

Wideband RCS Calculation Using Time-Domain Simulation and FFT

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Introduction

This model shows how to calculate the radar cross section (RCS) of a scatterer in a wide frequency range with the Electromagnetic Waves, Time Explicit physics interface. The problem is solved in the scattered-field formulation, where the background field is a temporally modulated Gaussian pulse. The simulated results present the scattered field in the frequency domain and time domain, and the RCS per unit length of a circle in the frequency domain.



Figure 1: A PEC circle is enclosed by a circular vacuum domain. The outermost layer is finished with an absorbing layer to absorb outgoing waves from the modulated Gaussian background pulse and the scattered field from the circular scatterer.

Model Definition

The model is solved using the scattered field formulation, that is automatically activated by adding a background field domain. The built-in Gaussian pulse, modulated with a sinusoidal function at 200 MHz, is used for background field. The wave vector of the background field is pointing toward the +x direction with z-directional polarization and $120\pi \Omega$ wave impedance. The distance from the coordinate system origin to the wave launching plane is set to 1.5 m (See Figure 1). So, the wave is launched at the boundary of the vacuum domain.

The metallic circle is modeled using the perfect electric conductor boundary condition and its inner part is removed from the model domain. This is done because the skin depth is much smaller than the size of the circle. The circle's scattered field is computed on the boundaries configured by the Far-Field Domain node and its Far-Field Calculation subfeature, by performing a near-field to far-field transformation in the frequency domain after a fast Fourier transform (FFT). The PEC circle is surrounded by vacuum. The simulations are performed with two different absorbing features:

- I A scattering boundary condition (first order absorbing boundary condition) applied on the exterior boundary of the vacuum domain.
- 2 An absorbing layer domain on the outside of the surrounding vacuum domain acting as an absorber of the scattered field. The absorbing layer is placed at more than one wavelength away from the scatterer. The effect of the absorbing layer is to make the outermost layer appear as much larger for the outgoing waves. At the outermost boundary, the waves will reach the boundary propagating in the normal direction. Thus, the scattering boundary condition, added to the outermost boundary, will effectively absorb the outgoing waves.

The entire simulation consists of two study steps and one study extension step. The first step is a Time Dependent study for computing a temporal solution. The second step is a Time to Frequency FFT study, where an FFT is performed to obtain a frequency spectrum of the temporal solution. The last step is a Combine Solutions study extension step. This study extension step removes the unwanted parts of the frequency spectrum after the FFT (the first and the last 5% of the frequency spectrum), using a user-defined expression such as freq<0.1*fb0 || freq>2*fb0-0.1*fb0.

Results and Discussion

In Figure 2, the dB-scaled RCS per unit length is plotted for 100 MHz, 200 MHz, and 300 MHz when using either an absorbing layer or a scattering boundary condition to absorb the outgoing wave from the background field and scattered field from the PEC circle. The RCS difference between two cases is less than 0.2 dB at the backward scattering direction and around 0.5 dB at the forward scattering direction.



Figure 2: The dB-scaled RCS per unit length with the absorbing layer (solid) and scattering boundary condition (dashed).

Notes About the COMSOL Implementation

In the scattered field formulation, the total field is defined as $\mathbf{E}_{total} = \mathbf{E}_{rel} + \mathbf{E}_{b}$ where \mathbf{E}_{rel} is the relative field and \mathbf{E}_{b} is the background field. The relative field is the difference between the total field caused by the presence of the scatterer and the background field. After performing the time dependent study and the FFT, only the relative field and postprocessing variables related to far-field analysis are available in the frequency domain, since the FFT takes only dependent variables. Other postprocessing variables are valid only in the time domain and can be accessed via stored solutions.

VARIABLE	DESCRIPTION	AVAILABILITY	
comp1.Ez or Ez	Dependent variable, Relative (scattered) field	Frequency domain	
ewte.Ez	Total field	Time domain	
ewte.Ebz	Background field	Time domain	
ewte.bRCS2D	RCS per unit length	Frequency domain	

TABLE I: AVAILABILITY OF VARIABLES FOR POSTPROCESSING.

Application Library path: RF_Module/Scattering_and_RCS/rcs_time_explicit

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click 🖉 Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click **2D**.
- 2 In the Select Physics tree, select Radio Frequency>Electromagnetic Waves, Time Explicit (ewte).
- 3 Click Add.
- 4 Click \bigcirc Study.
- 5 In the Select Study tree, select Preset Studies for Selected Physics Interfaces> Time Dependent with FFT.
- 6 Click M Done.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
fb0	200[MHz]	2E8 Hz	Modulated Gaussian center frequency
lda0	c_const/fb0	I.499 m	Wavelength
k0	2*pi/ldaO	4.1917 1/m	Wave number
Т0	1/fb0	5E-9 s	Modulation period

Here, c_const used in the free space wavelength is a predefined COMSOL constant for the speed of light in vacuum.

GEOMETRY I

Circle I (c1)

- I In the **Geometry** toolbar, click \bigcirc **Circle**.
- 2 In the Settings window for Circle, locate the Size and Shape section.
- 3 In the Radius text field, type 2.5.

Circle 2 (c2)

- I In the **Geometry** toolbar, click \bigcirc **Circle**.
- 2 In the Settings window for Circle, locate the Size and Shape section.
- 3 In the **Radius** text field, type 0.7.

Difference I (dif1)

- I In the Geometry toolbar, click i Booleans and Partitions and choose Difference.
- 2 Select the object **cl** only.
- 3 In the Settings window for Difference, locate the Difference section.
- 4 Find the Objects to subtract subsection. Select the 🔲 Activate Selection toggle button.
- **5** Select the object **c2** only.
- 6 Click 🟢 Build All Objects.



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ELECTROMAGNETIC WAVES, TIME EXPLICIT (EWTE)

- I In the Model Builder window, under Component I (compl) click Electromagnetic Waves, Time Explicit (ewte).
- **2** In the **Settings** window for **Electromagnetic Waves**, **Time Explicit**, locate the **Components** section.
- 3 From the Field components solved for list, choose H in plane (TE wave).

Background Field 1

- I In the Physics toolbar, click **Domains** and choose **Background Field**.
- **2** Select Domain 1 only.
- 3 In the Settings window for Background Field, locate the Settings section.
- 4 From the Polarization direction list, choose z.
- **5** In the f_0 text field, type fb0.
- **6** In the d_{offset} text field, type **2.5**.

Scattering Boundary Condition I

I In the Physics toolbar, click — Boundaries and choose Scattering Boundary Condition.





Far-Field Domain I In the **Physics** toolbar, click **Domains** and choose **Far-Field Domain**.

Far-Field Calculation 1

I In the Model Builder window, expand the Far-Field Domain I node, then click Far-Field Calculation I.



2 Select Boundaries 3, 4, 6, and 7 only.

MATERIALS

Material I (mat1)

- I In the Model Builder window, under Component I (compl) right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, locate the Material Contents section.
- **3** In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Relative permittivity	epsilonr_iso ; epsilonrii = epsilonr_iso, epsilonrij = 0	1	I	Basic

Property	Variable	Value	Unit	Property group
Relative permeability	mur_iso ; murii = mur_iso, murij = 0	1	1	Basic
Electrical conductivity	sigma_iso ; sigmaii = sigma_iso, sigmaij = 0	0	S/m	Basic

MESH I

- I In the Model Builder window, under Component I (compl) click Mesh I.
- 2 In the Settings window for Mesh, locate the Mesh Settings section.
- **3** From the Sequence type list, choose User-controlled mesh.

Size

- I In the Model Builder window, under Component I (compl)>Mesh I click Size.
- 2 In the Settings window for Size, locate the Element Size section.
- **3** Click the **Custom** button.
- 4 Locate the **Element Size Parameters** section. In the **Maximum element size** text field, type 1da0/5.

This sets the maximum mesh element size to 0.2 wavelengths.



STUDY I

Step 1: Time Dependent

- I In the Model Builder window, under Study I click Step I: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- 3 In the **Output times** text field, type range(0,1/(4*fb0),10*T0). The Sampling rate 4*fb0 satisfies the Nyquist condition for the time to frequency fast Fourier transform (FFT) where its bandwidth is 2*fb0 excluding negative frequencies.

Step 2: Time to Frequency FFT

- I In the Model Builder window, click Step 2: Time to Frequency FFT.
- 2 In the Settings window for Time to Frequency FFT, locate the Study Settings section.
- 3 In the End time text field, type 20*T0. This makes sure that the FFT end time is longer than the simulation time so zero-padding can be applied during the time to frequency FFT. This will generate a finer frequency resolution in the resulting frequency response.
- 4 In the Maximum output frequency text field, type 2*fb0.

Step 3: Combine Solutions

I In the Model Builder window, click Step 3: Combine Solutions.

- **2** In the **Settings** window for **Combine Solutions**, locate the **Combine Solutions Settings** section.
- **3** In the **Excluded if** text field, type freq<0.1*fb0 || freq>2*fb0-0.1*fb0. This excludes the first 5% and last 5% of the frequency response after FFT.
- **4** In the **Home** toolbar, click **= Compute**.

RESULTS

Polar Plot Group 1

- I In the Settings window for Polar Plot Group, locate the Data section.
- 2 From the Parameter selection (freq) list, choose From list.
- 3 In the Parameter values (freq (Hz)) list, choose IE8, 2E8, and 3E8.
- 4 Click to expand the Title section. From the Title type list, choose Manual.
- 5 In the Title text area, type Bistatic RCS per unit length (dB).

Radiation Pattern 1

- I In the Model Builder window, expand the Polar Plot Group I node, then click Radiation Pattern I.
- 2 In the Settings window for Radiation Pattern, click to expand the Legends section.
- 3 Select the Show legends check box.
- 4 Click to expand the **Coloring and Style** section. In the **Width** text field, type 2.

5 In the Polar Plot Group I toolbar, click **I** Plot.



The RCS per unit length of the circle is plotted.

2D Plot Group 2

- I In the Home toolbar, click 📠 Add Plot Group and choose 2D Plot Group.
- 2 In the Settings window for 2D Plot Group, locate the Data section.
- 3 From the Parameter value (freq (Hz)) list, choose 2E8.
- 4 Click to expand the Title section. From the Title type list, choose Manual.
- 5 In the Title text area, type Scattered field at 200MHz.

Surface 1

- I Right-click 2D Plot Group 2 and choose Surface.
- 2 In the Settings window for Surface, locate the Expression section.
- **3** In the **Expression** text field, type Ez. This depedent variable is z-component of the scattered field.



4 In the 2D Plot Group 2 toolbar, click **I** Plot.

2D Plot Group 3

- I In the Home toolbar, click 📠 Add Plot Group and choose 2D Plot Group.
- 2 In the Settings window for 2D Plot Group, locate the Data section.
- 3 From the Dataset list, choose Study I/Solution Store I (sol2).
- 4 From the Time (s) list, choose IE-8.
- 5 Locate the Title section. From the Title type list, choose Manual.
- 6 In the Title text area, type Scattered field at 10ns.

Surface 1

- I Right-click 2D Plot Group 3 and choose Surface.
- 2 In the Settings window for Surface, locate the Expression section.
- **3** In the **Expression** text field, type ewte.Ez-ewte.Ebz. This is the difference in z-components between the total field and background field.
- 4 Locate the Coloring and Style section. From the Color table list, choose HeatCameraLight.



5 In the 2D Plot Group 3 toolbar, click 💽 Plot.

Circle I (c1)

- I In the Model Builder window, under Component I (compl)>Geometry I click Circle I (cl).
- 2 In the Settings window for Circle, locate the Size and Shape section.
- **3** In the **Radius** text field, type **3.5**.
- 4 Click to expand the Layers section. In the table, enter the following settings:

Layer name	Thickness (m)		
Layer 1	1		



DEFINITIONS



2 Select Domains 1–4 only.



- 3 In the Settings window for Absorbing Layer, locate the Geometry section.
- 4 From the Type list, choose Cylindrical.

ELECTROMAGNETIC WAVES, TIME EXPLICIT (EWTE)

Background Field I

 In the Model Builder window, under Component I (comp1)>Electromagnetic Waves, Time Explicit (ewte) click Background Field I.





MESH I

In the Model Builder window, under Component I (comp1) right-click Mesh I and choose Build All.



ADD STUDY

I In the Home toolbar, click $\sim\sim$ Add Study to open the Add Study window.

- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select Preset Studies for Selected Physics Interfaces>Time Dependent with FFT.
- 4 Click + Add Study.
- 5 In the Home toolbar, click $\stackrel{\text{res}}{\longrightarrow}$ Add Study to close the Add Study window.

STUDY 2

Step 1: Time Dependent

- I In the Settings window for Time Dependent, locate the Study Settings section.
- 2 In the **Output times** text field, type range(0,1/(4*fb0),10*T0).

Step 2: Time to Frequency FFT

I In the Model Builder window, click Step 2: Time to Frequency FFT.

- 2 In the Settings window for Time to Frequency FFT, locate the Study Settings section.
- **3** In the **End time** text field, type 20*T0.
- 4 In the Maximum output frequency text field, type 2*fb0.

Step 3: Combine Solutions

- I In the Model Builder window, click Step 3: Combine Solutions.
- **2** In the **Settings** window for **Combine Solutions**, locate the **Combine Solutions Settings** section.
- 3 In the Excluded if text field, type freq<0.1*fb0 || freq>2*fb0-0.1*fb0.
- **4** In the **Home** toolbar, click **= Compute**.

RESULTS

Radiation Pattern 2

- I In the Model Builder window, under Results>Polar Plot Group I right-click Radiation Pattern I and choose Duplicate.
- 2 In the Settings window for Radiation Pattern, locate the Data section.
- 3 From the Dataset list, choose Study 2/Solution 4 (sol4).
- **4** From the **Parameter selection (freq)** list, choose **From list**.
- 5 In the Parameter values (freq (Hz)) list, choose IE8, 2E8, and 3E8.

Radiation Pattern 1

- I In the Model Builder window, click Radiation Pattern I.
- 2 In the Settings window for Radiation Pattern, locate the Legends section.
- 3 From the Legends list, choose Manual.
- **4** In the table, enter the following settings:

Legends

100	MHz	Sca	atte	ring	BC

200 MHz Scattering BC

300 MHz Scattering BC

Radiation Pattern 2

- I In the Model Builder window, click Radiation Pattern 2.
- 2 In the Settings window for Radiation Pattern, locate the Legends section.
- 3 From the Legends list, choose Manual.

4 In the table, enter the following settings:

Legends					
100	MHz	Absorbing	Layer		
200	MHz	Absorbing	Layer		
300	MHz	Absorbing	Layer		

5 Locate the **Coloring and Style** section. Find the **Line style** subsection. From the **Line** list, choose **Dashed**.

The RCS per unit length when using the scattering boundary condition and absorbing layer is shown in Figure 2.