

Photonic Crystal

Photonic crystal devices are periodic structures of alternating layers of materials with different refractive indices. Waveguides that are confined inside of a photonic crystal can have very sharp low-loss bends, which may enable an increase in integration density of several orders of magnitude.

Introduction

This application describes the wave propagation in a photonic crystal that consists of GaAs pillars placed equidistant from each other. The distance between the pillars prevents light of certain wavelengths to propagate into the crystal structure. Depending on the distance between the pillars, waves within a specific frequency range are reflected instead of propagating through the crystal. This frequency range is called the photonic band gap (Ref. 1). By removing some of the GaAs pillars in the crystal structure you can create a guide for the frequencies within the band gap. Light can then propagate along the outlined guide geometry.



The geometry is a square of air with an array of circular pillars of GaAs as described above. Some pillars are removed to make a waveguide with a 90° bend.

The objective of the application is to study TE waves propagating through the crystal. To model these, use a scalar equation for the transverse electric field component E_z ,

$$-\nabla \cdot \nabla E_z - n^2 k_0^2 E_z = 0$$

where n is the refractive index and k_0 is the free-space wave number.

Because there are no physical boundaries, you can use the scattering boundary condition at all boundaries. Set the amplitude E_z to 1 on the boundary of the incoming wave.

Results and Discussion

Figure 1 contains a plot of the *z* component of the electric field. It clearly shows the propagation of the wave through the guide.



Figure 1: The z component of the electric field showing how the wave propagates along the path defined by the pillars.

If the angular frequency of the incoming wave is less than the cutoff frequency of the waveguide, the wave does not propagate through the outlined guide geometry. In Figure 2 the wavelength has been increased by a factor of 1.3.



Figure 2: A longer wavelength does not propagate through the guide. This plot shows the norm of the electric field.

References

1. J.D. Joannopoulus, R.D. Meade, and J.N. Winn, *Photonic Crystals (Modeling the Flow of Light)*, Princeton University Press, 1995.

Application Library path: Wave_Optics_Module/Waveguides_and_Couplers/photonic_crystal

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click <u>Model Wizard</u>.

MODEL WIZARD

- I In the Model Wizard window, click 🧐 2D.
- 2 In the Select Physics tree, select Optics>Wave Optics>Electromagnetic Waves, Frequency Domain (ewfd).
- 3 Click Add.
- 4 Click \bigcirc Study.
- 5 In the Select Study tree, select Preset Studies for Selected Physics Interfaces> Wavelength Domain.
- 6 Click **M** Done.

GEOMETRY I

Import I (impl)

- I In the Home toolbar, click 📑 Import.
- 2 In the Settings window for Import, locate the Import section.
- 3 Click Browse.
- **4** Browse to the model's Application Libraries folder and double-click the file photonic_crystal.mphbin.
- 5 Click Import.
- 6 Click the **Zoom Extents** button in the **Graphics** toolbar.

MATERIALS

The refractive index of GaAs depends on the frequency. The material is added from the Optical Material Database.

ADD MATERIAL

- I In the Home toolbar, click 🙀 Add Material to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Optical>Inorganic Materials>As Arsenides>Experimental data> GaAs (Gallium arsenide) (Skauli et al. 2003: n 0.97-17 μm).
- 4 Click Add to Component in the window toolbar.
- 5 In the Home toolbar, click 🙀 Add Material to close the Add Material window.

MATERIALS

GaAs (Gallium arsenide) (Skauli et al. 2003: n 0.97-17 µm) (mat1)

Select Domains 1 and 3–86 only. This is most easily done by removing Domain 2 from the list once you have selected all domains.

Air

- I In the Model Builder window, right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type Air in the Label text field.
- **3** Select Domain 2 only.
- 4 Locate the Material Contents section. In the table, enter the following settings:

| Property | Variable | Value | Unit | Property group |
|------------------------|----------------------|-------|------|------------------|
| Refractive index, real | n_iso ; nii = n_iso, | 1 | I | Refractive index |
| part | nij = 0 | | | |

ELECTROMAGNETIC WAVES, FREQUENCY DOMAIN (EWFD)

Scattering Boundary Condition I

- I In the Model Builder window, under Component I (compl) right-click Electromagnetic Waves, Frequency Domain (ewfd) and choose Scattering Boundary Condition.
- **2** In the Settings window for Scattering Boundary Condition, locate the Boundary Selection section.
- 3 From the Selection list, choose All boundaries.

Scattering Boundary Condition 2

- I In the Physics toolbar, click Boundaries and choose Scattering Boundary Condition.
- 2 Select Boundary 5 only.
- **3** In the Settings window for Scattering Boundary Condition, locate the Scattering Boundary Condition section.
- 4 From the Incident field list, choose Wave given by E field.
- **5** Specify the \mathbf{E}_0 vector as

| 0 | x |
|---|---|
| 0 | v |

- 0 y
- 1 z

STUDY I

Step 1: Wavelength Domain

- I In the Model Builder window, under Study I click Step I: Wavelength Domain.
- 2 In the Settings window for Wavelength Domain, locate the Study Settings section.
- 3 In the Wavelengths text field, type 1[um] 1.3[um].

This will get you one solution for a free space wavelength of 1 μ m, and one for a free space wavelength of 1.3 μ m.

4 In the **Home** toolbar, click **= Compute**.

RESULTS

Electric Field (ewfd)

The default plot shows the distribution of the electric field norm for the lowest of the frequencies. Because this is below the cutoff frequency of the waveguide, the wave does not propagate through the outlined guide geometry.

- I In the Settings window for 2D Plot Group, locate the Data section.
- 2 From the Parameter value (lambda0 (µm)) list, choose I.
- 3 In the Electric Field (ewfd) toolbar, click 🗿 Plot.

300 THz, or a free space wavelength of 1 μ m, is within the band gap. The wave propagates all the way through the geometry, losing only a little of its energy. Try visualizing the instantaneous value of the field.

Surface 1

- I In the Model Builder window, expand the Electric Field (ewfd) node, then click Surface I.
- In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>
 Electromagnetic Waves, Frequency Domain>Electric>Electric field V/m>ewfd.Ez Electric field, z component.
- 3 Locate the Coloring and Style section. From the Color table list, choose WaveLight.

The WaveLight color table looks better if the range is symmetric around zero.

- 4 Select the Symmetrize color range check box.
- 5 In the Electric Field (ewfd) toolbar, click 🗿 Plot.

Cut Line 2D I

Finally, create a line plot comparing how the electric field magnitude falls off as the waves of the two frequencies under study enter the waveguide.

- I In the **Results** toolbar, click \frown **Cut Line 2D**.
- 2 In the Settings window for Cut Line 2D, locate the Line Data section.
- **3** In row **Point I**, set **Y** to **0.75e-6**.
- 4 In row Point 2, set X to 2.5e-6 and y to 0.75e-6.
- 5 Click 💽 Plot.

ID Plot Group 2

- I In the Results toolbar, click \sim ID Plot Group.
- 2 In the Settings window for ID Plot Group, locate the Data section.
- 3 From the Dataset list, choose Cut Line 2D I.

Line Graph I

- I Right-click ID Plot Group 2 and choose Line Graph.
- 2 In the ID Plot Group 2 toolbar, click 🗿 Plot.