



# Fluid-Structure Interaction in Aluminum Extrusion

## *Introduction*

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Out of all metals, the most frequently extruded is aluminum. Aluminum extrusion entails using a hydraulic ram to squeeze an aluminum bar through a die. This process will form the metal into a particular shape. Extruded aluminum is used in many manufacturing applications, such as building components for example. In massive forming processes like rolling or extrusion, metal alloys are deformed in a hot solid state with material flowing under ideally plastic conditions. Such processes can be simulated effectively using computational fluid dynamics, where the material is considered as a fluid with a very high viscosity that depends on velocity and temperature. Internal friction of the moving material acts as a heat source, so that the heat transfer equations are fully coupled with those ruling the fluid dynamics part. This approach is especially advantageous when large deformations are involved.

This model is adapted from a benchmark study in [Ref. 1](#). The original benchmark solves a thermal-structural coupling, because it is common practice in the simulation of such processes to use specific finite element codes that have the capability to couple the structural equations with heat transfer. The alternative scheme discussed here couples non-Newtonian flow with heat transfer equations. In addition, because it is useful to know the stress in the die due to fluid pressure and thermal loads, the model adds a structural mechanics analysis.

The die design is courtesy of Compes S.p.A., while the die geometry, boundary conditions, and experimental data are taken from [Ref. 1](#).

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**Note:** This application requires the Heat Transfer Module and the Structural Mechanics Module. In addition, it uses the Material Library.

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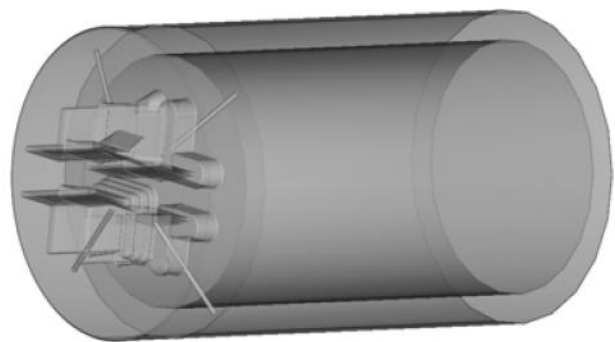
## *Model Definition*

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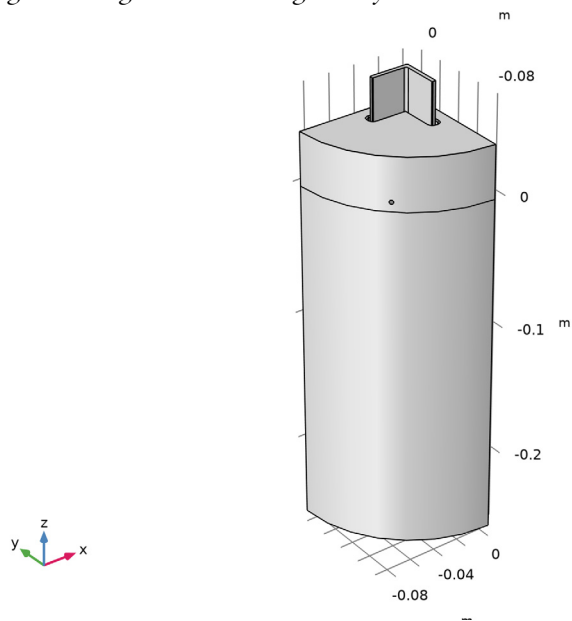
The model considers steady-state conditions, assuming a billet of infinite length flowing through the die. In the actual process, the billet is pushed by the ram through the die and its volume is continuously reducing.

[Figure 1](#) shows the original complete geometry with four different profiles. To have a model with reasonable dimensions, consider only a quarter of the original geometry. The

simplification involved in neglecting the differences between the four profiles does not affect the numerical scheme proposed. [Figure 2](#) shows the resulting model geometry.



*Figure 1: Original benchmark geometry.*



*Figure 2: Quarter of the original geometry considered in the model.*

## MATERIAL PROPERTIES

The documentation for the benchmark model (Ref. 1) serves as the data source for properties of the two main materials: AISI steel for the die and the container (the ram is not considered here) and aluminum for the billet.

### Structural Analysis

Because only the steel part is active in the structural analysis, consider a simple linear elastic behavior where the elastic properties are those of the material H11 mod (AISI 610) that can be found in the COMSOL Multiphysics Material Library.

### Heat Transfer Analysis

The benchmark model uses the following properties for aluminum and steel:

| ALUMINUM    | VALUE                                    | DESCRIPTION                        |
|-------------|------------------------------------------|------------------------------------|
| $k_{al}$    | 210 N/(s·K)                              | Thermal conductivity               |
| $\rho_{al}$ | 2700 kg/m <sup>3</sup>                   | Density                            |
| $C_{pal}$   | 2.94 N/(mm <sup>2</sup> ·K)/ $\rho_{al}$ | Heat capacity at constant pressure |
| STEEL       | VALUE                                    | DESCRIPTION                        |
| $k_{fe}$    | 24.33 N/(s·K)                            | Thermal conductivity               |
| $\rho_{fe}$ | 7850 kg/m <sup>3</sup>                   | Density                            |
| $C_{pfe}$   | 4.63 N/(mm <sup>2</sup> ·K)/ $\rho_{fe}$ | Heat capacity at constant pressure |

### Non-Newtonian Flow

The properties of the aluminum were experimentally determined and then checked using literature data for the same alloy and surface state. However the benchmark proposes an experimental constitutive law, suited for the structural mechanics codes usually used to simulate such processes, in the form of the flow stress data. For this model this requires a recalculation of the constitutive law to derive a general expression for the viscosity. The equivalent von Mises stress,  $\sigma_{eqv}$ , can be defined in terms of the total contraction of the deviatoric stress tensor as

$$\sigma_{eqv} = \sqrt{\frac{3}{2} \boldsymbol{\tau} : \boldsymbol{\tau}}$$

or, using  $\boldsymbol{\tau} = 2\eta \dot{\boldsymbol{\epsilon}}$  where  $\dot{\boldsymbol{\epsilon}}$  is the strain rate and  $\eta$  is the viscosity, as

$$\sigma_{eqv} = \sqrt{6\eta^2 \dot{\boldsymbol{\epsilon}} : \dot{\boldsymbol{\epsilon}}} \quad (1)$$

Introducing the equivalent strain rate

$$\dot{\phi}_{\text{eqv}} \equiv \sqrt{\frac{2}{3} \dot{\boldsymbol{\varepsilon}} : \dot{\boldsymbol{\varepsilon}}}$$

Equation 1 can be expressed as

$$\sigma_{\text{eqv}} = 3\eta\dot{\phi}_{\text{eqv}}$$

The strain rate tensor is defined as (Ref. 2)

$$\dot{\boldsymbol{\varepsilon}} = \frac{\nabla \mathbf{u} + (\nabla \mathbf{u})^T}{2} = \frac{1}{2} \dot{\boldsymbol{\gamma}}$$

The shear rate  $\dot{\boldsymbol{\gamma}}$  is defined as

$$\dot{\boldsymbol{\gamma}} = |\dot{\boldsymbol{\gamma}}| = \sqrt{\frac{1}{2} \dot{\boldsymbol{\gamma}} : \dot{\boldsymbol{\gamma}}}$$

so that

$$\dot{\phi}_{\text{eqv}} = \frac{1}{\sqrt{3}} \dot{\boldsymbol{\gamma}}$$

The flow rule

$$\sigma_{\text{eqv}} = \kappa_f$$

states that plastic yielding occurs if the equivalent stress,  $\sigma_{\text{eqv}}$ , reaches the flow stress,  $\kappa_f$ . The viscosity is defined as (see Ref. 2 for further details)

$$\eta = \frac{\kappa_f}{3\dot{\phi}_{\text{eqv}}}$$

The organizers of the benchmark propose specific flow-stress data expressed in terms of a generalized Zener-Hollomon function

$$\eta = \frac{\text{asinh}\left(\left(\frac{Z}{A}\right)^{\frac{1}{n}}\right)}{\sqrt{3}\alpha\dot{\boldsymbol{\gamma}}}$$

where  $A = 2.39 \cdot 10^8 \text{ s}^{-1}$ ,  $n = 2.976$ ,  $\alpha = 0.052 \text{ MPa}^{-1}$ , and

$$Z = \frac{1}{\sqrt{3}} \dot{\gamma} e^{\left(\frac{Q}{RT}\right)}$$

with  $Q = 153 \text{ kJ/mol}$  and  $R = 8.314 \text{ J/(K}\cdot\text{mol)}$ .

## SOURCES, INITIAL CONDITIONS, AND BOUNDARY CONDITIONS

### *Structural Analysis*

Because the model geometry is a quarter of the actual geometry, use symmetric boundary conditions for the two orthogonal planes. On the external surfaces of the die, apply roller boundary conditions because in reality other dies, not considered here, are present to increase the system's stiffness.

The main loads are the thermal loads from the heat transfer analysis and the total stress from the fluid dynamics analysis.

### *Heat Transfer Analysis*

For the billet, use a volumetric heat source related to the viscous heating effect.

The external temperature of the ram and the die is held constant at  $450^\circ\text{C}$  (723 K). The ambient temperature is  $25^\circ\text{C}$  (298 K). For the heat exchange between aluminum and steel, use the heat transfer coefficient of  $11 \text{ N/(s}\cdot\text{mm}\cdot\text{K)}$ . Also consider convective heat exchange with air outside the profiles with a fixed convective heat transfer coefficient of  $15 \text{ W/(m}^2\cdot\text{K)}$ .

Apply initial temperatures as given in the following table:

| PART      | VALUE                       |
|-----------|-----------------------------|
| Ram       | $380^\circ\text{C}$ (653 K) |
| Container | $450^\circ\text{C}$ (723 K) |
| Billet    | $460^\circ\text{C}$ (733 K) |
| Die       | $404^\circ\text{C}$ (677 K) |

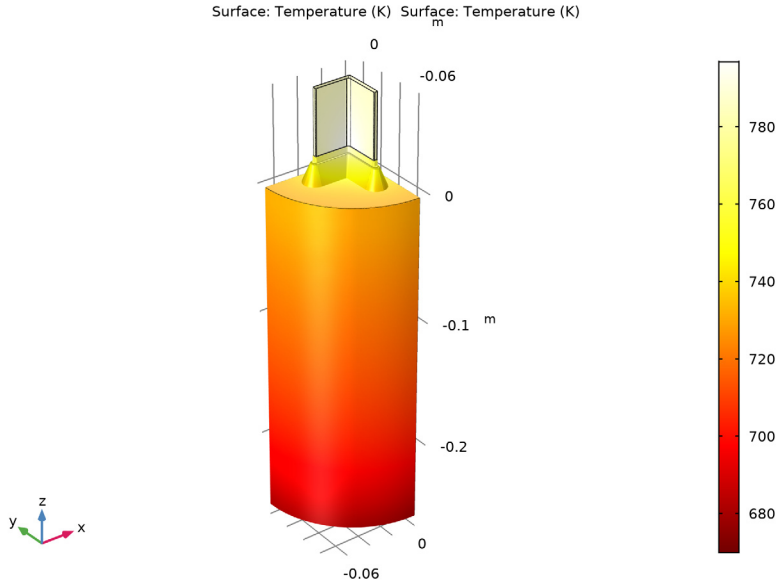
### *Non-Newtonian Flow*

At the inlet, the ram moves with a constant velocity of  $0.5 \text{ mm/s}$ . Impose this boundary condition by simply applying a constant inlet velocity. At the outlet, a normal stress condition with zero external pressure applies. On the surfaces placed on the two symmetry planes, use symmetric conditions. Finally, apply slip boundary conditions on the boundaries placed outside the profile.

## Results and Discussion

The general response of the proposed numerical scheme, especially in the zone of the profile, is in good accordance with the experience of the designers. A comparison between the available experimental data and the numerical results of the simulation shows good agreement.

On the basis of the results from the simulation, the engineer can improve the preliminary die design by adjusting relevant physical parameters and operating conditions. For this purpose, the volume plot in [Figure 3](#) showing the temperature field inside the profile gives important information. Furthermore, the combined streamline and slice plot in [Figure 4](#) reveals any imbalances in the velocity field that could result in a crooked profile. A proper design should also ensure that different parts of the profile travel at the same speed. [Figure 5](#) shows the von Mises equivalent stress in the steel part considering the thermal load and the pressure load due to the presence of the fluid.



*Figure 3: Temperature distribution in the billet.*

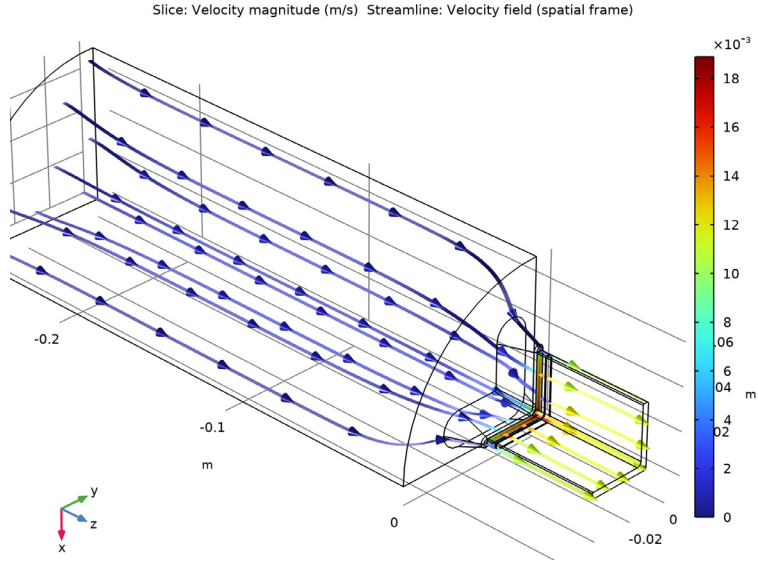


Figure 4: Velocity field and streamlines at the profile section.

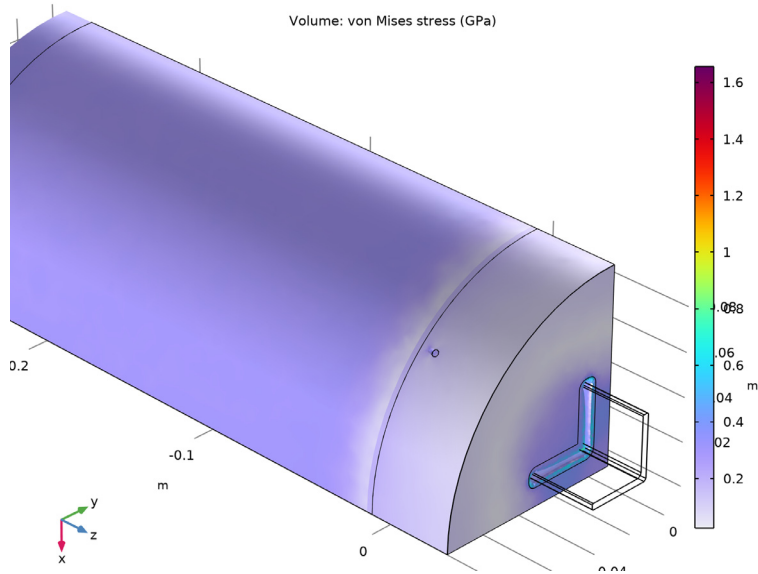


Figure 5: Equivalent von Mises stress distribution in the container.

## References

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1. M. Schikorra, L. Donati, L. Tomesani, and A.E. Tekkaya, “The Extrusion Benchmark 2007,” *Proceedings of the Extrusion Workshop 2007 and 2nd Extrusion Benchmark Conference*, Bologna, Italy, <http://diemtech.ing.unibo.it/extrusion07>.
2. E.D. Schmitter, “Modelling massive forming processes with thermally coupled fluid dynamics,” *Proceedings of the COMSOL Multiphysics User's Conference 2005* Frankfurt, Frankfurt, Germany.

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**Application Library path:** Heat\_Transfer\_Module/Thermal\_Processing/  
aluminum\_extrusion\_fsi

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## Modeling Instructions

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From the **File** menu, choose **New**.

### NEW

In the **New** window, click  **Model Wizard**.

### MODEL WIZARD

- 1 In the **Model Wizard** window, click  **3D**.
- 2 In the **Select Physics** tree, select **Heat Transfer>Conjugate Heat Transfer>Laminar Flow**.
- 3 Click **Add**.
- 4 In the **Select Physics** tree, select **Structural Mechanics>Solid Mechanics (solid)**.
- 5 Click **Add**.
- 6 Click  **Study**.
- 7 In the **Select Study** tree, select **General Studies>Stationary**.
- 8 Click  **Done**.

### GEOMETRY I

*Import I (impl)*

- 1 In the **Home** toolbar, click  **Import**.
- 2 In the **Settings** window for **Import**, locate the **Import** section.
- 3 Click  **Browse**.

4 Browse to the model's Application Libraries folder and double-click the file `aluminum_extrusion_fsi.mphbin`.

5 Click  **Import**.

6 Click the  **Zoom Extents** button in the **Graphics** toolbar.

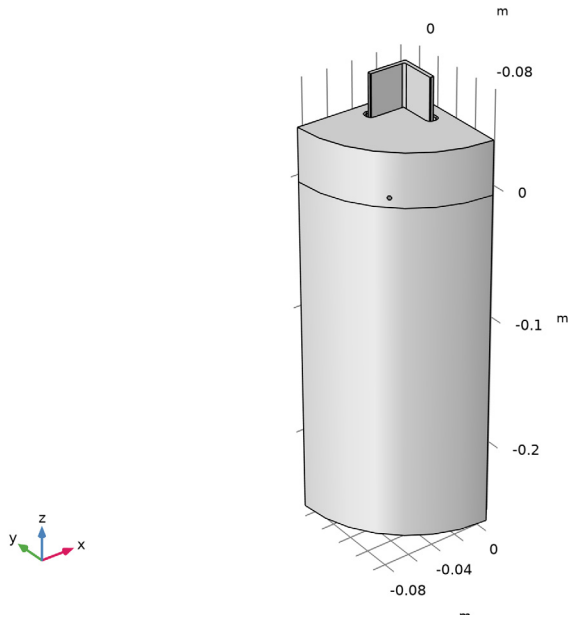
The imported geometry contains narrow face regions, which are not necessary for this model and will increase the number of elements significantly. Add a **Remove Details** feature to remove these details.

*Remove Details 1 (rmd1)*

1 In the **Geometry** toolbar, click  **Remove Details**.

2 Click  **Build All**.

You should now see the following geometry.



## GLOBAL DEFINITIONS

*Parameters 1*

1 In the **Model Builder** window, under **Global Definitions** click **Parameters 1**.

2 In the **Settings** window for **Parameters**, locate the **Parameters** section.

**3** In the table, enter the following settings:

| Name        | Expression     | Value                       | Description                                                        |
|-------------|----------------|-----------------------------|--------------------------------------------------------------------|
| D_alfe      | 1[mm]          | 0.001 m                     | Thickness of the high conductive layer                             |
| Heat_alfe   | 11[N/(s*mm*K)] | 11000 W/(m <sup>2</sup> *K) | Aluminum-steel heat exchange coefficient                           |
| T_billet    | 460[degC]      | 733.15 K                    | Billet temperature                                                 |
| T_container | 450[degC]      | 723.15 K                    | Container temperature                                              |
| T_ram       | 380[degC]      | 653.15 K                    | Ram temperature                                                    |
| T_pd1       | 404[degC]      | 677.15 K                    | Initial temperature around thermocouple at point PD1               |
| V_ram       | 0.5[mm/s]      | 5E-4 m/s                    | Ram velocity                                                       |
| P_init      | 0[bar]         | 0 Pa                        | External reference pressure                                        |
| T_air       | 25[degC]       | 298.15 K                    | Ambient temperature                                                |
| Q_eta       | 153000[J/mol]  | 1.53E5 J/mol                | Parameter Q for the generalized Zener-Hollomon function            |
| n_eta       | 2.976          | 2.976                       | Parameter n for the generalized Zener-Hollomon function            |
| A_eta       | 2.39e8[1/s]    | 2.39E8 1/s                  | Parameter A for the generalized Zener-Hollomon function            |
| alpha_eta   | 0.0521[1/MPa]  | 5.21E-8 1/Pa                | Parameter alpha for the generalized Zener-Hollomon function        |
| H_conv      | 15             | 15                          | Convective heat exchange coefficient with air                      |
| F           | sqrt(1/3)      | 0.57735                     | Factor for the conversion of the shear rate to COMSOL's definition |

## DEFINITIONS

*Variables /*

**1** In the **Home** toolbar, click  **Variables** and choose **Local Variables**.

**2** In the **Settings** window for **Variables**, locate the **Variables** section.

3 In the table, enter the following settings:

| Name  | Expression                                                                                                                                                                  | Unit | Description              |
|-------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------|--------------------------|
| Z_eta | $F \cdot \text{spf} \cdot \text{sr} \cdot \exp(Q_{\text{eta}} / (R_{\text{const}} \cdot T))$                                                                                | l/s  | Zener-Hollomon parameter |
| mu_al | $\text{asinh}((Z_{\text{eta}} / A_{\text{eta}})^{(1/n_{\text{eta}})}) / (3 \cdot \alpha_{\text{eta}} \cdot F \cdot \text{spf} \cdot \text{sr} + \sqrt{\epsilon \text{ps}})$ | Pa·s | Viscosity of aluminum    |

Create the selections to simplify the model specification.

#### Outside

- 1 In the **Definitions** toolbar, click  **Explicit**.
- 2 In the **Settings** window for **Explicit**, type Outside in the **Label** text field.
- 3 Locate the **Input Entities** section. From the **Geometric entity level** list, choose **Boundary**.
- 4 Select Boundaries 35–38, 42, 43, 50, 51, 53, 55, 70, 71, 79–82, 87, 88, 93, 95, 102, 103, 106, and 108 only.  
For more convenience in selecting these boundaries, you can click the **Paste Selection** button and paste the above numbers.

#### Interior

- 1 In the **Definitions** toolbar, click  **Explicit**.
- 2 In the **Settings** window for **Explicit**, type Interior in the **Label** text field.
- 3 Locate the **Input Entities** section. From the **Geometric entity level** list, choose **Boundary**.
- 4 Select Boundaries 8, 11, 14, 15, 19, 20, 24, 29–34, 41, 44, 45, 49, 52, 58–60, 64, 69, 72, 73, 76–78, 86, 89–92, 101, 104, 105, and 109 only.

Before creating the materials for the model, specify the fluid and solid domains. Using this information, the software can detect which material properties are needed.

### HEAT TRANSFER IN SOLIDS AND FLUIDS (HT)

#### Fluid 1

- 1 In the **Model Builder** window, under **Component 1 (comp1)> Heat Transfer in Solids and Fluids (ht)** click **Fluid 1**.
- 2 Select Domains 3 and 4 only.
- 3 In the **Settings** window for **Fluid**, locate the **Domain Selection** section.
- 4 Click  **Create Selection**.
- 5 In the **Create Selection** dialog box, type Billet in the **Selection name** text field.

6 Click **OK**.

#### **LAMINAR FLOW (SPF)**

- 1 In the **Model Builder** window, under **Component 1 (comp1)** click **Laminar Flow (spf)**.
- 2 In the **Settings** window for **Laminar Flow**, locate the **Physical Model** section.
- 3 From the **Compressibility** list, choose **Incompressible flow**.
- 4 Locate the **Domain Selection** section. From the **Selection** list, choose **Billet**.

#### **SOLID MECHANICS (SOLID)**

- 1 In the **Model Builder** window, under **Component 1 (comp1)** click **Solid Mechanics (solid)**.
- 2 In the **Settings** window for **Solid Mechanics**, locate the **Domain Selection** section.
- 3 Click  **Clear Selection**.
- 4 Select Domains 1 and 2 only.

Now, define the material for each domain.

#### **ADD MATERIAL**

- 1 In the **Home** toolbar, click  **Add Material** to open the **Add Material** window.
- 2 Go to the **Add Material** window.
- 3 In the tree, select **Material Library>Tool Steels>H11 mod (AISI 610)>H11 mod (AISI 610) [solid]**.
- 4 Click **Add to Component** in the window toolbar.
- 5 In the **Home** toolbar, click  **Add Material** to close the **Add Material** window.

#### **MATERIALS**

*H11 mod (AISI 610) [solid] (mat1)*

- 1 Select Domains 1 and 2 only.
- 2 In the **Settings** window for **Material**, locate the **Material Contents** section.

3 In the table, enter the following settings:

| Property                           | Variable | Value                                                     | Unit     | Property group |
|------------------------------------|----------|-----------------------------------------------------------|----------|----------------|
| Heat capacity at constant pressure | Cp       | $4.63 [N / (mm^2 \cdot K)] / \rho (T [1 / K]) [kg / m^3]$ | J/(kg·K) | Basic          |

The heat capacity is not used since it does not enter in the stationary heat transfer equation for solids without translational movement. The heat capacity is only provided for completeness in case you want to extend the model to perform transient simulations.

#### Billet

- 1 In the **Materials** toolbar, click  **Blank Material**.
- 2 In the **Settings** window for **Material**, type Billet in the **Label** text field.
- 3 Locate the **Geometric Entity Selection** section. From the **Selection** list, choose **Billet**.
- 4 Locate the **Material Contents** section. In the table, enter the following settings:

| Property                           | Variable                     | Value                              | Unit     | Property group |
|------------------------------------|------------------------------|------------------------------------|----------|----------------|
| Thermal conductivity               | k_iso ; kii = k_iso, kij = 0 | 210                                | W/(m·K)  | Basic          |
| Density                            | rho                          | 2700                               | kg/m³    | Basic          |
| Heat capacity at constant pressure | Cp                           | $2.94 [N / (mm^2 \cdot K)] / \rho$ | J/(kg·K) | Basic          |
| Dynamic viscosity                  | mu                           | mu_a1                              | Pa·s     | Basic          |

#### H11 mod (AISI 610) [solid] 1 (mat3)

- 1 In the **Model Builder** window, under **Component 1 (comp1)>Materials** right-click **H11 mod (AISI 610) [solid] (mat1)** and choose **Duplicate**.
- 2 In the **Settings** window for **Material**, locate the **Geometric Entity Selection** section.
- 3 From the **Geometric entity level** list, choose **Boundary**.
- 4 From the **Selection** list, choose **Interior**.

Now, define the volume reference temperature in the solid domains. This temperature is used by materials to define the density in solids for both the **Heat Transfer in Solids and Fluids** and **Solid Mechanics** interfaces, and by the **Thermal Expansion** feature as the zero strain reference.

## DEFINITIONS

### *Model Input 1*

- 1 In the **Physics** toolbar, click  **Shared Properties** and choose **Model Input**.
- 2 Select Domain 1 only.
- 3 In the **Settings** window for **Model Input**, locate the **Definition** section.
- 4 Click  **Select Quantity**.
- 5 In the **Physical Quantity** dialog box, type temperature in the text field.
- 6 Click  **Filter**.
- 7 In the tree, select **General>Volume reference temperature (K)**.
- 8 Click **OK**.
- 9 In the **Settings** window for **Model Input**, locate the **Definition** section.
- 10 In the text field, type  $T_{\text{container}}$ .

This value overrides the value defined under **Default Model Inputs** for the selected domain.

### *Model Input 2*

- 1 In the **Physics** toolbar, click  **Shared Properties** and choose **Model Input**.
- 2 Select Domain 2 only.
- 3 In the **Settings** window for **Model Input**, locate the **Definition** section.
- 4 Click  **Select Quantity**.
- 5 In the **Physical Quantity** dialog box, select **General>Volume reference temperature (K)** in the tree.
- 6 Click **OK**.
- 7 In the **Settings** window for **Model Input**, locate the **Definition** section.
- 8 In the text field, type  $T_{\text{pd1}}$ .

With the materials defined, you can set up the remaining physics of the model.

## LAMINAR FLOW (SPF)

In the current model, the high viscosity of the fluid flow implies that the model is diffusion dominated. Pseudo time stepping is thus not adapted to this case as it is based on the scale of the convective flux.

- 1 Click the  **Show More Options** button in the **Model Builder** toolbar.

- 2 In the **Show More Options** dialog box, in the tree, select the check box for the node **Physics>Advanced Physics Options**.
- 3 Click **OK**.
- 4 In the **Model Builder** window, click **Laminar Flow (spf)**.
- 5 In the **Settings** window for **Laminar Flow**, click to expand the **Advanced Settings** section.
- 6 Find the **Pseudo time stepping** subsection. From the **Use pseudo time stepping for stationary equation form** list, choose **Off**.

#### *Initial Values 1*

- 1 In the **Model Builder** window, under **Component 1 (comp1)>Laminar Flow (spf)** click **Initial Values 1**.
- 2 In the **Settings** window for **Initial Values**, locate the **Initial Values** section.
- 3 In the  $p$  text field, type  $P_{init}$ .

#### *Symmetry 1*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Symmetry**.
- 2 Select Boundaries 9 and 114 only.

#### *Inlet 1*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Inlet**.
- 2 Select Boundary 10 only.
- 3 In the **Settings** window for **Inlet**, locate the **Velocity** section.
- 4 Click the **Velocity field** button.
- 5 Specify the  $\mathbf{u}_0$  vector as

|           |   |
|-----------|---|
| 0         | x |
| 0         | y |
| $v_{ram}$ | z |

#### *Wall 2*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Wall**.
- 2 In the **Settings** window for **Wall**, locate the **Boundary Selection** section.
- 3 From the **Selection** list, choose **Outside**.
- 4 Locate the **Boundary Condition** section. From the **Wall condition** list, choose **Slip**.

#### *Outlet 1*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Outlet**.

- 2 Select Boundary 40 only.
- 3 In the **Settings** window for **Outlet**, locate the **Pressure Conditions** section.
- 4 In the  $p_0$  text field, type  $P_{init}$ .

## HEAT TRANSFER IN SOLIDS AND FLUIDS (HT)

### *Initial Values 1*

- 1 In the **Model Builder** window, under **Component 1 (comp1)> Heat Transfer in Solids and Fluids (ht)** click **Initial Values 1**.
- 2 In the **Settings** window for **Initial Values**, locate the **Initial Values** section.
- 3 In the  $T$  text field, type  $T_{container}$ .

### *Temperature 1*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Temperature**.
- 2 Select Boundaries 2, 5, and 7 only.
- 3 In the **Settings** window for **Temperature**, locate the **Temperature** section.
- 4 In the  $T_0$  text field, type  $T_{container}$ .

### *Heat Flux 1*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Heat Flux**.
- 2 Select Boundary 10 only.
- 3 In the **Settings** window for **Heat Flux**, locate the **Heat Flux** section.
- 4 From the **Flux type** list, choose **Convective heat flux**.
- 5 In the  $h$  text field, type  $Heat_{alfe}$ .
- 6 In the  $T_{ext}$  text field, type  $T_{ram}$ .

### *Heat Flux 2*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Heat Flux**.
- 2 In the **Settings** window for **Heat Flux**, locate the **Boundary Selection** section.
- 3 From the **Selection** list, choose **Outside**.
- 4 Locate the **Heat Flux** section. From the **Flux type** list, choose **Convective heat flux**.
- 5 In the  $h$  text field, type  $H_{conv}$ .
- 6 In the  $T_{ext}$  text field, type  $T_{air}$ .

### *Outflow 1*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Outflow**.
- 2 Select Boundary 40 only.

### Thin Layer 1

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Thin Layer**.
- 2 In the **Settings** window for **Thin Layer**, locate the **Boundary Selection** section.
- 3 From the **Selection** list, choose **Interior**.
- 4 Locate the **Layer Model** section. From the **Specify** list, choose **Thermal resistance**.
- 5 Locate the **Heat Conduction** section. In the  $R_s$  text field, type  $1/\text{Heat\_alfe}$ .

## MATERIALS

### H11 mod (AISI 610) [solid] 1 (mat3)

- 1 In the **Model Builder** window, under **Component 1 (comp1)**>**Materials** click **H11 mod (AISI 610) [solid] 1 (mat3)**.
- 2 In the **Settings** window for **Material**, locate the **Material Contents** section.
- 3 In the table, enter the following settings:

| Property  | Variable | Value  | Unit | Property group |
|-----------|----------|--------|------|----------------|
| Thickness | lth      | D_alfe | m    | Shell          |

## SOLID MECHANICS (SOLID)

For faster convergence use linear elements. You can always improve the solution using the default quadratic elements.

- 1 In the **Model Builder** window, under **Component 1 (comp1)** click **Solid Mechanics (solid)**.
- 2 In the **Settings** window for **Solid Mechanics**, click to expand the **Discretization** section.
- 3 From the **Displacement field** list, choose **Linear**.

### Linear Elastic Material 1

Both Young's modulus and Poisson's ratio are temperature dependent. Follow these steps to verify that the temperature is defined by the **Heat Transfer in Solids and Fluids** interface.

- 1 In the **Model Builder** window, under **Component 1 (comp1)**>**Solid Mechanics (solid)** click **Linear Elastic Material 1**.
- 2 In the **Settings** window for **Linear Elastic Material**, locate the **Model Input** section.
- 3 Click  **Go to Source** for **Temperature** for the **Temperature ( $T$ )**.

## GLOBAL DEFINITIONS

### *Default Model Inputs*

Locate the **Browse Model Inputs** section. The icon column of the table under **Model input contributions** shows that it is the **Heat Transfer in Solids and Fluids** interface that defines the temperature in the solid and fluid domains and on the thin-layer boundaries.

## SOLID MECHANICS (SOLID)

### *Roller I*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Roller**.
- 2 Select Boundaries 2, 5, and 7 only.

### *Symmetry I*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Symmetry**.
- 2 Select Boundaries 1, 4, 112, and 113 only.

## MULTIPHYSICS

### *Fluid-Structure Interaction I (fsi I)*

- 1 In the **Physics** toolbar, click  **Multiphysics Couplings** and choose **Boundary>Fluid-Structure Interaction**.
- 2 In the **Settings** window for **Fluid-Structure Interaction**, locate the **Boundary Selection** section.
- 3 From the **Selection** list, choose **All boundaries**.

### *Thermal Expansion I (te I)*

- 1 In the **Physics** toolbar, click  **Multiphysics Couplings** and choose **Domain>Thermal Expansion**.
- 2 Select Domains 1 and 2 only.

## MESH I

### *Free Triangular I*

- 1 In the **Mesh** toolbar, click  **Boundary** and choose **Free Triangular**.
- 2 Select Boundary 40 only.

### *Size I*

- 1 Right-click **Free Triangular I** and choose **Size**.
- 2 In the **Settings** window for **Size**, locate the **Element Size** section.

- 3 Click the **Custom** button.
- 4 Locate the **Element Size Parameters** section. Select the **Maximum element size** check box.
- 5 In the associated text field, type 0.0014.
- 6 Select the **Curvature factor** check box.
- 7 In the associated text field, type 0.2.
- 8 Click  **Build Selected**.

#### *Swept 1*

- 1 In the **Mesh** toolbar, click  **Swept**.
- 2 In the **Settings** window for **Swept**, locate the **Domain Selection** section.
- 3 From the **Geometric entity level** list, choose **Domain**.
- 4 Select Domain 4 only.

#### *Distribution 1*

- 1 Right-click **Swept 1** and choose **Distribution**.
- 2 In the **Settings** window for **Distribution**, locate the **Distribution** section.
- 3 In the **Number of elements** text field, type 24.
- 4 Click  **Build All**.

#### *Free Tetrahedral 1*

In the **Mesh** toolbar, click  **Free Tetrahedral**.

#### *Size 1*

- 1 Right-click **Free Tetrahedral 1** and choose **Size**.
- 2 In the **Settings** window for **Size**, locate the **Element Size** section.
- 3 Click the **Custom** button.
- 4 Locate the **Element Size Parameters** section. Select the **Maximum element size** check box.
- 5 In the associated text field, type 0.0085.

#### *Size 2*

- 1 In the **Model Builder** window, right-click **Free Tetrahedral 1** and choose **Size**.
- 2 In the **Settings** window for **Size**, locate the **Geometric Entity Selection** section.
- 3 From the **Geometric entity level** list, choose **Boundary**.
- 4 Select Boundaries 12 and 13 only.
- 5 Locate the **Element Size** section. Click the **Custom** button.
- 6 Locate the **Element Size Parameters** section. Select the **Maximum element size** check box.

7 In the associated text field, type 0.002.

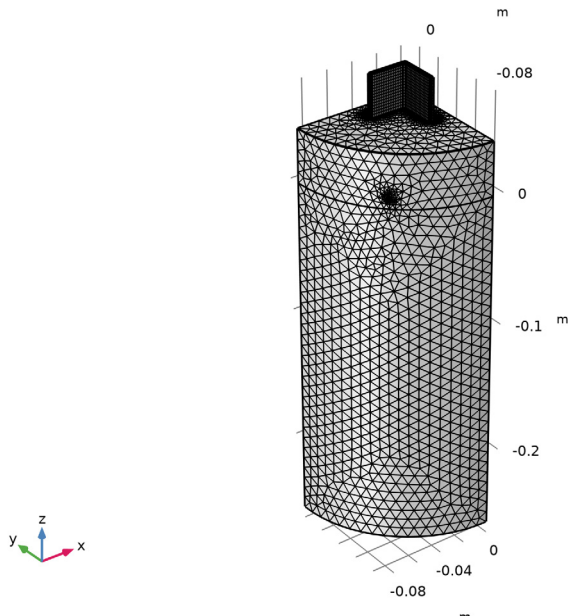
#### Size 3

- 1 Right-click **Free Tetrahedral 1** and choose **Size**.
- 2 In the **Settings** window for **Size**, locate the **Geometric Entity Selection** section.
- 3 From the **Geometric entity level** list, choose **Domain**.
- 4 Select Domain 3 only.
- 5 Locate the **Element Size** section. Click the **Custom** button.
- 6 Locate the **Element Size Parameters** section. Select the **Minimum element size** check box.
- 7 In the associated text field, type  $5e-4$ .

#### Size

- 1 In the **Model Builder** window, under **Component 1 (comp1)**>**Mesh 1** click **Size**.
- 2 In the **Settings** window for **Size**, locate the **Element Size** section.
- 3 From the **Predefined** list, choose **Finer**.
- 4 Click  **Build All**.

You should now see the following meshed geometry.



## STUDY 1

### *Step 1: Stationary*

Use two stationary study steps. Solve first for the fluid dynamics and heat transfer to determine the thermal load and the pressure load and then for the structural mechanics.

- 1 In the **Model Builder** window, under **Study 1** click **Step 1: Stationary**.
- 2 In the **Settings** window for **Stationary**, locate the **Physics and Variables Selection** section.
- 3 In the table, clear the **Solve for** check box for **Solid Mechanics (solid)**.
- 4 In the table, clear the **Solve for** check boxes for **Fluid-Structure Interaction 1 (fsi1)** and **Thermal Expansion 1 (tel)**.

### *Stationary 2*

- 1 In the **Study** toolbar, click  **Study Steps** and choose **Stationary>Stationary**.
- 2 In the **Settings** window for **Stationary**, locate the **Physics and Variables Selection** section.
- 3 In the table, clear the **Solve for** check boxes for **Heat Transfer in Solids and Fluids (ht)** and **Laminar Flow (spf)**.
- 4 In the table, clear the **Solve for** check box for **Nonisothermal Flow 1 (nitf1)**.

For the structural analysis, use a memory efficient iterative solver to make it possible to solve the problem also on computers with limited memory.

### *Solution 1 (sol1)*

- 1 In the **Study** toolbar, click  **Show Default Solver**.
- 2 In the **Model Builder** window, expand the **Solution 1 (sol1)** node.
- 3 In the **Model Builder** window, expand the **Study 1>Solver Configurations>Solution 1 (sol1)>Stationary Solver 2** node.
- 4 Right-click **Study 1>Solver Configurations>Solution 1 (sol1)>Stationary Solver 2** and choose **Iterative**.
- 5 In the **Study** toolbar, click  **Compute**.

## RESULTS

### *Temperature (ht)*

The first default plot shows the temperature (Figure 3).

- 1 In the **Settings** window for **3D Plot Group**, locate the **Data** section.
- 2 From the **Dataset** list, choose **Exterior Walls**.

### *Surface 2*

- 1 In the **Model Builder** window, expand the **Temperature (ht)** node, then click **Surface 2**.
- 2 In the **Settings** window for **Surface**, click to expand the **Title** section.
- 3 From the **Title type** list, choose **None**.
- 4 In the **Temperature (ht)** toolbar, click  **Plot**.

Modify the third default plot to see the velocity field and streamlines at the profile section (Figure 4).

### *Study 1/Solution Store 1 (sol2)*

In the **Model Builder** window, expand the **Results>Datasets** node, then click **Study 1/Solution Store 1 (sol2)**.

### *Selection*

- 1 In the **Results** toolbar, click  **Attributes** and choose **Selection**.
- 2 In the **Settings** window for **Selection**, locate the **Geometric Entity Selection** section.
- 3 From the **Geometric entity level** list, choose **Domain**.
- 4 From the **Selection** list, choose **Billet**.

### *Velocity (spf)*

- 1 In the **Model Builder** window, under **Results** click **Velocity (spf)**.
- 2 In the **Settings** window for **3D Plot Group**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Study 1/Solution Store 1 (sol2)**.

### *Slice*

- 1 In the **Model Builder** window, expand the **Velocity (spf)** node, then click **Slice**.
- 2 In the **Settings** window for **Slice**, locate the **Plane Data** section.
- 3 From the **Plane** list, choose **xy-planes**.
- 4 From the **Entry method** list, choose **Coordinates**.
- 5 In the **z-coordinates** text field, type 0.0151.
- 6 In the **Velocity (spf)** toolbar, click  **Plot**.

### *Velocity (spf)*

In the **Model Builder** window, click **Velocity (spf)**.

### *Streamline 1*

- 1 In the **Velocity (spf)** toolbar, click  **Streamline**.

- 2 In the **Settings** window for **Streamline**, click **Replace Expression** in the upper-right corner of the **Expression** section. From the menu, choose **Component 1 (comp1)>Laminar Flow>Velocity and pressure>u,v,w - Velocity field (spatial frame)**.
- 3 Locate the **Streamline Positioning** section. From the **Positioning** list, choose **Magnitude controlled**.
- 4 In the **Min distance** text field, type 0.01.
- 5 In the **Max distance** text field, type 0.1.
- 6 Locate the **Coloring and Style** section. Find the **Line style** subsection. From the **Type** list, choose **Ribbon**.
- 7 In the **Width expression** text field, type 0.001.
- 8 Select the **Width scale factor** check box.
- 9 Find the **Point style** subsection. From the **Type** list, choose **Arrow**.
- 10 Select the **Number of arrows** check box.
- 11 In the associated text field, type 70.
- 12 Click to expand the **Inherit Style** section.

#### *Color Expression 1*

- 1 In the **Velocity (spf)** toolbar, click  **Color Expression**.
- 2 In the **Settings** window for **Color Expression**, click **Replace Expression** in the upper-right corner of the **Expression** section. From the menu, choose **Component 1 (comp1)>Laminar Flow>Velocity and pressure>spf.U - Velocity magnitude - m/s**.

#### *Streamline 1*

- 1 In the **Model Builder** window, click **Streamline 1**.
- 2 In the **Settings** window for **Streamline**, locate the **Inherit Style** section.
- 3 From the **Plot** list, choose **Slice**.
- 4 In the **Velocity (spf)** toolbar, click  **Plot**.

To get a better view, rotate the geometry in the **Graphics** window. You can preserve a view for a plot by creating a **View** feature node as follows:

- 5 Click the  **Show More Options** button in the **Model Builder** toolbar.
- 6 In the **Show More Options** dialog box, in the tree, select the check box for the node **Results>Views**.
- 7 Click **OK**.

#### *View 3D 3*

- 1 In the **Model Builder** window, under **Results** right-click **Views** and choose **View 3D**.

- 2 Use the **Graphics** toolbox to get a satisfying view.
- 3 In the **Settings** window for **View 3D**, locate the **View** section.
- 4 Select the **Lock camera** check box.

Next, apply the view to the velocity plot.

#### *Velocity (spf)*

- 1 In the **Model Builder** window, under **Results** click **Velocity (spf)**.
- 2 In the **Settings** window for **3D Plot Group**, locate the **Plot Settings** section.
- 3 From the **View** list, choose **View 3D 3**.
- 4 In the **Velocity (spf)** toolbar, click  **Plot**.

For a clearer visualization, you can duplicate this plot group and remove the geometry edges and the velocity slice, and add instead a temperature surface at the outside part.

#### *Velocity and Outside Temperature*

- 1 Right-click **Velocity (spf)** and choose **Duplicate**.
- 2 In the **Settings** window for **3D Plot Group**, type **Velocity and Outside Temperature** in the **Label** text field.
- 3 In the **Model Builder** window, expand the **Velocity and Outside Temperature** node.
- 4 Right-click **Velocity and Outside Temperature** and choose **Move Up**.
- 5 Right-click **Velocity and Outside Temperature** and choose **Move Up**.

#### *Slice*

- 1 In the **Model Builder** window, under **Results>Velocity and Outside Temperature** right-click **Slice** and choose **Delete**.
- 2 Click **Yes** to confirm.

#### *Surface 2*

- 1 In the **Results** toolbar, click  **More Datasets** and choose **Surface**.
- 2 Select Boundaries 55, 95, and 108 only.

#### *Velocity and Outside Temperature*

In the **Model Builder** window, under **Results** click **Velocity and Outside Temperature**.

#### *Surface 1*

- 1 In the **Velocity and Outside Temperature** toolbar, click  **Surface**.
- 2 In the **Settings** window for **Surface**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Surface 2**.

- 4 Locate the **Coloring and Style** section. From the **Color table** list, choose **Thermal**.

#### *Velocity and Outside Temperature*

- 1 In the **Model Builder** window, click **Velocity and Outside Temperature**.
- 2 In the **Settings** window for **3D Plot Group**, locate the **Color Legend** section.
- 3 From the **Position** list, choose **Right double**.
- 4 Locate the **Plot Settings** section. Clear the **Plot dataset edges** check box.
- 5 In the **Velocity and Outside Temperature** toolbar, click  **Plot**.

#### *Stress (solid)*

The last plot shows the von Mises stress and deformation distribution in the container. To reproduce the [Figure 5](#), apply the **View 3D 3**.

- 1 In the **Model Builder** window, click **Stress (solid)**.
- 2 In the **Settings** window for **3D Plot Group**, locate the **Plot Settings** section.
- 3 From the **View** list, choose **View 3D 3**.

#### *Volume I*

- 1 In the **Model Builder** window, expand the **Stress (solid)** node, then click **Volume I**.
- 2 In the **Settings** window for **Volume**, locate the **Expression** section.
- 3 From the **Unit** list, choose **GPa**.
- 4 In the **Stress (solid)** toolbar, click  **Plot**.