

Nonisothermal MEMS Heat Exchanger

The following example builds and solves a conduction and convection heat transfer problem using the Nonisothermal Flow multiphysics coupling.

The example concerns a stainless-steel MEMS heat exchanger, which you can find in labon-a-chip devices in biotechnology and in microreactors such as for micro fuel cells. This application examines the heat exchanger in 3D, and it involves heat transfer through both convection and conduction.

Model Definition — Heat Exchanger

Figure 1 shows the geometry of the heat exchanger. It is necessary to model only one unit cell because they are all almost identical except for edge effects in the outer cells.

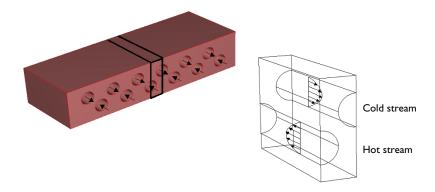


Figure 1: Depiction of the modeled part of the heat exchanger (left).

The governing equation for this model is the heat equation for conductive and convective heat transfer

$$\rho C_p \mathbf{u} \cdot \nabla T + \nabla \cdot (-k \nabla T) = Q$$

where C_p denotes the specific heat capacity (SI unit: J/(kg·K)), T is the temperature (SI unit: K), k is the thermal conductivity (SI unit: W/(m·K)), ρ is the density (SI unit: kg/ m^3), **u** is the velocity vector (SI unit: m/s), and Q is a sink or source term (which you set to zero because there is no production or consumption of heat in the device).

In the solid part of the heat exchanger the velocity is zero. In the channels the velocity field is determined using the Laminar Flow interface. With the Nonisothermal Flow

multiphysics coupling the flow computation also takes density and viscosity variations due to varying temperature into account.

The boundary conditions for heat transfer are insulating for all outer surfaces except for the inlet and outlet boundaries in the fluid channels. At the inlets, you specify constant temperatures for the cold and hot streams, $T_{\rm cold}$ and $T_{\rm hot}$, respectively. At the outlets, convection dominates the transport of heat so you apply the convective flux boundary condition:

$$-k\nabla T \cdot \mathbf{n} = 0$$

At the channel walls the velocity is zero. At the inlets a laminar velocity profile with an average velocity of 2.5 mm/s is applied. At the outlets where heat transport is dominated by convection the outlet boundary condition applies a constant pressure.

Results and Discussion

Figure 2 shows the temperature isosurfaces and the heat flux streamlines for the conductive heat flux in the device. The temperature isosurfaces clearly show the convective term's influence in the channels. Figure 3 displays the corresponding results for the extended application. As the plot shows, the temperature distribution is very similar to that in the first study, which can therefore be concluded to be a good approximation of the extended case.

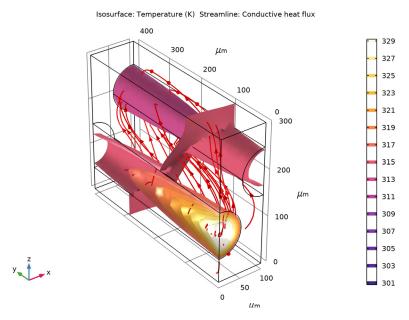


Figure 2: Isotherms and conductive heat flux streamlines in the cell unit's geometry.

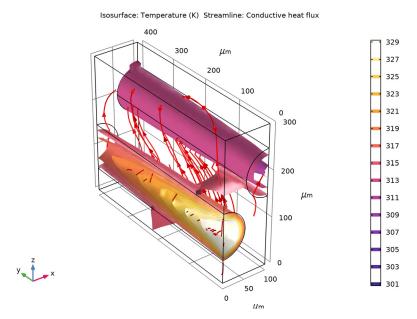


Figure 3: Extended application results; isotherms and conductive heat flux streamlines in the cell unit's geometry.

Application Library path: Heat Transfer Module/Heat Exchangers/ heat_exchanger_ni

Modeling Instruction

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click 1 3D.
- 2 In the Select Physics tree, select Fluid Flow>Nonisothermal Flow>Laminar Flow.
- 3 Click Add.

- 4 Click Study.
- 5 In the Select Study tree, select General Studies>Stationary.
- 6 Click Done.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description	
R	50[um]	5E-5 m	Channel radius	
v_mean	50[mm/s]	0.05 m/s	Mean velocity	
T_hot	330[K]	330 K	Temperature, hot channel	
T_cold	300[K]	300 K	Temperature, cold channel	
T_mean	(T_hot+T_cold)/2	315 K	Mean temperature	
rho_mean_w	1000[kg/m^3]	1000 kg/m³	Fluid mean density	

GEOMETRY I

- I In the Model Builder window, under Component I (compl) click Geometry I.
- 2 In the Settings window for Geometry, locate the Units section.
- 3 From the Length unit list, choose μm .

Block I (blk I)

- I In the Geometry toolbar, click Block.
- 2 In the Settings window for Block, locate the Size and Shape section.
- **3** In the **Width** text field, type 100.
- 4 In the **Depth** text field, type 400.
- 5 In the **Height** text field, type 300.
- 6 In the Geometry toolbar, click **Build All**.

Cylinder I (cyll)

- I In the Geometry toolbar, click (Cylinder.
- 2 In the Settings window for Cylinder, locate the Size and Shape section.

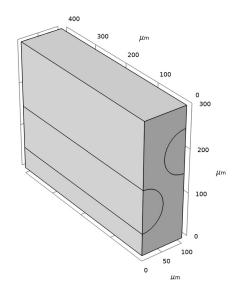
- 3 In the Radius text field, type R.
- 4 In the Height text field, type 400.
- 5 Locate the Position section. In the z text field, type 2*R.
- 6 Locate the Axis section. From the Axis type list, choose y-axis.
- 7 In the Geometry toolbar, click **Build All**.

Copy I (copy I)

- I In the Geometry toolbar, click Transforms and choose Copy.
- **2** Select the object **cyll** only.
- 3 In the Settings window for Copy, locate the Displacement section.
- 4 In the x text field, type 2*R.
- 5 In the z text field, type 2*R.
- 6 In the Geometry toolbar, click **Build All**.

Compose I (col)

- I In the Geometry toolbar, click Booleans and Partitions and choose Compose.
- 2 Click in the **Graphics** window and then press Ctrl+A to select all objects.
- 3 In the Settings window for Compose, locate the Compose section.
- 4 In the Set formula text field, type blk1*(cyl1+copy1)+blk1.
- 5 In the Geometry toolbar, click **Build All**.





Define some selections that will be useful during the model set-up.

DEFINITIONS

Solid

- I In the **Definitions** toolbar, click **\(\frac{1}{2} \) Explicit**.
- 2 In the Settings window for Explicit, type Solid in the Label text field.
- **3** Select Domain 1 only.

Hot Channel

- I In the **Definitions** toolbar, click **\(\frac{1}{2} \) Explicit**.
- 2 In the Settings window for Explicit, type Hot Channel in the Label text field.
- **3** Select Domain 2 only.

Cold Channel

- I In the **Definitions** toolbar, click **\(\) Explicit**.
- 2 In the Settings window for Explicit, type Cold Channel in the Label text field.
- **3** Select Domain 3 only.

Channels

- I In the **Definitions** toolbar, click **Union**.
- 2 In the Settings window for Union, type Channels in the Label text field.
- 3 Locate the Input Entities section. Under Selections to add, click + Add.
- 4 In the Add dialog box, in the Selections to add list, choose Hot Channel and Cold Channel.
- 5 Click OK.

Channel Walls

- I In the **Definitions** toolbar, click **Adjacent**.
- 2 In the Settings window for Adjacent, type Channel Walls in the Label text field.
- 3 Locate the Input Entities section. Under Input selections, click + Add.
- 4 In the Add dialog box, in the Input selections list, choose Solid and Channels.
- 5 Click OK.
- 6 In the Settings window for Adjacent, locate the Output Entities section.
- 7 Clear the Exterior boundaries check box.
- 8 Select the Interior boundaries check box.

Variables 1

- I In the **Definitions** toolbar, click **a= Local Variables**.
- 2 In the Settings window for Variables, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 From the Selection list, choose Channels.
- **5** Locate the **Variables** section. In the table, enter the following settings:

Name	Expression	Unit	Description
rho_w	rho_mean_w*(1-(T-T_mean)/T_mean)	kg/m³	Fluid density

ADD MATERIAL

- I In the Home toolbar, click **‡ Add Material** to open the **Add Material** window.
- 2 Go to the Add Material window.
- 3 In the tree, select Built-in>Steel AISI 4340.
- **4** Click **Add to Component** in the window toolbar.
- 5 In the tree, select Built-in>Water, liquid.
- **6** Click **Add to Component** in the window toolbar.
- 7 In the Home toolbar, click 🙀 Add Material to close the Add Material window.

MATERIALS

Steel AISI 4340 (mat1)

- I In the Model Builder window, under Component I (compl)>Materials click Steel AISI 4340 (mat I).
- 2 In the Settings window for Material, locate the Geometric Entity Selection section.
- 3 From the Selection list, choose Solid.

Water, liquid (mat2)

- I In the Model Builder window, click Water, liquid (mat2).
- 2 In the Settings window for Material, locate the Geometric Entity Selection section.
- 3 From the Selection list, choose Channels.

HEAT TRANSFER IN FLUIDS (HT)

I In the Model Builder window, under Component I (compl)>Heat Transfer in Fluids (ht) click Fluid 1.

- 2 In the Settings window for Fluid, locate the Thermodynamics, Fluid section.
- 3 From the Fluid type list, choose Gas/Liquid.
- **4** From the ρ list, choose **User defined**. In the associated text field, type rho w.
- **5** From the γ list, choose **User defined**.

Solid 1

- I In the Physics toolbar, click **Domains** and choose Solid.
- 2 In the Settings window for Solid, locate the Domain Selection section.
- 3 From the Selection list, choose Solid.

LAMINAR FLOW (SPF)

- I In the Model Builder window, under Component I (compl) click Laminar Flow (spf).
- 2 In the Settings window for Laminar Flow, locate the Domain Selection section.
- 3 From the Selection list, choose Channels.

Inlet I

- I In the Physics toolbar, click **Boundaries** and choose Inlet.
- 2 Select Boundary 5 only.
- 3 In the Settings window for Inlet, locate the Boundary Condition section.
- 4 From the list, choose Fully developed flow.
- 5 Locate the Fully Developed Flow section. In the U_{av} text field, type v_mean.

Inlet 2

- I In the Physics toolbar, click **Boundaries** and choose **Inlet**.
- 2 Select Boundary 15 only.
- 3 In the Settings window for Inlet, locate the Boundary Condition section.
- 4 From the list, choose Fully developed flow.
- 5 Locate the Fully Developed Flow section. In the U_{av} text field, type v_mean.

Outlet I

- I In the Physics toolbar, click **Boundaries** and choose **Outlet**.
- 2 Select Boundaries 11 and 14 only.

Symmetry I

- I In the Physics toolbar, click **Boundaries** and choose Symmetry.
- 2 Select Boundaries 4 and 17 only.

HEAT TRANSFER IN FLUIDS (HT)

In the Model Builder window, under Component I (compl) click Heat Transfer in Fluids (ht).

Inflow I

- I In the Physics toolbar, click **Boundaries** and choose Inflow.
- 2 Select Boundary 5 only.
- 3 In the Settings window for Inflow, locate the Upstream Properties section.
- **4** In the $T_{\rm ustr}$ text field, type T_hot.

Inflow 2

- I In the Physics toolbar, click **Boundaries** and choose Inflow.
- 2 Select Boundary 15 only.
- 3 In the Settings window for Inflow, locate the Upstream Properties section.
- **4** In the $T_{\rm ustr}$ text field, type T_cold.

Outflow I

- I In the Physics toolbar, click **Boundaries** and choose **Outflow**.
- **2** Select Boundaries 11 and 14 only.

MESH I

Free Triangular 1

- I In the Mesh toolbar, click A Boundary and choose Free Triangular.
- 2 In the Settings window for Free Triangular, locate the Boundary Selection section.
- 3 From the Selection list, choose Channel Walls.

Size 1

- I Right-click Free Triangular I and choose Size.
- 2 In the Settings window for Size, locate the Element Size section.
- **3** Click the **Custom** button.
- 4 Locate the Element Size Parameters section. Select the Maximum element size check box.
- 5 In the associated text field, type 10[um].

Free Tetrahedral I

- I In the Mesh toolbar, click A Free Tetrahedral.
- 2 In the Model Builder window, right-click Mesh I and choose Build All.

STUDY I

In the **Home** toolbar, click **Compute**.

RESULTS

Velocity (sbf)

The first default plot shows the velocity magnitude on slices.

Temperature (ht)

The third default plot shows the temperature on channel inner surfaces.

To reproduce Figure 3, proceed as follows:

Temperature Isosurfaces and Conductive Heat Flux Streamlines

- I In the Model Builder window, under Results click Isothermal Contours (ht).
- 2 In the Settings window for 3D Plot Group, type Temperature Isosurfaces and Conductive Heat Flux Streamlines in the Label text field.

Isosurface

- I In the Model Builder window, expand the Temperature Isosurfaces and Conductive Heat Flux Streamlines node, then click Isosurface.
- 2 In the Settings window for Isosurface, locate the Levels section.
- 3 From the Entry method list, choose Levels.
- 4 In the Levels text field, type range (301, 2, 329).

Temperature Isosurfaces and Conductive Heat Flux Streamlines

In the Model Builder window, click

Temperature Isosurfaces and Conductive Heat Flux Streamlines.

Streamline 1

- I In the Temperature Isosurfaces and Conductive Heat Flux Streamlines toolbar, click Streamline.
- 2 In the Settings window for Streamline, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)> Heat Transfer in Fluids>Domain fluxes>ht.dfluxx,...,ht.dfluxz - Conductive heat flux.
- 3 Locate the Streamline Positioning section. From the Positioning list, choose Startingpoint controlled.
- 4 Locate the Coloring and Style section. Find the Line style subsection. From the Type list, choose Tube.
- 5 Select the Radius scale factor check box.

- **6** Find the **Point style** subsection. From the **Type** list, choose **Arrow**.
- 7 In the Temperature Isosurfaces and Conductive Heat Flux Streamlines toolbar, click Plot.