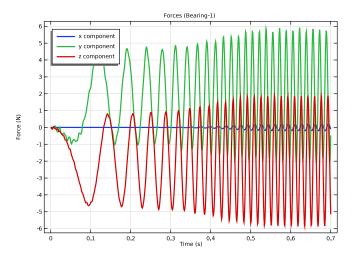


Figure 9: Forces in bearing-1 in transverse and axial directions.

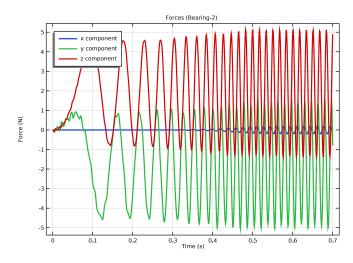


Figure 10: Forces in bearing-2 in transverse and axial directions.

Note that the dominant frequency contribution is centered around 60 Hz in spite of the electromagnetic forces having a frequency of 120 Hz. Small peaks can also be seen around 83 Hz which is the first natural frequency of the induction motor-housing assembly.

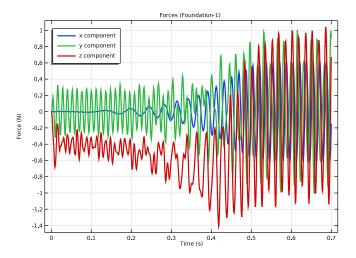


Figure 11: Forces in the housing-foundation connection at one of the locations.

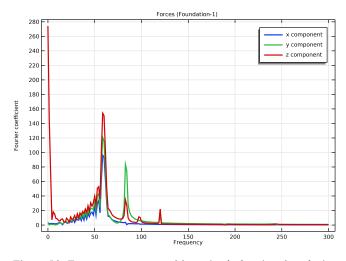


Figure 12: Frequency spectrum of forces in the housing-foundation connection.

As the electromagnetic forces are acting on the rotor in the transverse direction, and the bearings supporting the rotor at the ends have finite stiffness, rotor starts vibrating in the transverse direction with respect to the stator. This orbital motion, a combination of rotation and vibration, of the rotor at both the bearing locations is shown in Figure 13. Note that the orbits are not concentric because of the asymmetry in the inertia of the rotor in the axial direction.

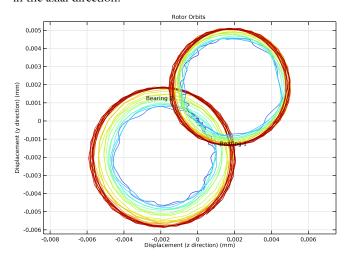


Figure 13: Orbital motion of the rotor at bearing locations.

Notes About the COMSOL Implementation

- The 2D geometry of the induction motor is the cross section of the 3D geometry. The length of the 2D geometry in the out-of-plane direction in the Rotating Machinery interface is set to the length of the rotor in the 3D geometry.
- The 2D geometry has stationary and rotating domains. As it is finalized with the assembly option, an identity pair forms automatically between the stationary and rotating domains.
- For faster computation, linear shape functions are used instead of the default quadratic shape functions for the magnetic vector potential.
- Some parts having comparatively higher structural stiffness are modeled as rigid elements using the Rigid Domain material model. The remaining parts are assumed flexible and modeled using Linear Elastic Material.

References

- 1. K. Davey, "Induction Motor Analysis: International TEAM Workshop Problem 30," http://www.compumag.org/jsite/images/stories/TEAM/problem30a.pdf.
- 2. Induction Motor in 2D, COMSOL Application, https://www.comsol.com/model/ download/347241/induction_motor_2d.pdf.

Application Library path: Multibody Dynamics Module/Electrical Machinery/ induction_motor_vibration/

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click **2** 2D.
- 2 In the Select Physics tree, select AC/DC>Electromagnetics and Mechanics> Rotating Machinery, Magnetic (rmm).
- 3 Click Add.
- 4 Click Study.
- 5 In the Select Study tree, select General Studies>Time Dependent.
- 6 Click **Done**.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click Load from File.
- 4 Browse to the model's Application Libraries folder and double-click the file induction motor vibration parameters.txt.

Import the 3D geometry of an induction motor in a 3D Component and then create 2D geometry using **Cross Section** functionality.

ADD COMPONENT

In the Model Builder window, right-click the root node and choose Add Component>3D.

GEOMETRY 2

Import I (impl)

- I In the Home toolbar, click Figure Import.
- 2 In the Settings window for Import, locate the Import section.
- 3 Click **Browse**.
- 4 Browse to the model's Application Libraries folder and double-click the file induction_motor_vibration.mphbin.

Work Plane I (wbl)

- I In the Geometry toolbar, click Work Plane.
- 2 In the Settings window for Work Plane, locate the Plane Definition section.
- 3 From the Plane list, choose yz-plane.

Form Union (fin)

- I In the Model Builder window, under Component 2 (comp2)>Geometry 2 click Form Union (fin).
- 2 In the Settings window for Form Union/Assembly, locate the Form Union/Assembly section.
- 3 From the Action list, choose Form an assembly.
- 4 Clear the Create pairs check box.
- 5 In the Geometry toolbar, click **Build All**.

GEOMETRY I

In the Model Builder window, under Component I (compl) click Geometry I.

Cross Section I (cro1)

In the Geometry toolbar, click A Cross Section.

Form Union (fin)

- I In the Model Builder window, under Component I (compl)>Geometry I click Form Union (fin).
- 2 In the Settings window for Form Union/Assembly, locate the Form Union/Assembly section.

- 3 From the Action list, choose Form an assembly.
- 4 In the Geometry toolbar, click iii Build All.

DEFINITIONS (COMPI)

Variables 1

- I In the Model Builder window, expand the Component I (compl)>Definitions node.
- 2 Right-click Component I (compl)>Definitions and choose Variables.
- 3 In the Settings window for Variables, locate the Variables section.
- **4** In the table, enter the following settings:

Name	Expression	Unit	Description
Ia	1[A]*sqrt(2)*cos(w0*t)	Α	Current on phase A
Ib	1[A]*sqrt(2)*cos(w0*t+ 120[deg])	Α	Current on phase B
Ic	1[A]*sqrt(2)*cos(w0*t- 120[deg])	Α	Current on phase C

Assign materials to the different parts of the motor.

ADD MATERIAL

- I In the Home toolbar, click **‡ Add Material** to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Built-in>Air.
- 4 Click Add to Component in the window toolbar.
- 5 In the tree, select Built-in>Aluminum.
- **6** Click **Add to Component** in the window toolbar.
- 7 In the Home toolbar, click 👯 Add Material to close the Add Material window.

MATERIALS

Aluminum (mat2)

Select Domain 18 only.

Steel: Rotor

- I In the Model Builder window, right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type Steel: Rotor in the Label text field.
- **3** Select Domains 19 and 20 only.

4 Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Variable Value		Property group	
Relative permeability	mur_iso; murii = mur_iso, murij = 0	30	I	Basic	
Electrical conductivity	sigma_iso; sigmaii = sigma_iso, sigmaij = 0	1.6e6[S /m]	S/m	Basic	
Relative permittivity	epsilonr_iso; epsilonrii = epsilonr_iso, epsilonrij = 0	1	I	Basic	

Steel: Stator

- I Right-click Steel: Rotor and choose Duplicate.
- 2 In the Settings window for Material, type Steel: Stator in the Label text field.
- 3 Locate the Geometric Entity Selection section. Click Clear Selection.
- **4** Select Domain 15 only.
- **5** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group	
Relative permeability	mur_iso; murii = mur_iso, murij = 0	30		Basic	
Electrical conductivity	sigma_iso ; sigmaii = sigma_iso, sigmaij = 0	0[S/m]	S/m	Basic	
Relative permittivity	epsilonr_iso; epsilonrii = epsilonr_iso, epsilonrij = 0	1	I	Basic	

ROTATING MACHINERY, MAGNETIC (RMM)

I In the Model Builder window, under Component I (compl) click Rotating Machinery, Magnetic (rmm).

- 2 Select Domains 3–20 only.
- 3 In the Settings window for Rotating Machinery, Magnetic, locate the Thickness section.
- **4** In the *d* text field, type L.
- 5 Click to expand the Discretization section. From the Magnetic vector potential list, choose Linear.

Coil: Phase A

- I In the Physics toolbar, click **Domains** and choose **Coil**.
- 2 In the Settings window for Coil, type Coil: Phase A in the Label text field.
- **3** Select Domains 4 and 13 only.
- 4 Locate the Coil section. From the Conductor model list, choose Homogenized multiturn.
- **5** Select the **Coil group** check box.
- **6** In the I_{coil} text field, type Ia.
- 7 Locate the Homogenized Multiturn Conductor section. In the N text field, type n0.

Reversed Current Direction I

- I In the Physics toolbar, click 🕞 Attributes and choose Reversed Current Direction.
- 2 Select Domain 13 only.

Coil: Phase B

- I In the Model Builder window, right-click Coil: Phase A and choose Duplicate.
- 2 In the Settings window for Coil, type Coil: Phase B in the Label text field.
- 3 Locate the Domain Selection section. Click Clear Selection.
- **4** Select Domains 7 and 9 only.
- **5** Locate the **Coil** section. In the I_{coil} text field, type Ib.

Reversed Current Direction 1

- I In the Model Builder window, expand the Coil: Phase B node, then click Reversed Current Direction 1.
- 2 In the Settings window for Reversed Current Direction, locate the Domain Selection section.
- 3 Click Clear Selection.
- 4 Select Domain 7 only.

Coil: Phase C

I In the Model Builder window, right-click Coil: Phase B and choose Duplicate.

- 2 In the Settings window for Coil, type Coil: Phase C in the Label text field.
- 3 Locate the Domain Selection section. Click Clear Selection.
- 4 Select Domains 5 and 11 only.
- **5** Locate the **Coil** section. In the I_{coil} text field, type Ic.

Reversed Current Direction 1

- I In the Model Builder window, expand the Coil: Phase C node, then click Reversed Current Direction 1.
- 2 In the Settings window for Reversed Current Direction, locate the Domain Selection section.
- 3 Click Clear Selection.
- 4 Select Domain 5 only.

Continuity Ia

- I In the Physics toolbar, click Pairs and choose Continuity.
- 2 In the Settings window for Continuity, locate the Pair Selection section.
- 3 Under Pairs, click + Add.
- 4 In the Add dialog box, select Identity Boundary Pair I (ap I) in the Pairs list.
- 5 Click OK.

Force Calculation: Rotor

- I In the Physics toolbar, click **Domains** and choose Force Calculation.
- 2 In the Settings window for Force Calculation, type Force Calculation: Rotor in the Label text field.
- **3** Locate the **Force Calculation** section. In the **Force name** text field, type **Rotor**.
- **4** Specify the \mathbf{r}_0 vector as



5 Select Domains 18–20 only.

Force Calculation: Stator

- I Right-click Force Calculation: Rotor and choose Duplicate.
- 2 In the Settings window for Force Calculation, type Force Calculation: Stator in the Label text field.
- 3 Locate the Force Calculation section. In the Force name text field, type Stator.

4 Specify the \mathbf{r}_0 vector as

0	×
0	у

- 5 Locate the Domain Selection section. Click Clear Selection.
- 6 Select Domains 3–15 only.

MESH I

- I In the Model Builder window, under Component I (compl) click Mesh I.
- 2 In the Settings window for Mesh, locate the Sequence Type section.
- 3 From the list, choose User-controlled mesh.

Size

- I In the Model Builder window, under Component I (compl)>Mesh I click Size.
- 2 In the Settings window for Size, locate the Element Size section.
- 3 From the Predefined list, choose Extra coarse.

Size 1

- I In the Model Builder window, right-click Free Triangular I and choose Size.
- 2 In the Settings window for Size, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 Select Domains 18–20 only.
- **5** Locate the **Element Size** section. From the **Predefined** list, choose **Finer**.

Size 2

- I Right-click Size I and choose Duplicate.
- 2 In the Settings window for Size, locate the Geometric Entity Selection section.
- 3 Click Clear Selection.
- 4 Click Paste Selection.
- 5 In the Paste Selection dialog box, type 17 in the Selection text field.
- 6 Click OK.
- 7 In the Settings window for Size, locate the Element Size section.
- 8 Click the **Custom** button.
- 9 Locate the Element Size Parameters section. Select the Maximum element size check box.
- 10 In the associated text field, type 0.00075.

Size 3

- I Right-click Size 2 and choose Duplicate.
- 2 In the Settings window for Size, locate the Geometric Entity Selection section.
- 3 Click Clear Selection.
- 4 Click Paste Selection.
- 5 In the Paste Selection dialog box, type 16 in the Selection text field.
- 6 Click OK.
- 7 In the Settings window for Size, locate the Element Size Parameters section.
- 8 In the Maximum element size text field, type 0.00125.

Boundary Layers 1

- I In the Mesh toolbar, click Boundary Layers.
- 2 In the Settings window for Boundary Layers, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 Select Domain 19 only.

Boundary Layer Properties

- I In the Model Builder window, click Boundary Layer Properties.
- 2 In the Settings window for Boundary Layer Properties, locate the Boundary Selection section.
- 3 Click Paste Selection.
- 4 In the Paste Selection dialog box, type 163 164 in the Selection text field.
- 5 Click OK.

Boundary Layers 2

- I In the Mesh toolbar, click Boundary Layers.
- 2 In the Settings window for Boundary Layers, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 Select Domain 18 only.

Boundary Layer Properties

- I In the Model Builder window, click Boundary Layer Properties.
- 2 In the Settings window for Boundary Layer Properties, locate the Boundary Selection section.
- 3 Click Paste Selection.
- 4 In the Paste Selection dialog box, type 161 162 in the Selection text field.

5 Click OK.

Next, add a Multibody Dynamics interface to the 3D component.

COMPONENT 2 (COMP2)

In the Model Builder window, click Component 2 (comp2).

ADD PHYSICS

- I In the Home toolbar, click Add Physics to open the Add Physics window.
- **2** Go to the **Add Physics** window.
- 3 In the tree, select Structural Mechanics>Multibody Dynamics (mbd).
- 4 Click Add to Component 2 in the window toolbar.
- 5 In the Home toolbar, click Add Physics to close the Add Physics window.

MULTIBODY DYNAMICS (MBD)

- I Click the **Click and Hide** button in the **Graphics** toolbar.
- 2 Select Domain 14 only.
- 3 Click the **Click and Hide** button in the **Graphics** toolbar.
- **4** Select Domains 1–4, 6–15, 17, 18, 21, 23, 25, 27, and 29–36 only.

ADD MATERIAL

- I In the Home toolbar, click Radd Material to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Built-in>Structural steel.
- 4 Click Add to Component in the window toolbar.
- 5 In the tree, select Built-in>Aluminum.
- **6** Click **Add to Component** in the window toolbar.
- 7 In the Home toolbar, click **4** Add Material to close the Add Material window.

MATERIALS

Aluminum (mat6)

- I In the Settings window for Material, locate the Geometric Entity Selection section.
- 2 Click Paste Selection.
- 3 In the Paste Selection dialog box, type 6 in the Selection text field.
- 4 Click OK.

MULTIBODY DYNAMICS (MBD)

Add Rigid Domain nodes for modeling the rotor and stator. Also apply electromagnetic torque and forces on both parts.

I In the Model Builder window, under Component 2 (comp2) click Multibody Dynamics (mbd).

Rigid Domain: Rotor with Shaft

- I In the Physics toolbar, click **Domains** and choose Rigid Domain.
- 2 In the Settings window for Rigid Domain, type Rigid Domain: Rotor with Shaft in the Label text field.
- 3 Locate the Domain Selection section. Click Paste Selection.
- 4 In the Paste Selection dialog box, type 1-4, 6-12 in the Selection text field.
- 5 Click OK.

Applied Force 1

- I In the Physics toolbar, click 🕞 Attributes and choose Applied Force.
- 2 In the Settings window for Applied Force, locate the Location section.
- 3 From the list, choose Centroid of selected entities.

Location: Boundary 1

- I In the Model Builder window, expand the Applied Force I node, then click Location: Boundary I.
- 2 In the Settings window for Location: Boundary, locate the Boundary Selection section.
- 3 Click Paste Selection.
- 4 In the Paste Selection dialog box, type 45 53 in the Selection text field.
- 5 Click OK.

Applied Force 1

- I In the Model Builder window, click Applied Force I.
- 2 In the Settings window for Applied Force, locate the Applied Force section.
- **3** Specify the \mathbf{F} vector as

0	x
comp1.rmm.Forcex_Rotor	у
comp1.rmm.Forcey_Rotor	z

Rigid Domain: Rotor with Shaft

In the Model Builder window, click Rigid Domain: Rotor with Shaft.

Applied Moment 1

- I In the Physics toolbar, click 🦳 Attributes and choose Applied Moment.
- 2 In the Settings window for Applied Moment, locate the Applied Moment section.
- **3** Specify the **M** vector as

comp1.rmm.Tz_Rotor	x
0	у
0	z

Rigid Domain: Stator

- I In the Physics toolbar, click **Domains** and choose Rigid Domain.
- 2 In the Settings window for Rigid Domain, type Rigid Domain: Stator in the Label text field.
- 3 Locate the Domain Selection section. Click Paste Selection.
- 4 In the Paste Selection dialog box, type 15, 17-18, 21, 23, 25, 27 in the Selection text field.
- 5 Click OK.

Applied Force 1

- I In the Physics toolbar, click 🕞 Attributes and choose Applied Force.
- 2 In the Settings window for Applied Force, locate the Applied Force section.
- **3** Specify the \mathbf{F} vector as



Rigid Domain: Stator

In the Model Builder window, click Rigid Domain: Stator.

Applied Moment 1

- I In the Physics toolbar, click 🕞 Attributes and choose Applied Moment.
- 2 In the Settings window for Applied Moment, locate the Applied Moment section.

3 Specify the **M** vector as

comp1.rmm.Tz_Stator	x
0	у
0	z

Next is to define the rotor-housing and housing-foundation connections using elastic Hinge Joints and Fixed Joints respectively.

Attachment: Bearing I

- I In the Physics toolbar, click **Boundaries** and choose **Attachment**.
- 2 In the Settings window for Attachment, type Attachment: Bearing 1 in the Label text field.
- 3 Locate the Boundary Selection section. Click Paste Selection.
- 4 In the Paste Selection dialog box, type 183-184, 186-187 in the Selection text field.
- 5 Click OK.

Attachment: Bearing 2

- I In the Physics toolbar, click **Boundaries** and choose **Attachment**.
- 2 In the Settings window for Attachment, type Attachment: Bearing 2 in the Label text field.
- 3 Locate the Boundary Selection section. Click Paste Selection.
- 4 In the Paste Selection dialog box, type 498-501 in the Selection text field.
- 5 Click OK.

Hinge Joint: Bearing I

- I In the Physics toolbar, click Global and choose Hinge Joint.
- 2 In the Settings window for Hinge Joint, type Hinge Joint: Bearing 1 in the Label text field.
- 3 Locate the Attachment Selection section. From the Source list, choose Attachment: Bearing 1.
- 4 From the Destination list, choose Rigid Domain: Rotor with Shaft.
- **5** Locate the **Joint Elasticity** section. From the list, choose **Elastic joint**.

Joint Elasticity I

I In the Model Builder window, expand the Hinge Joint: Bearing I node, then click Joint Elasticity 1.

- 2 In the Settings window for Joint Elasticity, locate the Spring section.
- 3 In the \mathbf{k}_{11} text field, type kb.
- **4** In the \mathbf{k}_{Θ} text field, type kbr.

Hinge Joint: Bearing 2

- I In the Model Builder window, right-click Hinge Joint: Bearing I and choose Duplicate.
- 2 In the Settings window for Hinge Joint, type Hinge Joint: Bearing 2 in the Label text field.
- 3 Locate the Attachment Selection section. From the Source list, choose Attachment: Bearing 2.

Attachment: Foundation 1

- I In the Model Builder window, expand the Hinge Joint: Bearing 2 node.
- 2 Right-click Multibody Dynamics (mbd) and choose Attachment.
- 3 In the Settings window for Attachment, type Attachment: Foundation 1 in the Label text field.
- 4 Locate the Boundary Selection section. Click Paste Selection.
- 5 In the Paste Selection dialog box, type 390-391 in the Selection text field.
- 6 Click OK.

Attachment: Foundation 2

- I Right-click Attachment: Foundation I and choose Duplicate.
- 2 In the Settings window for Attachment, type Attachment: Foundation 2 in the Label text field.
- 3 Locate the Boundary Selection section. Click | Clear Selection.
- 4 Click Paste Selection.
- 5 In the Paste Selection dialog box, type 470-471 in the Selection text field.
- 6 Click OK.

Attachment: Foundation 3

- I Right-click Attachment: Foundation 2 and choose Duplicate.
- 2 In the Settings window for Attachment, type Attachment: Foundation 3 in the Label text field.
- 3 Locate the Boundary Selection section. Click Clear Selection.
- 4 Click Paste Selection.
- 5 In the Paste Selection dialog box, type 472-473 in the Selection text field.

6 Click OK.

Attachment: Foundation 4

- I Right-click Attachment: Foundation 3 and choose Duplicate.
- 2 In the Settings window for Attachment, type Attachment: Foundation 4 in the Label text field.
- 3 Locate the Boundary Selection section. Click Clear Selection.
- 4 Click Paste Selection.
- 5 In the Paste Selection dialog box, type 392-393 in the Selection text field.
- 6 Click OK.

Fixed Joint: Foundation 1

- I In the Physics toolbar, click A Global and choose Fixed Joint.
- 2 In the Settings window for Fixed Joint, type Fixed Joint: Foundation 1 in the Label text field.
- 3 Locate the Attachment Selection section. From the Source list, choose Fixed.
- 4 From the Destination list, choose Attachment: Foundation 1.
- **5** Locate the **Joint Elasticity** section. From the list, choose **Elastic joint**.

Joint Elasticity I

- I In the Model Builder window, expand the Fixed Joint: Foundation I node, then click Joint Elasticity 1.
- 2 In the Settings window for Joint Elasticity, locate the Spring section.
- 3 In the \mathbf{k}_{u} text field, type kf.
- **4** In the \mathbf{k}_{θ} text field, type kfr.

Fixed Joint: Foundation 2

- I In the Model Builder window, right-click Fixed Joint: Foundation I and choose Duplicate.
- 2 In the Settings window for Fixed Joint, type Fixed Joint: Foundation 2 in the Label text field.
- 3 Locate the Attachment Selection section. From the Destination list, choose Attachment: Foundation 2.

Fixed Joint: Foundation 3

- I Right-click Fixed Joint: Foundation 2 and choose Duplicate.
- 2 In the Settings window for Fixed Joint, type Fixed Joint: Foundation 3 in the Label text field.

3 Locate the Attachment Selection section. From the Destination list, choose Attachment: Foundation 3.

Fixed Joint: Foundation 4

- I Right-click Fixed Joint: Foundation 3 and choose Duplicate.
- 2 In the Settings window for Fixed Joint, type Fixed Joint: Foundation 4 in the Label text field.
- 3 Locate the Attachment Selection section. From the Destination list, choose Attachment: Foundation 4.

DEFINITIONS (COMPI)

- I In the Model Builder window, under Component I (compl) click Definitions.
- 2 In the Definitions toolbar, click Moving Mesh and choose Domains>Rotating Domain.

MOVING MESH

Rotating Domain I

- I Select Domains 17–20 only.
- 2 In the Settings window for Rotating Domain, locate the Rotation section.
- 3 In the α text field, type comp2.mbd.hgj1.th.
- **4** Locate the **Axis** section. Specify the \mathbf{r}_{ax} vector as

0	Х
dy	Υ

STUDY I

Step 1: Time Dependent

- I In the Model Builder window, under Study I click Step I: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- 3 In the Output times text field, type range (0,0.001,0.7).

Solution I (soll)

- I In the Study toolbar, click Show Default Solver.
- 2 In the Model Builder window, expand the Solution I (soll) node, then click Time-Dependent Solver 1.
- 3 In the Settings window for Time-Dependent Solver, click to expand the Time Stepping section.

- 4 From the Steps taken by solver list, choose Intermediate.
- 5 From the Maximum step constraint list, choose Constant.
- **6** In the **Maximum step** text field, type 0.0002.
- 7 In the Model Builder window, expand the Study I>Solver Configurations> Solution I (soll)>Time-Dependent Solver I node.
- 8 In the Model Builder window, expand the Study I>Solver Configurations> Solution I (soll)>Time-Dependent Solver I node, then click Direct.
- 9 In the Settings window for Direct, locate the General section.
- **IO** From the **Solver** list, choose **PARDISO**.
- II In the Model Builder window, expand the Study I>Solver Configurations> Solution I (soll)>Time-Dependent Solver I>Segregated I node, then click **Multibody Dynamics.**
- 12 In the Settings window for Segregated Step, click to expand the Method and Termination section.
- 13 From the Jacobian update list, choose Once per time step.
- **14** From the **Termination technique** list, choose **Tolerance**.
- **15** In the **Tolerance factor** text field, type 1.
- 16 In the Model Builder window, under Study I>Solver Configurations>Solution I (soll)> Time-Dependent Solver I>Segregated I click Rotating Machinery, Magnetic.
- 17 In the Settings window for Segregated Step, locate the Method and Termination section.
- 18 From the Jacobian update list, choose On every iteration.
- 19 From the Termination technique list, choose Tolerance.
- 20 In the Maximum number of iterations text field, type 8.
- 21 In the Tolerance factor text field, type 1e-3.
- 22 In the Model Builder window, click Study 1.
- 23 In the Settings window for Study, locate the Study Settings section.
- **24** Clear the **Generate default plots** check box.
- 25 In the Study toolbar, click **Compute**.

RESULTS

Follow the instructions below to plot the magnetic flux density, electromagnetic torque, and the angular speed of the rotor as shown in Figure 3, Figure 5 and Figure 6 respectively.

Magnetic Flux Density Norm

- I In the Home toolbar, click **Add Plot Group** and choose **2D Plot Group**.
- 2 In the Settings window for 2D Plot Group, type Magnetic Flux Density Norm in the Label text field.
- 3 Locate the Plot Settings section. From the Frame list, choose Spatial (x, y, z).

Surface I

Right-click Magnetic Flux Density Norm and choose Surface.

Arrow Surface I

- I In the Model Builder window, right-click Magnetic Flux Density Norm and choose Arrow Surface.
- 2 In the Settings window for Arrow Surface, locate the Arrow Positioning section.
- 3 Find the x grid points subsection. In the Points text field, type 50.
- 4 Find the y grid points subsection. In the Points text field, type 50.
- 5 Locate the Coloring and Style section. Select the Scale factor check box.
- 6 In the associated text field, type 0.055.

Study I/Solution I (I) (soll)

In the Model Builder window, expand the Results>Datasets node, then click Study 1/ Solution I (I) (soll).

Selection

- I In the Results toolbar, click has a Attributes and choose Selection.
- 2 In the Settings window for Selection, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 Click Paste Selection.
- 5 In the Paste Selection dialog box, type 3-14, 16-20 in the Selection text field.
- 6 Click OK.

Study 1/Solution 1 (3) (soll)

In the Model Builder window, under Results>Datasets right-click Study 1/ Solution I (2) (soll) and choose Duplicate.

Selection

- I In the Model Builder window, right-click Study I/Solution I (3) (soll) and choose Selection.
- 2 In the Settings window for Selection, locate the Geometric Entity Selection section.

- 3 From the Geometric entity level list, choose Domain.
- 4 Click Paste Selection.
- 5 In the Paste Selection dialog box, type 13, 29-36 in the Selection text field.
- 6 Click OK.

Study I/Solution I (4) (soll)

In the Model Builder window, under Results>Datasets right-click Study I/ Solution I (3) (soll) and choose Duplicate.

Selection

- I In the Model Builder window, expand the Study I/Solution I (4) (soll) node, then click Selection.
- 2 In the Settings window for Selection, locate the Geometric Entity Selection section.
- 3 Click Clear Selection.
- 4 Click Paste Selection.
- 5 In the Paste Selection dialog box, type 1-4, 6-12, 17, 21, 25, 27 in the Selection text field.
- 6 Click OK.

Magnetic Flux Density Norm

- I In the Model Builder window, under Results click Magnetic Flux Density Norm.
- 2 In the Magnetic Flux Density Norm toolbar, click **2** Plot.
- 3 Click the Zoom Extents button in the Graphics toolbar.

Electromagnetic Torque (Rotor)

- I In the Home toolbar, click In Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Electromagnetic Torque (Rotor) in the Label text field.
- 3 Click to expand the Title section. From the Title type list, choose Manual.
- 4 In the **Title** text area, type Electromagnetic Torque (Rotor).

Global I

- I Right-click Electromagnetic Torque (Rotor) and choose Global.
- 2 In the Settings window for Global, locate the y-Axis Data section.

3 In the table, enter the following settings:

Expression	Unit	Description
comp1.rmm.Tz_Rotor	N*m	Torque, z component

4 Click to expand the Coloring and Style section. In the Width text field, type 2.

Electromagnetic Torque (Rotor)

- I In the Model Builder window, click Electromagnetic Torque (Rotor).
- 2 In the Settings window for ID Plot Group, locate the Legend section.
- 3 Clear the Show legends check box.
- 4 In the Electromagnetic Torque (Rotor) toolbar, click Plot.
- 5 Click the Zoom Extents button in the Graphics toolbar.

Rotor Speed

- I Right-click Electromagnetic Torque (Rotor) and choose Duplicate.
- 2 In the Settings window for ID Plot Group, type Rotor Speed in the Label text field.
- 3 Locate the **Title** section. In the **Title** text area, type Rotor Speed.

Global I

- I In the Model Builder window, expand the Rotor Speed node, then click Global I.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
comp2.mbd.hgj1.tht	rad/s	Relative angular velocity

- 4 In the Rotor Speed toolbar, click Plot.
- 5 Click the Zoom Extents button in the Graphics toolbar.

Follow the instructions below to plot the electromagnetic forces as a function of time and its frequency spectrum as shown in Figure 7 and Figure 8 respectively.

Electromagnetic Forces (Rotor)

- I In the Model Builder window, right-click Rotor Speed and choose Duplicate.
- 2 In the Settings window for ID Plot Group, type Electromagnetic Forces (Rotor) in the Label text field.
- 3 Locate the **Title** section. In the **Title** text area, type Electromagnetic Forces (Rotor).

Global I

- I In the Model Builder window, expand the Electromagnetic Forces (Rotor) node, then click Global I.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
rmm.Forcex_Rotor	N	Electromagnetic force, x component
rmm.Forcey_Rotor	N	Electromagnetic force, y component

Electromagnetic Forces (Rotor)

- I In the Model Builder window, click Electromagnetic Forces (Rotor).
- 2 In the Settings window for ID Plot Group, locate the Legend section.
- **3** Select the **Show legends** check box.
- 4 From the Position list, choose Lower left.
- **5** Locate the **Plot Settings** section. Select the **y-axis label** check box.
- **6** In the associated text field, type Force (N).
- 7 In the Electromagnetic Forces (Rotor) toolbar, click Plot.
- 8 Click the Zoom Extents button in the Graphics toolbar.

Electromagnetic Forces (Rotor): Frequency

- I Right-click Electromagnetic Forces (Rotor) and choose Duplicate.
- 2 In the Settings window for ID Plot Group, type Electromagnetic Forces (Rotor): Frequency in the Label text field.
- 3 Locate the Plot Settings section. Clear the y-axis label check box.
- 4 Locate the Legend section. From the Position list, choose Upper right.

Global I

- I In the Model Builder window, expand the Electromagnetic Forces (Rotor): Frequency node, then click Global I.
- 2 In the Settings window for Global, locate the x-Axis Data section.
- 3 From the Parameter list, choose Discrete Fourier transform.
- 4 From the Show list, choose Frequency spectrum.
- **5** Select the **Frequency range** check box.
- 6 In the Maximum text field, type 300.

8 Click the Zoom Extents button in the Graphics toolbar.

Follow the instructions below to plot the bearing and foundation forces as shown in Figure 9, Figure 10, Figure 11 and Figure 12 respectively.

Forces (Bearing-1)

- I In the Model Builder window, right-click Electromagnetic Forces (Rotor) and choose Duplicate.
- 2 In the Settings window for ID Plot Group, type Forces (Bearing-1) in the Label text field.
- 3 Locate the **Title** section. In the **Title** text area, type Forces (Bearing-1).

Global I

- I In the Model Builder window, expand the Forces (Bearing-I) node, then click Global I.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
comp2.mbd.hgj1.Fx	N	Joint force, x component
comp2.mbd.hgj1.Fy	N	Joint force, y component
comp2.mbd.hgj1.Fz	N	Joint force, z component

- 4 Click to expand the Legends section. From the Legends list, choose Manual.
- **5** In the table, enter the following settings:

Legends

- x component
- y component
- z component

Forces (Bearing-1)

- I In the Model Builder window, click Forces (Bearing-I).
- 2 In the Settings window for ID Plot Group, locate the Legend section.
- 3 From the Position list, choose Upper left.
- 4 In the Forces (Bearing-1) toolbar, click **Plot**.
- 5 Click the **Zoom Extents** button in the **Graphics** toolbar.

Forces (Bearing-2)

I Right-click Forces (Bearing-I) and choose Duplicate.

- 2 In the Settings window for ID Plot Group, type Forces (Bearing-2) in the Label text field.
- 3 Locate the **Title** section. In the **Title** text area, type Forces (Bearing-2).

- I In the Model Builder window, expand the Forces (Bearing-2) node, then click Global I.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
comp2.mbd.hgj2.Fx	N	Joint force, x component
comp2.mbd.hgj2.Fy	N	Joint force, y component
comp2.mbd.hgj2.Fz	N	Joint force, z component

- 4 In the Forces (Bearing-2) toolbar, click Plot.
- **5** Click the **Zoom Extents** button in the **Graphics** toolbar.

Forces (Foundation-1)

- I In the Model Builder window, right-click Forces (Bearing-2) and choose Duplicate.
- 2 In the Settings window for ID Plot Group, type Forces (Foundation-1) in the Label text field.
- 3 Locate the **Title** section. In the **Title** text area, type Forces (Foundation-1).

Global I

- I In the Model Builder window, expand the Forces (Foundation-I) node, then click Global I.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
comp2.mbd.fxj1.Fx	N	Joint force, x component
comp2.mbd.fxj1.Fy	N	Joint force, y component
comp2.mbd.fxj1.Fz	N	Joint force, z component

- **5** Click the **Zoom Extents** button in the **Graphics** toolbar.

Forces (Foundation-I): Frequency

I In the Model Builder window, right-click Forces (Foundation-I) and choose Duplicate.

2 In the Settings window for ID Plot Group, type Forces (Foundation-1): Frequency in the Label text field.

Global I

- I In the Model Builder window, expand the Forces (Foundation-I) I node, then click Results>Forces (Foundation-I): Frequency>Global I.
- 2 In the Settings window for Global, locate the x-Axis Data section.
- 3 From the Parameter list, choose Discrete Fourier transform.
- 4 From the Show list, choose Frequency spectrum.
- **5** Select the **Frequency range** check box.
- 6 In the Maximum text field, type 300.

Forces (Foundation-I): Frequency

- I In the Model Builder window, click Forces (Foundation-I): Frequency.
- 2 In the Settings window for ID Plot Group, locate the Legend section.
- 3 From the Position list, choose Upper right.
- 4 Locate the **Plot Settings** section. Clear the **y-axis label** check box.
- 5 In the Forces (Foundation-I): Frequency toolbar, click Plot.
- **6** Click the **Zoom Extents** button in the **Graphics** toolbar.

Follow the instructions below to plot the orbital motion of the rotor as shown in Figure 13.

Rotor Orbits

- I In the Home toolbar, click Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Rotor Orbits in the Label text field.
- 3 Locate the Title section. From the Title type list, choose Manual.
- 4 In the **Title** text area, type Rotor Orbits.
- 5 Locate the Data section. From the Dataset list, choose Study 1/Solution 1 (2) (sol1).

Global I

- I Right-click Rotor Orbits and choose Global.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
mbd.hgj1.u2	mm	Displacement (y direction)

- 4 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- 5 In the Expression text field, type mbd.hgj1.u3.
- **6** From the **Unit** list, choose **mm**.
- 7 Select the **Description** check box.
- **8** In the associated text field, type Displacement (z direction).

Color Expression 1

- I Right-click Global I and choose Color Expression.
- 2 In the Settings window for Color Expression, locate the Expression section.
- **3** In the **Expression** text field, type t.

Global 2

- I In the Model Builder window, under Results>Rotor Orbits right-click Global I and choose Duplicate.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
mbd.hgj2.u2	mm	Displacement (y direction)

4 Locate the x-Axis Data section. In the Expression text field, type mbd.hgj2.u3.

Annotation I

- I In the Model Builder window, right-click Rotor Orbits and choose Annotation.
- 2 In the Settings window for Annotation, locate the Annotation section.
- 3 In the **Text** text field, type Bearing 1.
- 4 Locate the **Position** section. In the **X** text field, type 1e-3.
- 5 In the Y text field, type -1e-3.
- 6 Locate the Coloring and Style section. Clear the Show point check box.

Annotation 2

- I Right-click Annotation I and choose Duplicate.
- 2 In the Settings window for Annotation, locate the Annotation section.
- 3 In the **Text** text field, type Bearing 2.
- 4 Locate the **Position** section. In the **X** text field, type -3e-3.
- 5 In the Y text field, type 1.5e-3.

Rotor Orbits

- I In the Model Builder window, click Rotor Orbits.
- 2 In the Settings window for ID Plot Group, locate the Legend section.
- 3 Clear the Show legends check box.
- 4 Locate the Axis section. Select the Preserve aspect ratio check box.
- 5 In the Rotor Orbits toolbar, click Plot.
- 6 Click the Zoom Extents button in the Graphics toolbar.

Housing Stress

- I In the Home toolbar, click Add Plot Group and choose 3D Plot Group.
- 2 In the Settings window for 3D Plot Group, locate the Data section.
- 3 From the Dataset list, choose Study I/Solution I (3) (soll).
- 4 In the Label text field, type Housing Stress.

Surface 1

- I Right-click Housing Stress and choose Surface.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type mbd.mises.
- 4 Click to expand the Range section. Select the Manual color range check box.
- 5 In the Maximum text field, type 5e4.
- 6 Locate the Coloring and Style section. From the Color table list, choose TrafficLightClassic.

Deformation I

- I Right-click Surface I and choose Deformation.
- 2 In the Settings window for Deformation, locate the Scale section.
- 3 Select the Scale factor check box.
- 4 In the associated text field, type 2000.
- 5 In the Housing Stress toolbar, click Plot.
- **6** Click the **Zoom Extents** button in the **Graphics** toolbar.

Housing Stress (with Rotor)

- I In the Model Builder window, right-click Housing Stress and choose Duplicate.
- 2 In the Settings window for 3D Plot Group, type Housing Stress (with Rotor) in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study I/Solution I (2) (soll).

4 Locate the Plot Settings section. From the Frame list, choose Spatial (x, y, z).

Surface 1

- I In the Model Builder window, expand the Housing Stress (with Rotor) node, then click Surface 1.
- 2 In the Settings window for Surface, locate the Data section.
- 3 From the Dataset list, choose Study I/Solution I (3) (soll).
- 4 From the Solution parameters list, choose From parent.

Deformation I

- I In the Model Builder window, expand the Surface I node, then click Deformation I.
- 2 In the Settings window for Deformation, locate the Scale section.
- 3 In the Scale factor text field, type 1.

Contour I

- I In the Model Builder window, right-click Housing Stress (with Rotor) and choose Contour.
- 2 In the Settings window for Contour, locate the Data section.
- 3 From the Dataset list, choose Study I/Solution I (3) (soll).
- 4 From the Solution parameters list, choose From parent.
- 5 Locate the Expression section. In the Expression text field, type mbd.mises.
- 6 Locate the Levels section. In the Total levels text field, type 10.
- 7 Locate the Coloring and Style section. From the Coloring list, choose Uniform.
- 8 From the Color list, choose Black.
- **9** Click to expand the **Title** section. From the **Title type** list, choose **None**.
- **10** Locate the Coloring and Style section. Clear the Color legend check box.

Deformation I

- I Right-click Contour I and choose Deformation.
- 2 In the Settings window for Deformation, locate the Scale section.
- 3 Select the Scale factor check box.
- 4 In the associated text field, type 1.

Surface 2

- I In the Model Builder window, right-click Housing Stress (with Rotor) and choose Surface.
- 2 In the Settings window for Surface, locate the Data section.
- 3 From the Dataset list, choose Study I/Solution I (4) (soll).

- 4 From the Solution parameters list, choose From parent.
- **5** Locate the **Expression** section. In the **Expression** text field, type mbd.vel.
- 6 Locate the Coloring and Style section. From the Color table list, choose AuroraBorealis.

Deformation I

- I Right-click Surface 2 and choose Deformation.
- 2 In the Settings window for Deformation, locate the Scale section.
- 3 Select the Scale factor check box.
- 4 In the associated text field, type 1.

Housing Stress (with Rotor)

- I In the Model Builder window, under Results click Housing Stress (with Rotor).
- 2 In the Settings window for 3D Plot Group, locate the Color Legend section.
- 3 From the Position list, choose Right double.
- 4 In the Housing Stress (with Rotor) toolbar, click **Plot**.
- 5 Click the Zoom Extents button in the Graphics toolbar.

Create animations to visualize the variation of magnetic flux density and stress distribution in different parts of the motor over time.

Animation I

- I In the Results toolbar, click Animation and choose Player.
- 2 In the Settings window for Animation, locate the Frames section.
- 3 In the Number of frames text field, type 50.

Animation 2

- I Right-click Animation I and choose Duplicate.
- 2 In the Settings window for Animation, locate the Scene section.
- 3 From the Subject list, choose Housing Stress.
- 4 Locate the Animation Editing section. From the Time selection list, choose Interpolated.
- 5 In the Times (s) text field, type range (0,0.01,0.7).
- 6 Locate the Frames section. In the Number of frames text field, type 70.

Animation 3

- I Right-click Animation 2 and choose Duplicate.
- 2 In the Settings window for Animation, locate the Scene section.
- 3 From the Subject list, choose Housing Stress (with Rotor).