

Axisymmetric Condenser Microphone

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Introduction

This is a model of a condenser microphone with a simple axisymmetric geometry. The model aims to give a precise description of the physical working principles of such a microphone.

The condenser microphone is considered to be the microphone with highest quality when performing precise acoustical measurements and with high-fidelity reproduction properties when performing sound recordings; see Ref. 2. This electro-mechanical acoustic transducer works by transforming the mechanical deformation of a thin membrane (diaphragm) into an AC voltage signal.



Figure 1: Sketch of the condenser microphone system including variables and coordinate system. The red box indicates the modeled region.

Models for describing condenser microphones have classically been of the equivalent network type; see Ref. 2. Analytical models exist for simpler geometries, but there are also highly advanced analytical models for more complex geometries; see for example Ref. 1 or Ref. 4. In the present detailed finite-element model the thermoviscous acoustic, electric, and structural problem is solved fully coupled using the frequency-domain linear perturbation solver. This includes the DC charging (prepolarization) and deformation of the membrane which makes out the zeroth order linearization point. A small external circuit model is added to model the pre-amplifier. In some cases, lumping of the electrical part is a good approximation, especially for simple geometries such as this one, where the back electrode is flat and has no perforations. During the initial design steps, lumped

models are an important tool. In more complex geometries, solving the full set of equations is necessary to get the correct response.

THEORETICAL MEMBRANE MODEL

In order to compare the results of the simulation, the model uses the analytical solution derived for an undamped axisymmetric membrane. The displacement U of a thin axisymmetric membrane of thickness t_m , under constant tension T_m , and with a density ρ_m is governed by the following equation

$$T_{m}\frac{\partial}{\partial r}\left(r\frac{\partial U}{\partial r}\right) - \rho_{ms}r\frac{\partial^{2}U}{\partial t^{2}} - rF_{s} = 0$$
⁽¹⁾

where *r* is the radial coordinate, *t* is time, $\rho_{\rm ms} = \rho_{\rm m}/t_{\rm m}$ is the surface density, and F_s is the sum of surface forces; see for example Ref. 3. In the present model, the surface force is the sum of the external incident pressure $p_{\rm in}$ (it is assumed to be uniform over the microphone membrane), the internal pressure $p = p(\mathbf{r})$ (given by the thermoviscous acoustics model), and the electrostatic force which is the sum of the quiescent Maxwell surface stress $\mathbf{n} \cdot \tau$ (given by the electrostatic model) and the small-signal force $f_{\rm es}$. The variation of the deformation *U* is assumed to be small and harmonic on top of the static contribution U_0 from the DC polarization, such that

$$U(\mathbf{r}, t) = U_0(\mathbf{r}) + U(\mathbf{r})e^{i\omega t}$$

$$p_{in}(\mathbf{r}, t) = p_{in}e^{i\omega t}$$

$$p(\mathbf{r}, t) = p(\mathbf{r})e^{i\omega t}$$

$$F_{es}(\mathbf{r}, t) = \mathbf{n} \cdot \tau + f_{es}/(2\pi R_m^2) \cdot e^{i\omega t}$$
(2)

Using these expressions, Equation 1 is reformulated into a static and a time-harmonic equation as

$$T_{\rm m} \frac{\partial}{\partial r} \left(r \frac{\partial U_0}{\partial r} \right) - r(\mathbf{n} \cdot \tau) = 0$$

$$T_{\rm m} \frac{\partial}{\partial r} \left(r \frac{\partial U}{\partial r} \right) + \rho_{\rm ms} r \omega^2 U - r(f_{\rm es} / (2\pi R_{\rm mem}^2) + p_{\rm in} - p) = 0$$
(3)

The latter equation may be rewritten in terms of the axial velocity, $u_m = i\omega U$, of the membrane in the form of a Helmholtz equation:

$$T_{m}\frac{\partial}{\partial r}\left(r\frac{\partial u_{m}}{\partial r}\right) + T_{m}k_{m}^{2}ru_{m} - i\omega r(p_{in} - p) = 0$$

$$k_{m}^{2} = \frac{\omega^{2}\rho_{ms}}{T_{m}}$$
(4)

Here $k_{\rm m}$ is the membrane wave number. In this model you disregard the change in tension due to the movement of the membrane, which is a nonlinear effect that is small compared to the tension $T_{\rm m}$.

The current model represents a true multiphysics problem that involves several physics interfaces: Thermoviscous Acoustics, Electrostatics, Electrical Circuit, a Membrane model and the Moving Mesh feature.

Note: This application requires the AC/DC Module and the Structural Mechanics Module in addition to the Acoustics Module.

Model Definition

The geometry and model definitions are shown in Figure 1. In many microphones there is a back-volume below the electrode. In this model, a simplified approach is taken and a pressure release condition is applied with $p_0 = 0$ Pa. The membrane is deformed due to the electrostatic forces from charging the capacitor and because of the pressure variation from the external incoming uniform acoustic signal p_{in} . The chosen dimensions of the microphone are typical generic dimensions. Dimensions and parameters are given in Table 1.

SYMBOL	SIZE & UNIT	DESCRIPTION	
$H_{\rm m}$	18 μm	Air gap thickness	
$R_{\rm mem}$	2 mm	Membrane radius	
G	54 μm	Slit gap width	
$T_{\rm m0}$	3150 N/m	Membrane static tension	
E _m	221 GPa	Membrane elastic modulus	
t _m	7 μm	Membrane thickness	
ρ_{m}	8300 kg/m ³	Membrane density	
$V_{ m pol}$	100 V	Target polarization voltage	

TABLE I: MICROPHONE DIMENSIONS AND PARAMETERS.

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SYMBOL	SIZE & UNIT	DESCRIPTION
$R_{ m preamp}$	ΙGΩ	Pre-amplifier output impedance
v _m	0.4	Poisson's ratio for the membrane

The membrane is backed by a thin air gap of thickness $H_{\rm m}$ and a back electrode. Because the gap is so small, the inclusion of thermal and viscous losses in the acoustic model is essential, thus using the thermoviscous acoustics interface. The membrane and back electrode make up a capacitor that is polarized by an external DC voltage source through the pre-amplifier resistance R_{preamp}. This will give rise to a surface charge $Q_{\rm m}$. The air gap acts as a damping layer for the membrane vibrations. As the gap between the membrane and the back electrode varies, a voltage change is induced. This AC voltage is the output of the microphone.

The sensitivity of the condenser microphone L, is measured in the unit dB (relative to 1 V/Pa). It is defined as the ratio of the open circuit output voltage V_{out} to the input pressure p_{in} and is given by

$$L = 20\log\left[\left|\frac{V_{\text{out}}}{p_{\text{in}}}\right| / \left(1\frac{V}{Pa}\right)\right]$$
(5)

In the present model, the membrane (or diaphragm) is modeled using the dedicated Membrane interface from the Structural Mechanics Module. The membrane is subject to a surface load that is the sum of the external incident pressure p_{in} , the internal pressure $p = p(\mathbf{r})$ (given by the thermoviscous acoustics model), and the electrostatic force given by the Maxwell surface stress, $\mathbf{n} \cdot \tau$. The incident pressure is here assumed to be uniform over the microphone membrane, which is only an approximation. At the highest frequencies modeled, the acoustic wavelength becomes comparable with the membrane radius.

Results and Discussion

This model involves a detailed description of the physical effects in a simple condenser microphone. The sensitivity of the microphone L, is directly determined from the model (voltage on the terminal divided by the incident pressure) and is shown in Figure 2 below. Notice the slight roll-off at the low frequencies, this is due to the interaction with the pre-amplifier circuit. By increasing the output impedance R_{preamt} this effect will disappear, if the value is decreased the roll-off will be more significant.



Figure 2: Sensitivity curve of the microphone measured in dB relative to 1 V/Pa.

For the case of the simple geometry used in this model, an analytical solution exists for the dynamics of the undamped membrane; see Ref. 3. The axial displacement is given by

$$U_{\rm th}(r) = \frac{p_{\rm in}}{T_{\rm m}k_{\rm m}^2} \left(1 - \frac{J_0(k_{\rm m}r)}{J_0(k_{\rm m}R_{\rm mem})} \right)$$
(6)

where $k_{\rm m}$ is the wave number defined in Equation 4. The analytical approximation is compared to the model results in Figure 3, which shows the average deformation versus frequency. The results agree well below the resonance frequency of the system. The average behavior above the first resonance (in between resonances) is also well captured by the approximate theoretical model. In the real system, the damping introduced by the thermal and viscous losses in the air gap is important, especially at the resonances. This is also seen from the figure, where the resonance of the full (real) system is damped and shifted in frequency. The comparison of the two is used as an extra indicator for the correctness of the COMSOL model.

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Figure 3: Comparison of the average membrane deformation given by the COMSOL model and by the theoretical approximation for the undamped membrane.

The shape of the deformed membrane is plotted for f = 300 kHz as a 3D surface in Figure 4, using a revolution 2D dataset. At this frequency, it is clear to see how higher order modes in the membrane are the cause of the poor sensitivity.



Figure 4: 3D representation of the harmonic membrane deformation at 300 kHz.

The principles described in this model can be extended to 3D models with more complex geometries. Because the full set of equations is solved, such a model includes all physical effects to a high degree of detail. For example, as in The Brüel & Kjær 4134 Condenser Microphone. It can be used to optimize the performance of microphones, to make virtual tests of new geometries, or to investigate the relative importance of different parameters.

Notes About the COMSOL Implementation

COUPLED STATIC AND FREQUENCY-DOMAIN MODEL USING THE FREQUENCY DOMAIN, PRESTRESSED STUDY

The current model solves a fully coupled problem using the Frequency Domain, Prestressed study. A stationary study determines the linearization point and the full system of equations is then linearized and solved around this point to determine the harmonic small-signal response (the Frequency Domain Perturbation study step).

The first step is to determine the linearization point for the problem which requires solving a static model that determines the shape of the membrane after the polarization voltage

and the membrane tension are applied. The first step solves the electrostatic model (using the Electrostatics interface in the AC/DC Module) coupled to the membrane model. The acoustic model is automatically deactivated as it is, per construction, a small perturbation and thus has no contribution to the static solver step. To determine the correct capacitance (and electric fields) a Moving Mesh feature is needed. The capacitance is a geometry-dependent quantity.

The second step is to solve the linear perturbation frequency-domain model that describes the time-harmonic small-signal deformation of the membrane and the interaction with the fluid (described by a Thermoviscous Acoustics, Frequency Domain interface) within the microphone.

References

1. T. Lavergne, S. Durand, M. Bruneau, N. Joly, and D. Rodrigues, "Dynamic behavior of the circular membrane of an electrostatic microphone: Effect of holes in the backing electrode," *J. Acoust. Soc. Am.*, vol. 128, p. 3459, 2010.

2. W. Marshall Leach, Jr., *Introduction to Electroacoustics and Audio Amplifier Design*, 3rd ed., Kendall/Hunt Publishing Company, 2003.

3. P.M. Morse and K. Uno Ignard, *Theoretical Acoustics*, Princeton University Press, 1968.

4. V.C. Henriquez, *Numerical Transducer Modelling*, PhD Thesis, DTU, November 2001.

Application Library path: Acoustics_Module/Electroacoustic_Transducers/ condenser_microphone

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click 🙆 Model Wizard.

MODEL WIZARD

I In the Model Wizard window, click 🚈 2D Axisymmetric.

- 2 In the Select Physics tree, select AC/DC>Electric Fields and Currents>Electrostatics (es).
- 3 Click Add.

This is an appropriate choice because it is a good assumption that the electric processes in this model are quasistatic.

- 4 In the Select Physics tree, select AC/DC>Electrical Circuit (cir).
- 5 Click Add.
- 6 In the Select Physics tree, select Acoustics>Thermoviscous Acoustics> Thermoviscous Acoustics, Frequency Domain (ta).
- 7 Click Add.
- 8 In the Select Physics tree, select Structural Mechanics>Membrane (mbrn).
- 9 Click Add.
- **IO** In the **Displacement field** text field, type um.

II In the Displacement field components table, enter the following settings:

um	
vm	

wm

The displacement field of the membrane is (um,vm,wm) while the velocity field in the fluid is (u,v,w).

12 Click 🔿 Study.

13 In the Select Study tree, select Preset Studies for Selected Physics Interfaces>Membrane> Frequency Domain, Prestressed.

I4 Click M Done.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click 📂 Load from File.
- 4 Browse to the model's Application Libraries folder and double-click the file condenser_microphone_parameters.txt.

These are the parameters specifying the geometry and the physical properties of the microphone and membrane.

GEOMETRY I

- I In the Model Builder window, under Component I (compl) click Geometry I.
- 2 In the Settings window for Geometry, locate the Units section.
- 3 From the Length unit list, choose mm.

Rectangle 1 (r1)

- I In the Geometry toolbar, click 📃 Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type Rmem.
- 4 In the **Height** text field, type Hm.
- 5 Click 틤 Build Selected.

Rectangle 2 (r2)

- I In the **Geometry** toolbar, click **Rectangle**.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- **3** In the **Width** text field, type G.
- 4 In the **Height** text field, type Hm.
- 5 Locate the **Position** section. In the **r** text field, type Rmem-G.
- 6 Click 🟢 Build All Objects.

DEFINITIONS

Create a selection corresponding to the membrane for use when adding features to the membrane edge.

Membrane

- I In the Definitions toolbar, click 🐚 Explicit.
- 2 In the Settings window for Explicit, locate the Input Entities section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 Select Boundaries 3 and 6 only.
- 5 In the Label text field, type Membrane.

Load the variables that define the theoretical response of an undamped membrane.

Variables I

- I In the **Definitions** toolbar, click $\partial =$ **Local Variables**.
- 2 In the Settings window for Variables, locate the Variables section.
- 3 Click 📂 Load from File.

4 Browse to the model's Application Libraries folder and double-click the file condenser_microphone_variables.txt.

Integration 1 (intop1)

- I In the Definitions toolbar, click 🖉 Nonlocal Couplings and choose Integration.
- 2 In the Settings window for Integration, type intop_be in the Operator name text field.
- **3** Locate the **Source Selection** section. From the **Geometric entity level** list, choose **Boundary**.
- 4 Select Boundary 3 only.

ADD MATERIAL

- I In the Home toolbar, click 👬 Add Material to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Built-in>Air.
- 4 Click Add to Component in the window toolbar.
- 5 In the Home toolbar, click 🙀 Add Material to close the Add Material window.

Having set up the materials, proceed to setting up and defining the physics. Begin with the electric problem: Electrostatics and Circuit.

ELECTROSTATICS (ES)

Terminal I

- I In the Model Builder window, under Component I (compl) right-click Electrostatics (es) and choose the boundary condition Terminal.
- **2** Select Boundary 2 only.
- 3 In the Settings window for Terminal, locate the Terminal section.
- 4 From the Terminal type list, choose Circuit.

Ground I

- I In the Physics toolbar, click Boundaries and choose Ground.
- 2 In the Settings window for Ground, locate the Boundary Selection section.
- 3 From the Selection list, choose Membrane.

Finally, add the **Force Calculation** feature that will announce the electrostatic forces used in the Membrane physics.

Force Calculation 1

I In the Physics toolbar, click **Domains** and choose Force Calculation.

2 In the Settings window for Force Calculation, locate the Domain Selection section.

3 From the Selection list, choose All domains.

Now, set up the small external electrical circuit that is depicted in Figure 1.

ELECTRICAL CIRCUIT (CIR)

In the Model Builder window, under Component I (compl) click Electrical Circuit (cir).

External I vs. U I (IvsUI)

I In the Electrical Circuit toolbar, click - External I vs. U.

2 In the Settings window for External I vs. U, locate the Node Connections section.

3 In the table, enter the following settings:

Label	Node names	
Ρ	1	
n	0	

4 Locate the External Device section. From the V list, choose Terminal voltage (es/term1).

Resistor I (RI)

I In the Electrical Circuit toolbar, click ----- Resistor.

2 In the Settings window for Resistor, locate the Node Connections section.

3 In the table, enter the following settings:

Label	Node names
Р	1
n	2

4 Locate the **Device Parameters** section. In the *R* text field, type **Rpreamp**.

Voltage Source 1 (V1)

I In the Electrical Circuit toolbar, click 🔅 Voltage Source.

2 In the Settings window for Voltage Source, locate the Node Connections section.

3 In the table, enter the following settings:

Label	Node names	
Р	2	
n	0	

4 Locate the **Device Parameters** section. In the v_{src} text field, type Vpo1.

Next, set up the acoustics before turning to the membrane model and the Moving Mesh interface.

THERMOVISCOUS ACOUSTICS, FREQUENCY DOMAIN (TA)

In the Model Builder window, under Component I (compl) click Thermoviscous Acoustics, Frequency Domain (ta).

Pressure (Adiabatic) I

- I In the Physics toolbar, click Boundaries and choose Pressure (Adiabatic).
- 2 Select Boundary 5 only.
- 3 In the Settings window for Pressure (Adiabatic), locate the Pressure section.
- **4** In the p_{bnd} text field, type p0.

MULTIPHYSICS

Thermoviscous Acoustic-Structure Boundary 1 (tsb1)

- I In the Physics toolbar, click An Multiphysics Couplings and choose Boundary> Thermoviscous Acoustic-Structure Boundary.
- 2 In the Settings window for Thermoviscous Acoustic-Structure Boundary, locate the Boundary Selection section.
- 3 From the Selection list, choose Membrane.

The last step couples the membrane to the thermoviscous acoustic domain. The multiphysics coupling feature sets the acoustic velocity equal to $i\omega$ times the deformation of the membrane (this is the time derivative in the frequency domain). This condition is a bidirectional constraint, meaning that a reaction force is added to the membrane equation, ensuring a bidirectional coupling.

Now, set up the membrane model, constrain it at the outer perimeter where it is fixed and add the forces that act on it. They are the electrostatic forces given by the Maxwell stress tensor and the incident pressure field pin. Use the linper() operator to tell COMSOL that the incident pressure is only a harmonic frequency-dependent quantity (not a static load).

MEMBRANE (MBRN)

- I In the Model Builder window, under Component I (compl) click Membrane (mbrn).
- 2 In the Settings window for Membrane, locate the Boundary Selection section.
- 3 From the Selection list, choose Membrane.

Thickness and Offset I

- I In the Model Builder window, under Component I (compl)>Membrane (mbrn) click Thickness and Offset I.
- 2 In the Settings window for Thickness and Offset, locate the Thickness and Offset section.
- **3** In the *d* text field, type tm.

Linear Elastic Material I

- I In the Model Builder window, click Linear Elastic Material I.
- **2** In the **Settings** window for **Linear Elastic Material**, locate the **Linear Elastic Material** section.
- 3 From the E list, choose User defined. In the associated text field, type Em.
- 4 From the v list, choose User defined. In the associated text field, type num.
- **5** From the ρ list, choose **User defined**. In the associated text field, type rhom.

Initial Stress and Strain 1

- I In the Physics toolbar, click Attributes and choose Initial Stress and Strain.
- **2** In the **Settings** window for **Initial Stress and Strain**, locate the **Initial Stress and Strain** section.
- **3** In the N_0 table, enter the following settings:

TmO O 0 TmO

Fixed Constraint I

- I In the Physics toolbar, click 💭 Points and choose Fixed Constraint.
- **2** Select Point 6 only.

Face Load I

- I In the Physics toolbar, click Boundaries and choose Face Load.
- 2 In the Settings window for Face Load, locate the Boundary Selection section.
- 3 From the Selection list, choose Membrane.
- 4 Locate the Force section. From the \mathbf{F}_A list, choose Maxwell surface stress tensor (es/ fcall).

Face Load 2

- I In the Physics toolbar, click Boundaries and choose Face Load.
- 2 In the Settings window for Face Load, locate the Boundary Selection section.

- 3 From the Selection list, choose Membrane.
- 4 Locate the Force section. From the Load type list, choose Pressure.
- **5** In the *p* text field, type linper(pin).

COMPONENT I (COMPI)

Deforming Domain I

- I In the Definitions toolbar, click Moving Mesh and choose Domains> Deforming Domain.
- 2 In the Settings window for Deforming Domain, locate the Domain Selection section.
- 3 From the Selection list, choose All domains.

Fixed Boundary I

- I In the Definitions toolbar, click Moving Mesh and choose Boundaries> Fixed Boundary.
- 2 Select Boundaries 2, 5, and 7 only.

Symmetry/Roller 1

- I In the Definitions toolbar, click Moving Mesh and choose Boundaries>Symmetry/ Roller.
- 2 Select Boundary 1 only.

The above **Moving Mesh** feature ensures that the computational mesh deforms according to the membrane deformation (um,wm). The deformation of the (adjacent) membrane is automatically used as the mesh movement on the boundary.

MESH I

Mapped I

- I In the Mesh toolbar, click Mapped.
- 2 In the Settings window for Mapped, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 Click in the Graphics window and then press Ctrl+A to select both domains.
- **5** Click to expand the **Reduce Element Skewness** section. Select the **Adjust edge mesh** check box.

Distribution I

- I Right-click Mapped I and choose Distribution.
- 2 Select Boundary 3 only.

- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 30.

Distribution 2

- I In the Model Builder window, right-click Mapped I and choose Distribution.
- 2 Select Boundary 4 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- **4** From the **Distribution type** list, choose **Predefined**.
- **5** In the **Number of elements** text field, type **10**.
- 6 In the Element ratio text field, type 2.
- 7 Select the Symmetric distribution check box.

Distribution 3

- I Right-click Mapped I and choose Distribution.
- **2** Select Boundary 6 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 4.

Boundary Layers 1

- I In the Mesh toolbar, click Boundary Layers.
- 2 In the Settings window for Boundary Layers, click to expand the Transition section.
- **3** Clear the **Smooth transition to interior mesh** check box.

Boundary Layer Properties

- I In the Model Builder window, click Boundary Layer Properties.
- **2** Select Boundary 4 only.
- 3 In the Settings window for Boundary Layer Properties, locate the Layers section.
- 4 In the Number of layers text field, type 5.
- **5** From the **Thickness specification** list, choose **First layer**.
- 6 In the Thickness text field, type 2[um].
- 7 Click 🔚 Build Selected.

The mesh is built such that it resolves the acoustic boundary layer at the maximal frequency of 300 kHz. At this frequency the viscous boundary layer is about 4 μ m thick, corresponding to roughly 1/5 of the air-gap thickness.

STUDY I

- I In the Model Builder window, click Study I.
- 2 In the Settings window for Study, locate the Study Settings section.
- **3** Clear the **Generate default plots** check box.

Step 1: Stationary

Notice that the Include geometric nonlinearity check box is selected but unavailable, as it is needed for the prestress study to work.

Notice the small orange warning sign next to Thermoviscous Acoustics and the Multiphysics coupling indicating that these are not solved in the stationary study step (as expected).

Step 2: Frequency Domain Perturbation

- I In the Model Builder window, click Step 2: Frequency Domain Perturbation.
- **2** In the **Settings** window for **Frequency Domain Perturbation**, locate the **Study Settings** section.
- 3 From the Frequency unit list, choose kHz.
- 4 In the Frequencies text field, type {0.1 range(2.5,2.5,300)}.

This gives a frequency range of 100 Hz - 300 kHz. The reason for including such high frequencies is to be able to observe the fall-off in sensitivity.

5 In the **Home** toolbar, click **= Compute**.

RESULTS

Global Evaluation 1

- I In the Model Builder window, expand the Results node.
- 2 Right-click Results>Derived Values and choose Global Evaluation.
- 3 In the Settings window for Global Evaluation, locate the Data section.
- 4 From the Parameter selection (freq) list, choose First.
- **5** Locate the **Expressions** section. In the table, enter the following settings:

Expression	Unit	Description
es.V0_1	V	Terminal voltage
es.Q0_1	C	Terminal charge

- 6 From the Expression evaluated for list, choose Static solution.
- 7 Click **=** Evaluate.

TABLE

I Go to the Table window.

The static polarization voltage across the membrane should equal 100.0 V (as defined). The resulting static membrane charge is 5.9e-10 C.

RESULTS

Velocity

- I In the **Results** toolbar, click **2D Plot Group**.
- 2 In the Settings window for 2D Plot Group, type Velocity in the Label text field.

Surface 1

- I Right-click Velocity and choose Surface.
- 2 In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>
 Thermoviscous Acoustics, Frequency Domain>Acceleration and velocity>ta.v_inst Instantaneous total acoustic velocity m/s.
- **3** In the **Velocity** toolbar, click **I** Plot.

To get a better view of the long slender geometry, disable the Preserve aspect ratio option.

DEFINITIONS

Axis

- I In the Model Builder window, expand the View I node, then click Axis.
- 2 In the Settings window for Axis, locate the Axis section.
- 3 From the View scale list, choose Automatic.
- 4 Click 🚺 Update.
- **5** Click the **Comextents** button in the **Graphics** toolbar.

RESULTS

Velocity

The plot should look like this.



In the same way you can also plot the acoustic pressure (replacing ta.v_inst with ta.p_t) or acoustic temperature variations (replacing ta.v_inst with ta.T_t).

Potential

- I In the Home toolbar, click 🚛 Add Plot Group and choose 2D Plot Group.
- 2 In the Settings window for 2D Plot Group, type Potential in the Label text field.

Surface 1

Right-click Potential and choose Surface.

Potential

I In the **Potential** toolbar, click **I** Plot.

The plot should look like this.



Sensitivity

- I In the Home toolbar, click 🚛 Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Sensitivity in the Label text field.
- 3 Click to expand the Title section. From the Title type list, choose Label.
- 4 Locate the Plot Settings section.
- 5 Select the y-axis label check box. In the associated text field, type Sensitivity (dB rel. 1 V/Pa).
- 6 Locate the Legend section. From the Position list, choose Lower left.

Octave Band I

- I In the Sensitivity toolbar, click \sim More Plots and choose Octave Band.
- 2 In the Settings window for Octave Band, locate the Selection section.
- **3** From the **Geometric entity level** list, choose **Global**.
- 4 Locate the y-Axis Data section. In the Expression text field, type es.VO_1.

5 In the Amplitude reference text field, type pin/sqrt(2).

Notice that the amplitude reference is an RMS value.

- 6 Locate the Plot section. From the Quantity list, choose Continuous power spectral density.
- 7 In the **Sensitivity** toolbar, click **I** Plot.

The microphone sensitivity curve should look like Figure 2.

Now, plot the membrane deformation in a 1D plot, both the static and the harmonic components, as function of the radial coordinate.

Membrane Deformation

- I In the Home toolbar, click 🚛 Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Membrane Deformation in the Label text field.
- 3 Locate the Title section. From the Title type list, choose Label.

Line Graph I

- I Right-click Membrane Deformation and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the Selection section.
- 3 From the Selection list, choose Membrane.
- 4 Locate the y-Axis Data section. In the Expression text field, type wm.
- 5 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- 6 In the Expression text field, type r.

7 In the Membrane Deformation toolbar, click 💿 Plot.

The plot should look like this.



Static Membrane Deformation

- I In the Model Builder window, right-click Membrane Deformation and choose Duplicate.
- 2 In the Settings window for ID Plot Group, type Static Membrane Deformation in the Label text field.
- 3 Locate the Data section. From the Parameter selection (freq) list, choose Last.

Line Graph 1

- I In the Model Builder window, expand the Static Membrane Deformation node, then click Line Graph I.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- 3 From the Expression evaluated for list, choose Static solution.

4 In the **Static Membrane Deformation** toolbar, click **O Plot**.

The plot should look like this.



Average Membrane Velocity

- I In the Home toolbar, click 🚛 Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Average Membrane Velocity in the Label text field.
- 3 Locate the Title section. From the Title type list, choose Label.
- 4 Locate the Plot Settings section.
- 5 Select the y-axis label check box. In the associated text field, type log₁₀ (|um_{av}| (m/s)).
- 6 Locate the Legend section. From the Position list, choose Upper left.

Global I

- I Right-click Average Membrane Velocity and choose Global.
- 2 In the Settings window for Global, locate the y-Axis Data section.

3 In the table, enter the following settings:

Expression	Unit	Description
log10(abs(um_av))		Model
log10(abs(uth_av))		Analytical approximation

- **4** In the Average Membrane Velocity toolbar, click **I** Plot.
- **5** Click the **x-Axis Log Scale** button in the **Graphics** toolbar.

The plot should look like this.



Average Membrane Deformation

- I In the Home toolbar, click 🚛 Add Plot Group and choose ID Plot Group.
- 2 In the **Settings** window for **ID Plot Group**, type Average Membrane Deformation in the **Label** text field.
- 3 Locate the Title section. From the Title type list, choose Label.
- 4 Locate the Plot Settings section.
- 5 Select the y-axis label check box. In the associated text field, type log₁₀ (|U_{av}| (m)).
- 6 Locate the Legend section. From the Position list, choose Upper left.

Global I

- I Right-click Average Membrane Deformation and choose Global.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
log10(abs(U_av))		Model
log10(abs(Uth_av))		Analytical approximation

4 In the Average Membrane Deformation toolbar, click **I** Plot.

5 Click the **x-Axis Log Scale** button in the **Graphics** toolbar.

The microphone sensitivity curve should look like Figure 3.

Finally, plot the membrane deformation on a 3D revolved geometry using a 2D revolution dataset, to reproduce Figure 4.

Revolution 2D 1

In the **Results** toolbar, click **More Datasets** and choose **Revolution 2D**.

3D Membrane Deformation

- I In the **Results** toolbar, click 间 **3D Plot Group**.
- 2 In the Settings window for 3D Plot Group, type 3D Membrane Deformation in the Label text field.

Surface 1

- I Right-click 3D Membrane Deformation and choose Surface.
- In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>Membrane> Displacement>mbrn.disp Displacement magnitude m.

Deformation I

- I Right-click Surface I and choose Deformation.
- 2 In the Settings window for Deformation, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)> Membrane>Displacement>um,vm,wm Displacement field.
- **3** In the **3D Membrane Deformation** toolbar, click **O** Plot.

The 3D plot should look like Figure 4.