

Heating Circuit

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Introduction

Small heating circuits are used in many applications. For example, in manufacturing processes they heat up reactive fluids. Figure 1 illustrates a typical heating device for this model. The device consists of an electrically resistive layer deposited on a glass plate, which causes Joule heating when a voltage is applied to the circuit. The layer's properties determine the amount of heat produced.



Figure 1: Geometry of a heating device.

In this particular model, you must observe three important design considerations:

- Noninvasive heating
- · Minimal deflection of the heating device
- · Avoidance of overheating the process fluid

The heater must also work without failure. You achieve the first and second requirements by inserting a glass plate between the heating circuit and the fluid; it acts as a conducting separator. Glass is an ideal material for both of these purposes because it is nonreactive and has a low coefficient of thermal expansion.

You must also avoid overheating due to the risk of self-ignition of the reactive fluid stream. Ignition is also the main reason for separating the electrical circuit from direct contact with the fluid. The heating device is tailored for each application, making virtual prototyping very important for manufacturers.

For heating circuits in general, detachment of the resistive layer often determines the failure rate. This is caused by excessive thermally induced interfacial stresses. Once the layer is detached it gets locally overheated, which accelerates the detachment. Finally, in the worst case, the circuit might overheat and burn. From this perspective, it is also important to study the interfacial tension due to the differences in temperature as well as

the different thermal-expansion coefficients of the resistive layer and the substrate. The geometric shape of the layer is a key parameter to design circuits for proper functioning. You can investigate all of the abovementioned aspects by modeling the circuit.

This multiphysics example simulates the electrical heat generation, the heat transfer, and the mechanical stresses and deformations of a heating circuit device. The model uses the Heat Transfer in Solids interface of the Heat Transfer Module in combination with the Electric Currents, Layered Shell interface from the AC/DC Module and the Solid Mechanics and Membrane interfaces from the Structural Mechanics Module.

Note: This model requires the AC/DC Module, Heat Transfer Module, and Structural Mechanics Module.

Model Definition

Figure 2 shows a drawing of the modeled heating circuit.



Figure 2: Drawing of the heating circuit deposited on a glass plate.

The device consists of a serpentine-shaped Nichrome resistive layer, $10 \ \mu m$ thick and 5 mm wide, deposited on a glass plate. At each end, it has a silver contact pad measuring 10 mm-by-10 mm-by-10 μm . When the circuit is in use, the deposited side of the glass plate is in contact with surrounding air, and the back side is in contact with the heated fluid. Assume that the edges and sides of the glass plate are thermally insulated.

Table 1 gives the resistor's dimensions.

ОВЈЕСТ	LENGTH	WIDTH	THICKNESS
Glass Plate	130 mm	80 mm	2 mm
Pads and Circuit	-	-	10 µm

During operation the resistive layer produces heat. Model the electrically generated heat using the Electric Currents, Layered Shell interface from the AC/DC Module. An electric potential of 12 V is applied to the pads. In the model, you achieve this effect by setting the potential at one edge of the first pad to 12 V and that of one edge of the other pad to 0 V.

To model the heat transfer in the thin conducting layer, use the Thin Layer feature from the Heat Transfer in Solids interface. The heat rate per unit area (measured in W/m^2) produced inside the thin layer is given by

$$q_{\rm prod} = dQ_{\rm DC} \tag{1}$$

where $Q_{\text{DC}} = \mathbf{J} \cdot \mathbf{E} = \sigma |\nabla_t V|^2 (W/m^3)$ is the power density. The generated heat appears as an inward heat flux at the surface of the glass plate.

At steady state, the resistive layer dissipates the heat it generates in two ways: on its up side to the surrounding air (at 293 K), and on its down side to the glass plate. The glass plate is similarly cooled in two ways: on its circuit side by air, and on its back side by a process fluid (353 K). You model the heat fluxes to the surroundings using heat transfer coefficients, *h*. For the heat transfer to air, $h = 5 \text{ W/(m}^2 \cdot \text{K})$, representing natural convection. On the glass plate's back side, $h = 20 \text{ W/(m}^2 \cdot \text{K})$, representing convective heat transfer to the fluid. The sides of the glass plate are insulated.

The model simulates thermal expansion using static structural-mechanics analyses. It uses the Solid Mechanics interface for the glass plate, and the Membrane interface for the circuit layer. The equations of these two interfaces are described in the *Structural Mechanics Module User's Guide*. The stresses are set to zero at 293 K. You determine the boundary conditions for the Solid Mechanics interface by fixing one corner with respect to the *x*-, *y*-, and *z*-displacements and rotation.

Table 2 summarizes the material properties used in the model.

MATERIAL	E [GPa]	ν	α [I/K]	<i>k</i> [W/(m·K)]	ρ [kg/m ³]	C_p [J/(kg·K)]
Silver	83	0.37	1.89e-5	420	10500	230

TABLE 2: MATERIAL PROPERTIES.

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MATERIAL	E [GPa]	ν	α [I/K]	<i>k</i> [W/(m·K)]	$\rho \ [kg/m^3]$	C_p [J/(kg·K)]
Nichrome	213	0.33	le-5	15	9000	20
Glass	73.1	0.17	5.5e-7	1.38	2203	703

Results and Discussion

Figure 3 shows the heat that the resistive layer generates.

Surface: Surface loss density, electromagnetic (W/m²)



Figure 3: Stationary heat generation in the resistive layer when 12 V is applied.

The highest heating power occurs at the inner corners of the curves due to the higher current density at these spots. The total generated heat, as calculated by integration, is approximately 13.8 W.







Figure 4: Temperature distribution in the heating device at steady state.

The highest temperature is approximately 428 K, and it appears in the central section of the circuit layer. It is interesting to see that the differences in temperature between the fluid side and the circuit side of the glass plate are quite small because the plate is very thin. Using boundary integration, the integral heat flux on the fluid side evaluates to approximately 8.5 W. This means that the device transfers the majority of the heat it generates — 8.5 W out of 13.8 W — to the fluid, which is good from a design perspective, although the thermal resistance of the glass plate results in some losses.

The temperature rise also induces thermal stresses due the materials' different coefficients of thermal expansion. As a result, mechanical stresses and deformations arise in the layer

and in the glass plate. Figure 5 shows the equivalent stress distribution in the device and the resulting deformations. During operation, the glass plate bends toward the air side.



Volume: von Mises stress (MPa)

Figure 5: The thermally induced von Mises stress plotted with the deformation.

The highest equivalent stress, approximately 13 MPa, occurs at the inner corners of the curves of the Nichrome circuit. The yield stress for high quality glass is roughly 250 MPa, and for Nichrome it is 360 MPa. This means that the individual objects remain structurally intact for the simulated heating power loads.

You must also consider stresses in the interface between the resistive layer and the glass plate. Assume that the yield stress of the surface adhesion in the interface is in the region of 50 MPa — a value significantly lower than the yield stresses of the other materials in the device. If the equivalent stress increases above this value, the resistive layer locally detaches from the glass. Once it has detached, heat transfer is locally impeded, which can lead to overheating of the resistive layer and eventually cause the device to fail.

Figure 6 displays the effective forces acting on the adhesive layer during heater operation. As the figure shows, the device experiences a maximum interfacial stress that is an order of magnitude smaller than the yield stress. This means that the device is well designed in terms of adhesive stress.



Figure 6: The effective forces at the interface between the resistive layer and the glass plate.





Figure 7: Deviation from a plane surface on the fluid side of the glass plate.

The maximum deviation from being a planar surface, is approximately $50 \mu m$. For high-precision applications, such as semiconductor processing, this might be a significant value that limits the device's operating temperature.

Application Library path: Heat_Transfer_Module/ Power_Electronics_and_Electronic_Cooling/heating_circuit

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click 🕙 Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click 间 3D.
- 2 In the Select Physics tree, select Structural Mechanics>Thermal-Structure Interaction> Thermal Stress, Solid.
- 3 Click Add.
- 4 In the Select Physics tree, select AC/DC>Electric Fields and Currents> Electric Currents in Layered Shells (ecis).
- 5 Click Add.
- 6 In the Select Physics tree, select Structural Mechanics>Membrane (mbrn).
- 7 Click Add.
- 8 Click \bigcirc Study.
- 9 In the Select Study tree, select General Studies>Stationary.
- 10 Click 🗹 Done.

GEOMETRY I

The Thermal Stress interface includes Heat Transfer in Solids and Solid Mechanics. In the volume, these two interfaces solve for temperature and displacement, respectively. In the shell representing the circuit, the temperature, the electrical potential and displacement are solved by Heat Transfer In Solids, Electric Currents, Layered Shell, and Membrane interfaces, respectively.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.

3 In the table, enter the following settings:

Name	Expression	Value	Description
V_in	12[V]	12 V	Input voltage
d_layer	10[um]	IE-5 m	Layer thickness
sigma_silver	6.3e7[S/m]	6.3E7 S/m	Electric conductivity of silver
sigma_nichrome	9.3e5[S/m]	9.3E5 S/m	Electric conductivity of Nichrome
T_air	20[degC]	293.15 K	Air temperature
h_air	5[W/(m^2*K)]	5 W/(m²·K)	Heat transfer film coefficient, air
T_fluid	353[K]	353 K	Fluid temperature
h_fluid	20[W/(m^2*K)]	20 W/(m²·K)	Heat transfer film coefficient, fluid

GEOMETRY I

- I In the Model Builder window, under Component I (compl) click Geometry I.
- 2 In the Settings window for Geometry, locate the Units section.
- 3 From the Length unit list, choose mm.

Block I (blkI)

- I In the **Geometry** toolbar, click 🗍 Block.
- 2 In the Settings window for Block, locate the Size and Shape section.
- 3 In the Width text field, type 80.
- 4 In the **Depth** text field, type 130.
- 5 In the **Height** text field, type 2.
- 6 Click 틤 Build Selected.

Work Plane I (wp1)

- I In the Geometry toolbar, click 📥 Work Plane.
- 2 In the Settings window for Work Plane, locate the Plane Definition section.

- 3 In the z-coordinate text field, type 2.
- 4 Click 📥 Show Work Plane.

Work Plane I (wp1)>Plane Geometry

Click the **Click the Come Extents** button in the **Graphics** toolbar.

Work Plane 1 (wp1)>Square 1 (sq1)

- I In the Work Plane toolbar, click Square.
- 2 In the Settings window for Square, locate the Size section.
- 3 In the Side length text field, type 10.
- 4 Locate the **Position** section. In the **xw** text field, type 7.
- **5** In the **yw** text field, type **10**.
- 6 Click 틤 Build Selected.

Work Plane 1 (wp1)>Square 2 (sq2)

- I Right-click Component I (comp1)>Geometry I>Work Plane I (wp1)>Plane Geometry> Square I (sq1) and choose Duplicate.
- 2 In the Settings window for Square, locate the Position section.
- **3** In the **xw** text field, type **30**.
- 4 In the **yw** text field, type 8.
- 5 Click 틤 Build Selected.

Work Plane 1 (wp1)>Polygon 1 (poll)

- I In the Work Plane toolbar, click / Polygon.
- 2 In the Settings window for Polygon, locate the Coordinates section.
- 3 From the Data source list, choose File.
- 4 Click **Prowse**.
- 5 Browse to the model's Application Libraries folder and double-click the file heating_circuit_polygon.txt.
- 6 Click 틤 Build Selected.

Work Plane I (wp1)>Fillet I (fill)

I In the Work Plane toolbar, click / Fillet.

2 On the object poll, select Points 2–8, 23–29, 34, 36, 37, 41, and 42 only.

It might be easier to select the points by using the **Selection List** window. To open this window, in the **Home** toolbar click **Windows** and choose **Selection List**. (If you are running the cross-platform desktop, you find **Windows** in the main menu.)



- 3 In the Settings window for Fillet, locate the Radius section.
- 4 In the Radius text field, type 10.
- 5 Click 🔚 Build Selected.

Work Plane I (wp1)>Fillet 2 (fil2)

- I In the Work Plane toolbar, click 🥢 Fillet.
- 2 On the object fill, select Points 6–12, 26–31, 37, 40, 43, 46, 49, and 50 only.
- 3 In the Settings window for Fillet, locate the Radius section.
- 4 In the Radius text field, type 5.
- 5 In the Work Plane toolbar, click 📳 Build All.

Form Union (fin)

I In the Home toolbar, click 🟢 Build All.

The geometry should look like the figure below.



DEFINITIONS

Add a selection that you can use later when applying boundary conditions and shell physics settings.

Circuit

- I In the **Definitions** toolbar, click **here Explicit**.
- 2 In the Settings window for Explicit, type Circuit in the Label text field.
- 3 Locate the Input Entities section. From the Geometric entity level list, choose Boundary.
- **4** Select Boundaries 6–8 only.

Before creating the materials for use in this model, it is a good idea to specify which boundaries are to be modeled as conducting shells. Using this information, COMSOL Multiphysics can detect which material properties are needed.

HEAT TRANSFER IN SOLIDS (HT)

Thin Layer 1

- I In the Model Builder window, under Component I (compl) right-click Heat Transfer in Solids (ht) and choose Thin Structures>Thin Layer.
- 2 In the Settings window for Thin Layer, locate the Boundary Selection section.
- 3 From the Selection list, choose Circuit.
- **4** Locate the **Layer Model** section. From the **Layer type** list, choose **Thermally thin approximation**.
- 5 Select the Layerwise constant properties check box.

ELECTRIC CURRENTS IN LAYERED SHELLS (ECIS)

- I In the Model Builder window, under Component I (comp1) click Electric Currents in Layered Shells (ecis).
- 2 In the Settings window for Electric Currents in Layered Shells, locate the Boundary Selection section.
- **3** From the **Selection** list, choose **Circuit**.

Conductive Shell I

- I In the Model Builder window, under Component I (comp1)> Electric Currents in Layered Shells (ecis) click Conductive Shell I.
- 2 In the Settings window for Conductive Shell, locate the Constitutive Relation D-E section.
- **3** From the ε_r list, choose **User defined**.

Use **Layered Linear Elastic Material** in membrane interface so that **Layered Thermal Expansion** multiphysics coupling can be used for modeling thermal effects.

MEMBRANE (MBRN)

- I In the Model Builder window, under Component I (compl) click Membrane (mbrn).
- 2 In the Settings window for Membrane, locate the Boundary Selection section.
- **3** From the **Selection** list, choose **Circuit**.

Layered Linear Elastic Material I

- I In the Physics toolbar, click 🔚 Boundaries and choose Layered Linear Elastic Material.
- **2** In the **Settings** window for **Layered Linear Elastic Material**, locate the **Boundary Selection** section.
- 3 From the Selection list, choose Circuit.

MULTIPHYSICS

Layered Thermal Expansion 1 (tell)

In the Physics toolbar, click An Multiphysics Couplings and choose Boundary> Layered Thermal Expansion.

Now set up the materials.

ADD MATERIAL

- I In the Home toolbar, click 👬 Add Material to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Built-in>Silica glass.
- 4 Click Add to Component in the window toolbar.
- 5 In the Home toolbar, click 🙀 Add Material to close the Add Material window.

MATERIALS

Silver Layer

- I In the Model Builder window, under Component I (comp1) right-click Materials and choose Layers>Single Layer Material.
- 2 In the Settings window for Material, type Silver Layer in the Label text field.
- 3 Locate the Geometric Entity Selection section. From the Selection list, choose Circuit.
- 4 Locate the Orientation and Position section. From the Position list, choose Bottom side on boundary.
- 5 Locate the Material Contents section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Heat capacity at constant pressure	Ср	230	J/(kg·K)	Basic
Density	rho	10500	kg/m³	Basic
Young's modulus	E	83e9	Pa	Young's modulus and Poisson's ratio
Poisson's ratio	nu	0.37	I	Young's modulus and Poisson's ratio

Property	Variable	Value	Unit	P roperty group
Thermal conductivity	k_iso ; kii = k_iso, kij = 0	420	W/(m·K)	Basic
Electrical conductivity	sigma_iso; sigmaii = sigma_iso, sigmaij = 0	sigma_si lver	S/m	Basic
Coefficient of thermal expansion	alpha_iso ; alphaii = alpha_iso, alphaij = 0	18.9e-6	I/K	Basic
Thickness	lth	d_layer	m	Shell

Nichrome Layer

- I Right-click Materials and choose Layers>Single Layer Material.
- **2** Select Boundary 7 only.
- 3 In the Settings window for Material, type Nichrome Layer in the Label text field.
- 4 Locate the Orientation and Position section. From the Position list, choose Bottom side on boundary.
- **5** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Heat capacity at constant pressure	Ср	20	J/(kg·K)	Basic
Density	rho	9000	kg/m³	Basic
Young's modulus	E	213e9	Pa	Young's modulus and Poisson's ratio
Poisson's ratio	nu	0.33	I	Young's modulus and Poisson's ratio
Thermal conductivity	k_iso ; kii = k_iso, kij = 0	15	W/(m·K)	Basic

Property	Variable	Value	Unit	Property group
Electrical conductivity	sigma_iso ; sigmaii = sigma_iso, sigmaij = 0	sigma_nic hrome	S/m	Basic
Coefficient of thermal expansion	alpha_iso ; alphaii = alpha_iso, alphaij = 0	10e-6	I/K	Basic
Thickness	lth	d_layer	m	Shell

ELECTRIC CURRENTS IN LAYERED SHELLS (ECIS)

In the Model Builder window, under Component I (compl) click Electric Currents in Layered Shells (ecis).

Ground I

- I In the Physics toolbar, click 🔚 Edges and choose Ground.
- 2 Select Edge 43 only.

Electric Potential I

- I In the Physics toolbar, click 🔚 Edges and choose Electric Potential.
- 2 Select Edge 10 only.
- 3 In the Settings window for Electric Potential, locate the Electric Potential section.
- **4** In the V_0 text field, type V_in.

Continuity I a

- I In the Physics toolbar, click 📄 Edges and choose Continuity.
- 2 In the Settings window for Continuity, locate the Layer Selection section.
- 3 From the Source list, choose Silver Layer (mat2).
- 4 From the Destination list, choose Nichrome Layer (mat3).

With the materials defined, set up the remaining physics of the model. In the next section, the resistive loss within the circuit is defined as a heat source for the thermal stress physics. The resistive loss is calculated automatically within the **Electric Currents, Layered Shell** physics interface. Add the coupling feature **Electromagnetic Heating** to take the resistive loss into account.

MULTIPHYSICS

Electromagnetic Heating, Layered Shell 1 (ehls1)

In the Physics toolbar, click An Multiphysics Couplings and choose Boundary> Electromagnetic Heating, Layered Shell.

Add the coupling feature Solid-Shell Connection to connect the Solid Mechanics with Membrane.

Solid-Thin Structure Connection 1 (sshc1)

In the Physics toolbar, click A Multiphysics Couplings and choose Global>Solid-Thin Structure Connection.

HEAT TRANSFER IN SOLIDS (HT)

In the Model Builder window, under Component I (compl) click Heat Transfer in Solids (ht).

Heat Flux 1

- I In the Physics toolbar, click 🔚 Boundaries and choose Heat Flux.
- **2** Select Boundaries 4 and 6–8 only.



- 3 In the Settings window for Heat Flux, locate the Heat Flux section.
- 4 From the Flux type list, choose Convective heat flux.
- 5 In the *h* text field, type h_air.
- **6** In the T_{ext} text field, type T_air.

Heat Flux 2

- I In the Physics toolbar, click 🔚 Boundaries and choose Heat Flux.
- **2** Select Boundary 3 only.
- 3 In the Settings window for Heat Flux, locate the Heat Flux section.
- 4 From the Flux type list, choose Convective heat flux.
- **5** In the *h* text field, type h_fluid.
- **6** In the T_{ext} text field, type T_fluid.

SOLID MECHANICS (SOLID)

In order for the problem to be well posed, the glass plate must be constrained so that it does not have any possible rigid body translations or rotations. The constraints must be such that no stresses are induced by inhibited thermal expansion.

I In the Model Builder window, under Component I (compl) click Solid Mechanics (solid).

Rigid Motion Suppression 1

- I In the Physics toolbar, click 📒 Domains and choose Rigid Motion Suppression.
- **2** Select Domain 1 only.

MESH I

Free Triangular 1

- I In the Mesh toolbar, click \bigwedge Boundary and choose Free Triangular.
- **2** Select Boundaries 4 and 6–8 only.

Size 1

- I Right-click Free Triangular I and choose Size.
- 2 In the Settings window for Size, locate the Geometric Entity Selection section.
- **3** From the **Selection** list, choose **Circuit**.
- 4 Locate the **Element Size** section. Click the **Custom** button.
- 5 Locate the Element Size Parameters section. Select the Maximum element size check box.
- 6 In the associated text field, type 2.

Swept I

In the Mesh toolbar, click A Swept.

Distribution I

I Right-click Swept I and choose Distribution.

- 2 In the Settings window for Distribution, locate the Distribution section.
- 3 In the Number of elements text field, type 3.
- 4 Click 📗 Build All.

STUDY I

In order to improve the solver's performance, set the scaling of **Solid Mechanics** degree of freedom to 1e-3.

Solution 1 (soll)

- I In the Study toolbar, click **The Show Default Solver**.
- 2 In the Model Builder window, expand the Solution I (soll) node.
- 3 In the Model Builder window, expand the Study I>Solver Configurations> Solution I (solI)>Dependent Variables I node, then click Displacement field (compl.u).
- 4 In the Settings window for Field, locate the Scaling section.
- 5 From the Method list, choose Manual.
- 6 In the Scale text field, type 1e-3.
- 7 In the Model Builder window, under Study I>Solver Configurations>Solution I (soll)> Dependent Variables I click Displacement field (compl.u2).
- 8 In the Settings window for Field, locate the Scaling section.
- 9 In the Scale text field, type 1e-3.
- **IO** In the **Study** toolbar, click **= Compute**.

RESULTS

The first default plot shows the von Mises stress and the deformation of the device (Figure 5). The second default plot shows the temperature distribution on the surface of the full 3D geometry (Figure 4). Two plots are also generated to visualize the electric potential and the von Mises stress on the circuit layer.

Volume 1

- I In the Model Builder window, expand the Results>Stress (solid) node, then click Volume I.
- 2 In the Settings window for Volume, locate the Expression section.
- 3 From the Unit list, choose MPa.
- **4** In the **Stress (solid)** toolbar, click **I** Plot.

Surface 1

- I In the Model Builder window, expand the Results>Stress (mbrn) node, then click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 From the Unit list, choose MPa.
- 4 In the Stress (mbrn) toolbar, click **I** Plot.

Surface 2

- I In the Model Builder window, expand the Results>Temperature (ht) node, then click Surface 2.
- 2 In the Settings window for Surface, click to expand the Title section.
- **3** From the **Title type** list, choose **None**.

Study I/Solution I (2) (soll)

- I In the Model Builder window, expand the Results>Datasets node.
- 2 Right-click Results>Datasets>Study I/Solution I (soll) and choose Duplicate.

Selection

- I In the Results toolbar, click 🖣 Attributes and choose Selection.
- 2 In the Settings window for Selection, locate the Geometric Entity Selection section.
- **3** From the **Geometric entity level** list, choose **Boundary**.
- 4 From the Selection list, choose Circuit.

To generate Figure 3 follow the steps below.

Surface Losses

- I In the Results toolbar, click 间 3D Plot Group.
- 2 In the Settings window for 3D Plot Group, type Surface Losses in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study I/Solution I (2) (soll).

Surface 1

- I In the Surface Losses toolbar, click 🔲 Surface.
- 2 In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>
 Electric Currents in Layered Shells>Heating and losses>ecis.Qsh Surface loss density, electromagnetic W/m².
- **3** In the **Surface Losses** toolbar, click **O Plot**.
- **4** Click the **v** Scene Light button in the Graphics toolbar.

5 Click the \leftrightarrow **Zoom Extents** button in the **Graphics** toolbar.

The following steps generate a plot of the norm of the surface traction vector in the surface plane (see Figure 6):

Interface Stress

- I In the Home toolbar, click 🔎 Add Plot Group and choose 3D Plot Group.
- 2 In the Settings window for 3D Plot Group, type Interface Stress in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study I/Solution I (2) (soll).

Surface 1

- I In the Interface Stress toolbar, click T Surface.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type sqrt(solid.Tax^2+solid.Tay^2).
- 4 From the Unit list, choose MPa.
- 5 Locate the Coloring and Style section. From the Color table list, choose Prism.
- 6 In the Interface Stress toolbar, click 💿 Plot.

Finally, to obtain Figure 7, proceed as follows:

7 In the **Results** toolbar, click **More Datasets** and choose **Surface**.

Surface 1

Select Boundary 3 only.

Displacement, Bottom Boundary

- I In the **Results** toolbar, click **2D Plot Group**.
- 2 In the Settings window for 2D Plot Group, type Displacement, Bottom Boundary in the Label text field.

Surface 1

- I Right-click Displacement, Bottom Boundary and choose Surface.
- In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (comp1)>Solid Mechanics> Displacement>solid.disp Displacement magnitude m.
- 3 Locate the Expression section. In the Unit field, type um.
- 4 Locate the Coloring and Style section. From the Color table list, choose SpectrumLight.
- 5 In the Displacement, Bottom Boundary toolbar, click 💽 Plot.

The absolute displacement is not important in itself, since it is just a function of how the rigid body constraints are applied. Instead, you want to see how much the boundary deviates from being planar. To display that, create a linear approximation of the deformation using a least-squares fit. Then, plot the deviation from that plane.

DEFINITIONS (COMPI)

Integration 1 (intop1)

- I In the Definitions toolbar, click Nonlocal Couplings and choose Integration.
- 2 In the Settings window for Integration, type intBelow in the Operator name text field.
- **3** Locate the **Source Selection** section. From the **Geometric entity level** list, choose **Boundary**.
- 4 Select Boundary 3 only.
- 5 Locate the Advanced section. From the Frame list, choose Material (X, Y, Z).

Variables I

- I In the Model Builder window, right-click Definitions and choose Variables.
- 2 In the Settings window for Variables, locate the Variables section.
- 3 Click **b** Load from File.
- **4** Browse to the model's Application Libraries folder and double-click the file heating_circuit_variables.txt.
- **5** Click the **5** Show More Options button in the Model Builder toolbar.
- 6 In the Show More Options dialog box, in the tree, select the check box for the node General>Variable Utilities.
- 7 Click OK.

Matrix Inverse 1 (matinv1)

- I In the Definitions toolbar, click a_{a} Variable Utilities and choose Matrix Inverse.
- 2 In the Settings window for Matrix Inverse, type AInv in the Name text field.
- 3 Locate the Input Matrix section. From the Matrix format list, choose Symmetric.
- **4** In the table, enter the following settings:

A1	Ax	Ay
Ax	Axx	Аху
Ау	Аху	Ауу

STUDY I

In the **Study** toolbar, click **C Update Solution**.

RESULTS

Surface 1

- I In the Model Builder window, under Results>Displacement, Bottom Boundary click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- **3** In the **Expression** text field, type w- (w_0+w_x*X+w_y*Y).
- 4 In the Displacement, Bottom Boundary toolbar, click 💿 Plot.



To calculate the values for the total generated heat and the integrated heat flux on the fluid side, perform a boundary integration:

Surface Integration 1

- I In the Results toolbar, click ^{8,85}_{e-12} More Derived Values and choose Integration> Surface Integration.
- **2** Select Boundary **3** only.
- 3 In the Settings window for Surface Integration, click Replace Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (compl)> Heat Transfer in Solids>Boundary fluxes>ht.q0 Inward heat flux W/m².

4 Click **=** Evaluate.

TABLE

I Go to the Table window.

The result should be close to 8.5 W.

RESULTS

Surface Integration 2

- I In the Results toolbar, click ^{8.85}_{e-12} More Derived Values and choose Integration> Surface Integration.
- 2 In the Settings window for Surface Integration, locate the Selection section.
- **3** From the **Selection** list, choose **Circuit**.
- 4 Click Replace Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (comp1)>Electric Currents in Layered Shells>
 Heating and losses>ecis.Qsh Surface loss density, electromagnetic W/m².
- 5 Click **= Evaluate**.

TABLE

I Go to the Table window.

The result should be close to 13.8 W.