

Biot Poroelasticity

Introduction

Poroelastic models describe the linked interaction between fluids and deformation in porous media. The fluids in a reservoir absorb stress, which registers as fluid pressure or equally hydraulic head. For example, if pumping significantly reduces pore fluid pressures, sediments could shift due to the increased load. Because the reduction in the pore space brings about more fluid movement, the reservoir could compact further. It follows that lateral stretching must compensate for the vertical compaction.

Model Definition

This example analyzes fluid and solid behavior within three sedimentary layers overlying an impermeable bedrock in a basin. The bedrock is faulted, which creates a step near a mountain front. The sediment stack totals 420 m at the centerline of the basin (x = 0 m) and thins to 120 m above the step (x > 4000 m). The top two layers are each 20 m thick.



Figure 1: Model geometry showing boundary segments (from Leake and Hsieh, Ref. 1).

Pumping from the lower aquifer reduces hydraulic head down the centerline of the basin by 6 m per year. The head drop moves fluid away from the step. The middle layer is relatively impermeable. The pumping does not diminish the supply of fluids in the unpumped reservoir above it. The flow field is initially at steady state. The period of interest is 10 years.

Governing Equations

This example uses the Poroelasticity multiphysics node, which includes the time rate of change in strain from the Solid Mechanics interface in the Darcy's Law interface and adds the fluid pressure gradient as stress contribution in the Solid Mechanics interface. The following sections describe the built-in equations when using the Poroelastic Material feature as well as the initial and boundary conditions.

FLUID FLOW

Use the Darcy's Law interface to estimate the flow field in the poroelastic model with the pressure head formulation

$$\rho_{\rm f} S_{\alpha} \frac{\partial H}{\partial t} + \nabla \cdot \rho_{\rm f} [-K \nabla H] = -\rho_{\rm f} \alpha_{\rm B} \frac{\partial}{\partial t} \varepsilon_{\rm vol} \tag{1}$$

where ρ_f is the fluid density, H is the pressure head (m), K is the hydraulic conductivity (m/s), ε_{vol} is the volumetric strain of the porous matrix, and α_B is the Biot-Willis coefficient; in this model the Biot-Willis coefficient equals 1, which is a common value for "soft soils." You can interpret the term on the right-hand side as the time rate of expansion of the porous matrix. The volume fraction available for liquid increases and thereby gives rise to liquid sink, which is why the sign is reversed in the source term. Leake and Hsieh (Ref. 1) defined S_{α} using coefficients from the solids equation, the Young's modulus, E, and Poisson's ratio, v. Debate over poroelastic storage coefficients is heated (Ref. 2), and the subscript α here denotes that conventional storage terms might need redefinition for poroelasticity models.

The main differences between the Terzaghi compaction model and this poroelastic analysis lie in material coefficients and sources; the boundary conditions are identical: H is the offset in hydraulic head since an initial steady-state distribution of H_0 . This subtle twist simplifies describing the boundary conditions: the value at the outlet boundary becomes the decline in hydraulic head with time, and at the upper aquifer, the hydraulic head is fixed at H_0 . All other boundaries have no-flow conditions. The boundary and initial conditions for the Darcy's law analysis are

$\mathbf{n} \cdot K \nabla H = 0$	$\partial \Omega$ base	A
$\mathbf{n} \cdot K \nabla H = 0$	$\partial \Omega$ other	B
$H = H_0$	$\partial \Omega$ upper edge	e C
$H = H_0$	$\partial \Omega$ surface	D
H = H(t)	$\partial \Omega$ outlet	E

where **n** is the normal to the boundary. The letters A through E come from Leake and Hsieh (Ref. 1), each letter denoting a specific boundary (see Figure 1).

POROUS MATRIX DEFORMATION

The governing equation for the poroelastic material model is

$$-\nabla \cdot \boldsymbol{\sigma} = \rho \boldsymbol{g} \tag{2}$$

here, σ is the stress tensor, ρ is the total density, and **g** is acceleration of gravity. The poroelastic material model uses Equation 2 to describe changes in the stress tensor σ and porous matrix displacement **u** due to boundary conditions and changes in pore pressure. This focus on changes in displacement is standard poroelasticity and greatly simplifies specifying loads, boundaries, and initial conditions. Equation 2 defines a state of static equilibrium because the changes in the solid equilibrate quickly, unlike vibrations or waves, that is, there are no time-dependent terms. Still the time rate of change in strain $\partial \varepsilon_{vol}/\partial t$ appears as a coupling term in Darcy's Law because the solids equation becomes quasi-static when solved simultaneously with a time-dependent flow model.

The governing equation for the bedrock step problem describes the deformation state of plane strain, which is the norm for 2D poroelasticity problems (Ref. 1 and Ref. 2), so the strain normal to the *xy*-plane equals zero. COMSOL Multiphysics solves Equation 2 using the Solid Mechanics interface.

For an isotropic porous material under plane strain conditions, this simplifies to

$$\begin{bmatrix} \sigma_{xx} \\ \sigma_{yy} \\ \sigma_{xy} \end{bmatrix} = \frac{E}{(1+\nu)(1-2\nu)} \begin{bmatrix} 1-\nu & \nu & 0 \\ \nu & 1-\nu & 0 \\ 0 & 0 & 1-2\nu \end{bmatrix} \begin{bmatrix} \varepsilon_{xx} \\ \varepsilon_{yy} \\ \varepsilon_{xy} \end{bmatrix} - \begin{bmatrix} \alpha_{B}p & 0 & 0 \\ 0 & \alpha_{B}p & 0 \\ 0 & 0 & \alpha_{B}p \end{bmatrix}$$
(3)

where *E* is Young's modulus (Pa) and v is Poisson's ratio of the drained porous matrix. The term $\alpha_{\rm B} p$ (Pa) amounts to the fluid pressure contribution and is often described as the fluid-to-structure coupling expression. This contribution is added by the Poroelasticity multiphysics node.

With small deformations for plane strain analyses, the normal strains ε_{xx} , ε_{yy} , ε_{zz} and shear strains ε_{xy} , ε_{yz} , ε_{xz} relate to the displacements u and v as

$$\varepsilon_{xx} = \frac{\partial u}{\partial x} \qquad \varepsilon_{yy} = \frac{\partial v}{\partial y} \qquad \varepsilon_{xy} = \frac{1}{2} \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) \qquad \varepsilon_{xy} = \varepsilon_{yx} \qquad \varepsilon_{xz} = \varepsilon_{yz} = \varepsilon_{yz} = 0 \quad (4)$$

4 | BIOT POROELASTICITY

Inserting the relationships from Equation 3 and Equation 4 into Equation 2 gives the equation that COMSOL Multiphysics solves.

The boundary conditions on the porous matrix are a series of constraints on the displacement that allow for horizontal movement at the surface and throughout the basin. The base of the sediments is fixed, which means you constrain horizontal and vertical displacement to zero. The upper surface is free to vary in the horizontal and the vertical directions. The boundary on left of Figure 1 is a roller condition, so the sediments are free to move in the vertical direction, but there is no horizontal displacement. These conditions result in the following boundary expressions

fixed constraint	$\partial \Omega$ base	A
free	$\partial \Omega$ other	B
free	$\partial \Omega$ upper edg	e C
free	$\partial \Omega$ surface	D
roller	$\partial \Omega$ outlet	E

where, once again, the letters A through E come from Leake and Hsieh, and denote the boundaries in Figure 1.

Model Data

The coefficients and parameters for the poroelasticity model are as follows:

VARIABLE	DESCRIPTION	VALUE
g	Gravity	9.82 m/s ²
ρ_{f}	Fluid density	1000 kg/m ³
ρ_d	Drained density of porous layer	2750 kg/m ³
S_{lpha}	Poroelastic storage coefficient, aquifer layers	I · 10 ⁻⁶ m ⁻¹
S_{lpha}	Poroelastic storage coefficient, confining layer	I · 10 ⁻⁵ m ⁻¹
Κ	Hydraulic conductivity, aquifer layers	25 m/day
K	Hydraulic conductivity, confining layer	0.01 m/day
$\alpha_{\rm B}$	Biot-Willis coefficient	I
H_0	Initial hydraulic head	0 m
H(t)	Declining head boundary	(6 m/year)∙t
Ε	Drained Young's modulus, aquifer layers	8·10 ⁸ Pa
Ε	Drained Young's modulus, confining layer	8·10 ⁷ Pa
ν	Drained Poisson's ratio, all regions	0.25

Results and Discussion

Figure 2, Figure 3, and Figure 4 are Year 2, Year 5, and Year 10 snapshots, respectively, from the COMSOL Multiphysics solution to the problem (Ref. 1) of linked fluid flow and solid deformation near a bedrock step in a sedimentary basin. The shading and arrows, respectively, represent the change in hydraulic head and velocities brought about by pumping from the basin interior at x = 0 m. The fluid moves from the surface toward the well screens in the lower aquifer, with an abrupt change in direction and velocity near the bedrock step. In this way, the flow solution here is similar to the results in Terzaghi compaction model.

The results for the solids displacement tell another story. In Figure 2, Figure 3, and Figure 4, contours and deformed shapes illustrate the total displacement. The plot sequence illustrates the evolution of lateral deformations that compensate for the changing surface elevation above the bedrock step.



Figure 2: Solution for a poroelasticity analysis of the bedrock step problem of Leake and Hsieh (Ref. 1): Hydraulic head (surface plot), displacement (contours and deformations) at Year 2. The arrows indicate the hydraulic head gradient. The vertical axis is expanded for clarity.



Figure 3: Hydraulic head (surface plot), displacement (contours and deformations), and hydraulic head gradient (arrows) at Year 5. The vertical axis and deformation are exaggerated for clarity.



Figure 4: Hydraulic head (surface plot), displacement (contours and deformations), and hydraulic head gradient (arrows) at Year 10. The vertical axis and deformation are exaggerated for clarity.

Figure 5, represents the coupling terms that link the fluid and structure equations. The shading gives the structure-to-fluid link, which is the negative of the time rate of change in strain (see Equation 1).



Figure 5: The solid-to-fluid coupling term evaluated at Year 10 with the poroelastic analysis. The squeeze of porous matrix results in an apparent mass source term.

The Terzaghi and Biot solutions differ most when it comes to predicting the horizontal strain at the edge of the bedrock step. The Biot poroelasticity analysis predicts horizontal strain; the Terzaghi compaction analysis does not. The horizontal strains at the ground surface from the Biot poroelasticity approach appear in Figure 6. It depicts negative strain or compaction immediately on the basin side of the step; the positive strains correspond to tension or lengthening on the mountain side.



Figure 6: COMSOL Multiphysics estimates of horizontal strain from poroelastic analysis for the bedrock step problem of Leake and Hsieh: Year 2 (blue line), Year 5 (green line), and Year 10 (red line).

Failure criteria or expressions defining a critical threshold for stress, strain, or displacements facilitate evaluating whether the strain differential at the bedrock steps is big enough to produce fissures. Figure 7 plots von Mises stresses (surface plot), fluid velocities (streamlines), and total displacement (deformation). The von Mises stresses are postprocessing variables defined by COMSOL Multiphysics in all structural-deformation analyses. The von Mises stresses are variables in many failure expressions and you can also use them as yield functions in the elasto-plastic materials dialog boxes.



Figure 7: COMSOL Multiphysics estimates of von Mises stresses (surface plot), fluid velocities (streamlines), and displacement (deformation) at Year 10. These results correspond to the poroelastic analysis from Leake and Hsieh (Ref. 1). The vertical axis and deformation are exaggerated for clarity.

Notes About the COMSOL Implementation

During the simulation an equilibrium between the gravity forces and the poroelastic forces is reached after about 0.2 years. After that, the simulation results change further only due to the changing hydraulic head at the left-hand side boundary. To reproduce this behavior correctly, it is important to start with a small time step in the beginning to reproduce the development of an equilibrium state correctly, whereas later on, a bigger time step is sufficient and should be chosen to save computational time.

References

1. S.A. Leake and P.A. Hsieh, Simulation of Deformation of Sediments from Decline of Ground-Water Levels in an Aquifer Underlain by a Bedrock Step, U.S. Geological Survey Open File Report 97-47, 1997.

2. H.F. Wang, *Theory of Linear Poroelasticity with Application to Geomechanics and Hydrogeology*, Princeton Univ. Press, 2000.

Application Library path: Subsurface_Flow_Module/ Flow_and_Solid_Deformation/biot_poroelasticity

Modeling Instructions

ROOT

Start by opening the model containing the solution for the compaction according to Terzaghi theory and use it as entry point for a two-way coupled poroelasticity study according to Biot's theory.

- I From the File menu, choose Open.
- 2 Browse to the model's Application Libraries folder and double-click the file terzaghi_compaction.mph.

RESULTS

Contour I

Add a Solid Mechanics interface and a Poroelasticity multiphysics node.

ADD PHYSICS

- I In the Home toolbar, click 🙀 Add Physics to open the Add Physics window.
- 2 Go to the Add Physics window.
- 3 In the tree, select Structural Mechanics>Solid Mechanics (solid).
- 4 Click Add to Component I in the window toolbar.
- 5 In the Home toolbar, click 🙀 Add Physics to close the Add Physics window.

ADD MULTIPHYSICS

- I In the Home toolbar, click 🙀 Add Multiphysics to open the Add Multiphysics window.
- 2 Go to the Add Multiphysics window.
- 3 In the tree, select Structural Mechanics>Poroelasticity>Poroelasticity, Solid.
- 4 Click Add to Component in the window toolbar.
- 5 In the Home toolbar, click 🙀 Add Multiphysics to close the Add Multiphysics window.

MULTIPHYSICS

Poroelasticity I (porol)

The insertion of the multiphysics node automatically inserts a poroelastic storage material model in Darcy's Law and sets the **Discretization** to linear.

DARCY'S LAW (DL)

Poroelastic Storage 1

- I In the Model Builder window, expand the Darcy's Law (dl) node, then click Poroelastic Storage I.
- 2 In the Settings window for Poroelastic Storage, locate the Fluid Properties section.
- 3 From the Fluid material list, choose Fluid (matl).
- 4 Locate the Matrix Properties section. From the Permeability model list, choose Hydraulic conductivity.
- **5** In the *K* text field, type K_s.

SOLID MECHANICS (SOLID)

In the Model Builder window, expand the Component I (comp1)>Materials node, then click Component I (comp1)>Solid Mechanics (solid).

Gravity I

- I In the Physics toolbar, click **Domains** and choose **Gravity**.
- 2 In the Settings window for Gravity, locate the Domain Selection section.
- 3 From the Selection list, choose All domains.

Fixed Constraint I

- I In the Physics toolbar, click Boundaries and choose Fixed Constraint.
- **2** Select Boundaries 2, 8, and 9 only.

Roller 1

- I In the Physics toolbar, click Boundaries and choose Roller.
- 2 Select Boundaries 1, 3, and 5 only.

MULTIPHYSICS

Poroelasticity I (porol)

I In the Model Builder window, under Component I (compl)>Multiphysics click Poroelasticity I (porol).

- **2** In the **Settings** window for **Poroelasticity**, locate the **Poroelastic Coupling Properties** section.
- **3** From the α_B list, choose **User defined**. In the associated text field, type 1.

MATERIALS

Fill the required fields in the material properties tables.

Fluid (mat1)

I In the Model Builder window, under Component I (compl)>Materials click Fluid (matl).

2 In the Settings window for Material, locate the Material Contents section.

3 In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Compressibility of fluid	chif	4e-10	I/Pa	Basic
Density	rho	1000	kg/m³	Basic

Porous I (mat2)

I In the Model Builder window, click Porous I (mat2).

2 In the Settings window for Material, locate the Material Contents section.

3 In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	E	800[MPa]	Pa	Basic
Poisson's ratio	nu	0.25	I	Basic
Density	rho	2750	kg/m³	Basic

Porous 2 (mat3)

I In the Model Builder window, click Porous 2 (mat3).

2 In the Settings window for Material, locate the Material Contents section.

3 In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	E	80[MPa]	Pa	Basic
Poisson's ratio	nu	0.25	I	Basic
Density	rho	2750	kg/m³	Basic

DEFINITIONS

Create a variable to calculate the solid-to-fluid coupling term.

Variables 3

- I In the Model Builder window, expand the Component I (compl)>Definitions node, then click Variables 3.
- 2 In the Settings window for Variables, locate the Variables section.
- **3** In the table, enter the following settings:

Name	Expression	Unit
Q_biot	-poro1.alphaB*d(solid.evol,TIME)*dl.rho	kg/(m³·s)

STUDY I

Disable the newly created nodes in the existing study.

Step 1: Time Dependent

- I In the Model Builder window, expand the Study I node, then click Step I: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Physics and Variables Selection section.
- 3 In the table, clear the Solve for check box for Solid Mechanics (solid).
- 4 In the table, clear the Solve for check box for Poroelasticity I (porol).
- 5 Select the Modify model configuration for study step check box.
- 6 In the Physics and variables selection tree, select Component I (compl)>Darcy's Law (dl)> Poroelastic Storage I.
- 7 Click 🕖 Disable.

ADD STUDY

- I In the Home toolbar, click $\sim\sim$ Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies> Time Dependent.
- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click ~ 1 Add Study to close the Add Study window.

STUDY 2

Step 1: Time Dependent

Now set up the fully coupled study. As described in Notes About the COMSOL Implementation in the beginning, the time step has to be small until an equilibrium between gravity forces and poroelastic forces is reached. Studies have shown that this is the case after 0.2 years. After that, a bigger time step is sufficient and should be chosen with respect to computational time and space.

- I In the Settings window for Time Dependent, locate the Study Settings section.
- 2 From the Time unit list, choose a.
- 3 Click Range.
- 4 In the Range dialog box, type 0.01 in the Step text field.
- **5** In the **Stop** text field, type **0.2**.
- 6 Click Replace.
- 7 In the Settings window for Time Dependent, locate the Study Settings section.
- 8 Click Range.
- 9 In the Range dialog box, type 1 in the Step text field.
- **IO** In the **Start** text field, type 1.
- II In the **Stop** text field, type 10.
- I2 Click Add.
- **I3** In the **Home** toolbar, click **= Compute**.

RESULTS

Follow the steps below to reproduce the plots shown in Figure 2 through Figure 4.

Hydraulic Head, Poroelasticity

- I In the Home toolbar, click 📠 Add Plot Group and choose 2D Plot Group.
- 2 In the Settings window for 2D Plot Group, type Hydraulic Head, Poroelasticity in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study 2/Solution 2 (sol2).

Surface 1

- I Right-click Hydraulic Head, Poroelasticity and choose Surface.
- 2 In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>Darcy's Law> dl.H Hydraulic head m.

Contour I

- I In the Model Builder window, right-click Hydraulic Head, Poroelasticity and choose Contour.
- 2 In the Settings window for Contour, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>Solid Mechanics> Displacement>solid.disp - Displacement magnitude - m.
- 3 Locate the Levels section. From the Entry method list, choose Levels.
- 4 In the Levels text field, type range(0,0.2,2.3).
- 5 Locate the Coloring and Style section. From the Coloring list, choose Uniform.
- 6 From the Color list, choose Black.
- 7 Clear the **Color legend** check box.
- 8 Click to expand the Quality section. From the Resolution list, choose Extra fine.

Arrow Surface 1

- I Right-click Hydraulic Head, Poroelasticity and choose Arrow Surface.
- 2 In the Settings window for Arrow Surface, locate the Expression section.
- **3** In the **X** component text field, type d(dl.H,X).
- **4** In the **Y** component text field, type d(dl.H,Y).
- **5** Select the **Description** check box.
- 6 In the associated text field, type Hydraulic head gradient (1).
- 7 Locate the Arrow Positioning section. Find the X grid points subsection. In the Points text field, type 25.

Deformation I

- I In the Model Builder window, right-click Surface I and choose Deformation.
- 2 In the Settings window for Deformation, locate the Scale section.
- 3 Select the Scale factor check box.
- **4** In the associated text field, type **10**.
- 5 Right-click Deformation I and choose Copy.

Deformation I

In the Model Builder window, right-click Contour I and choose Paste Deformation.

Arrow Surface 1

- I In the Settings window for Arrow Surface, locate the Coloring and Style section.
- 2 Select the Scale factor check box.

- 3 In the Hydraulic Head, Poroelasticity toolbar, click **9** Plot.
- 4 In the associated text field, type 2e4.

Deformation 1

Right-click Arrow Surface I and choose Paste Deformation.

Hydraulic Head, Poroelasticity

- I In the Settings window for 2D Plot Group, locate the Data section.
- 2 From the Time (a) list, choose 2.
- **3** In the **Hydraulic Head**, **Poroelasticity** toolbar, click **O Plot**.
- 4 Click the Zoom Extents button in the Graphics toolbar.
 Compare the resulting plot with that in Figure 2.
- 5 From the Time (a) list, choose 5.
- 6 In the Hydraulic Head, Poroelasticity toolbar, click 🗿 Plot.

The plot in the **Graphics** window should now look like that in Figure 3.

- 7 From the Time (a) list, choose 10.
- 8 In the Hydraulic Head, Poroelasticity toolbar, click 💽 Plot.

Compare with Figure 4.

Next, modify the second default plot to reproduce Figure 7.

von Mises Stress

- I In the Model Builder window, under Results click Stress (solid).
- 2 In the Settings window for 2D Plot Group, type von†Mises Stress in the Label text field.
- 3 In the Model Builder window, expand the von Mises Stress node.

Deformation

- I In the Model Builder window, expand the Results>von Mises Stress>Surface I node, then click Deformation.
- 2 In the Settings window for Deformation, locate the Scale section.
- **3** Select the **Scale factor** check box.
- **4** In the associated text field, type **10**.

Streamline 1

- I In the Model Builder window, right-click von Mises Stress and choose Streamline.
- 2 In the Settings window for Streamline, locate the Streamline Positioning section.

- **3** From the **Positioning** list, choose **Starting-point controlled**.
- 4 From the Entry method list, choose Coordinates.
- **5** In the **X** text field, type **0**.
- **6** In the **Y** text field, type range(-450, 50, -50).
- 7 Locate the Coloring and Style section. Find the Point style subsection. From the Color list, choose White.
- 8 Click to expand the Quality section. From the Smoothing list, choose Everywhere.

Deformation

In the Model Builder window, right-click Deformation and choose Copy.

Deformation

In the Model Builder window, right-click Streamline I and choose Paste Deformation.

Next, reproduce the plot in Figure 5 showing the solid-to-fluid coupling term.

Solid-to-Fluid Coupling Term

- I In the Home toolbar, click 📠 Add Plot Group and choose 2D Plot Group.
- 2 In the Settings window for 2D Plot Group, type Solid-to-Fluid Coupling Term in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study 2/Solution 2 (sol2).
- 4 Click → Plot Last.

Surface 1

- I Right-click Solid-to-Fluid Coupling Term and choose Surface.
- 2 In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>Definitions> Variables>Q_biot kg/(m³·s).
- 3 In the Solid-to-Fluid Coupling Term toolbar, click **D** Plot.

To set up the plot in Figure 6 proceed as follows:

Cut Line 2D I

- I In the **Results** toolbar, click \frown **Cut Line 2D**.
- 2 In the Settings window for Cut Line 2D, locate the Data section.
- 3 From the Dataset list, choose Study 2/Solution 2 (sol2).
- 4 Locate the Line Data section. In row Point I, set X to 1000.
- **5** In row **Point 2**, set **X** to 5000.

Horizontal Strain

- I In the **Results** toolbar, click \sim **ID Plot Group**.
- 2 In the Settings window for ID Plot Group, type Horizontal Strain in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Cut Line 2D I.
- 4 From the Time selection list, choose From list.
- 5 In the Times (a) list, choose 2, 5, and 10.

Line Graph 1

- I Right-click Horizontal Strain and choose Line Graph.
- 2 In the Settings window for Line Graph, click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>
 Solid Mechanics>Strain>Strain tensor (material and geometry frames)>solid.eXX Strain tensor, XX component.
- 3 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- 4 Click Replace Expression in the upper-right corner of the x-Axis Data section. From the menu, choose Component I (compl)>Geometry>
 Coordinate (material and geometry frames)>X X-coordinate.
- 5 Click to expand the Legends section. Select the Show legends check box.
- 6 In the Horizontal Strain toolbar, click 💽 Plot.