Analyzing Porous Structures on the Microscopic Scale

Introduction

Modeling flow through realistic porous structures is difficult due to the complexity of the structure itself. Resolving the flow field in detail is not feasible in real-life applications. Therefore, macroscopic approaches utilizing averaged quantities of the porous structure, such as porosity and permeability, are used. This example analyzes the flow field at the pore scale in detail. The results are used to validate and adapt the macroscopic description, which in turn are used to model large-scale porous geometries.

Model Definition

The modeled geometry shown in Figure 1 is a representative elementary volume (REV) whose properties are representative for the entire system.
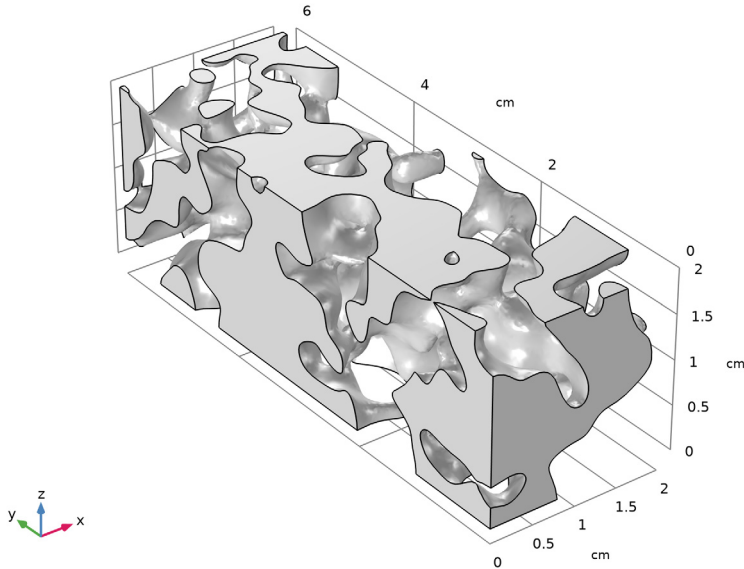

Figure 1: Geometry of the REV's pore volume.

Because only the area of the pore space is required for modeling, the porous matrix is not resolved explicitly. The REV has a quadratic cross section of 2 cm side length and a width of 6 cm. Water flows with a velocity of $u = 0.1$ mm/s and can flow out freely in the normal direction at the other end. The other boundaries are assumed to be symmetry boundaries.

This does not correspond to the actual situation, but for modeling an REV, symmetry boundary conditions are very well suited.

To characterize the flow inside the porous structure one can estimate the Reynolds number according to

$$\text{Re} = \frac{\rho u L}{\mu}$$

with the water density $\rho = 1000$ kg/m^3 and viscosity $\mu = 10^{-3}$ Pa·s. The cross-section side length serves as the characteristic length scale, L. This results in $\text{Re} = 2$ and the Stokes equation can be used to describe the flow where inertia terms are neglected.

Finally, the goal of the model is to obtain the averaged values for porosity and permeability to describe a macroscopic model with, for example, Darcy's law or the Brinkman equation. The porosity is defined as the fraction of pore space volume V_{fluid} to total volume V_{tot}:

$$\varepsilon = \frac{V_{\text{fluid}}}{V_{\text{tot}}}.$$

To calculate the permeability κ (m^2) the following relationship is used:

$$\mathbf{u} = -\frac{\kappa}{\mu}\nabla p$$

Approximating the pressure gradient ∇p by the pressure difference between the inlet and the outlet, Δp, divided by the side length L, and replacing the velocity vector $\mathbf{u}$ by the outlet velocity u_{out} in the flow direction gives the expression

$$\kappa = u_{\text{out}}\mu\frac{L}{\Delta p}.$$

Results and Discussion

First of all it is interesting to have a look at the mesh, or rather the mesh quality. Although the mesh quality in itself says nothing about the quality of the results, a good mesh quality is beneficial for convergence. The overall mesh quality as shown in Figure 2 is very good.
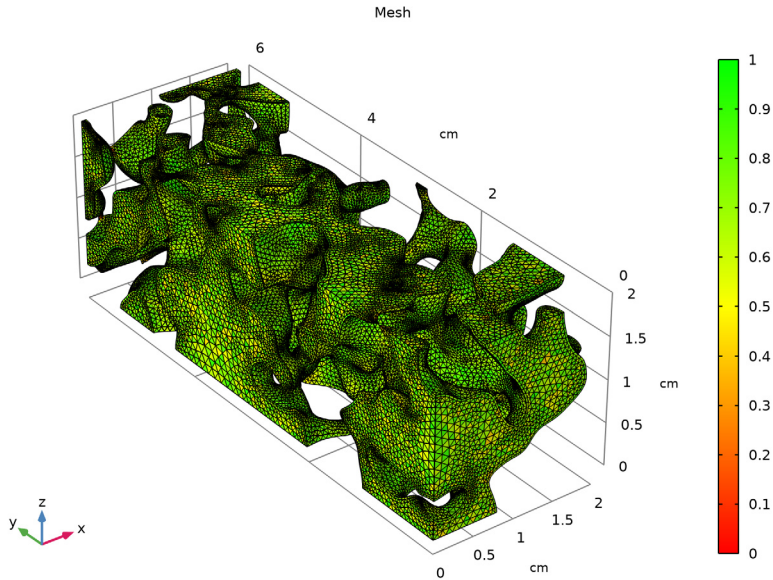

Figure 2: Mesh quality plot.

The velocity field in the REV is shown in Figure 3. Characteristic for the flow in a porous material are areas with high and areas with low velocity. In some areas the flow also stagnates. This behavior is characterized by the permeability.
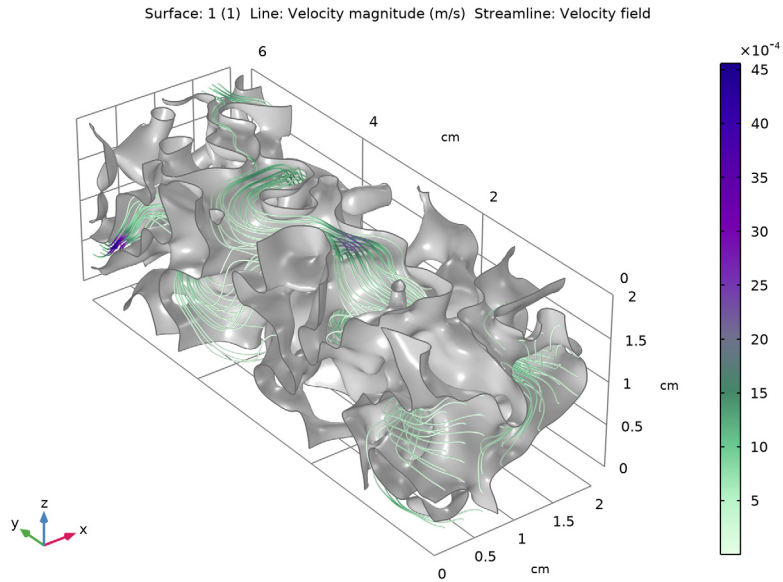
Surface: 1 (1) Line: Velocity magnitude (m/s) Streamline: Velocity field

Figure 3: Velocity in the REV.

From the simulation the values for the porosity and permeability are obtained, with $\varepsilon = 0.373$ and $\kappa \approx 3 \cdot 10^{-8} \, \mathrm{m}^2$.

Notes About the COMSOL Implementation

The geometry is characterized by narrow regions and a complex free surface. This has a great influence on the mesh. The automatic meshing algorithm can be tuned by certain manual settings, which is beneficial for both mesh quality and performance.

Application Library path: `Porous_Media_Flow_Module/Fluid_Flow/pore_scale_flow_3d`

Modeling Instructions

From the **File** menu, choose **New**.

N E W

In the **New** window, click **Model Wizard**.

M O D E L   W I Z A R D

1 In the **Model Wizard** window, click ▊ **3D**.

2 In the **Select Physics** tree, select **Fluid Flow>Single-Phase Flow>Creeping Flow (spf)**.

3 Click **Add**.

4 Click ➡ **Study**.

5 In the **Select Study** tree, select **General Studies>Stationary**.

6 Click ☑ **Done**.

G E O M E T R Y   1

1 In the **Model Builder** window, under **Component 1 (comp1)** click **Geometry 1**.

2 In the **Settings** window for **Geometry**, locate the **Units** section.

3 From the **Length unit** list, choose **cm**.

Import 1 (imp1)

1 In the **Home** toolbar, click ↤ **Import**.

2 In the **Settings** window for **Import**, locate the **Import** section.

3 Click **Browse**.

4 Browse to the model's Application Libraries folder and double-click the file
   `pore_scale_flow_3d.mphbin`.

5 Click **Import**.

G L O B A L   D E F I N I T I O N S

Add some parameters that are used to set up the model.

Parameters 1

1 In the **Model Builder** window, under **Global Definitions** click **Parameters 1**.

2 In the **Settings** window for **Parameters**, locate the **Parameters** section.

3 In the table, enter the following settings:

Name	Expression	Value	Description
rho_f	1000[kg/m^3]	1000 kg/m³	Fluid density
mu_f	1e-3[Pa*s]	0.001 Pa·s	Fluid viscosity
u_in	1e-4[m/s]	1E-4 m/s	Inlet velocity
width	2[cm]	0.02 m	REV width
length	6[cm]	0.06 m	REV length
V_tot	width^2*length	2.4E-5 m³	Total REV volume

MATERIALS

Water

1 In the **Model Builder** window, under **Component 1 (comp1)** right-click **Materials** and choose **Blank Material**.

2 In the **Settings** window for **Material**, type Water in the **Label** text field.

3 Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Density	rho	rho_f	kg/m³	Basic
Dynamic viscosity	mu	mu_f	Pa·s	Basic

CREEPING FLOW (SPF)

1 In the **Model Builder** window, under **Component 1 (comp1)** click **Creeping Flow (spf)**.

2 In the **Settings** window for **Creeping Flow**, click to expand the **Discretization** section.

3 From the **Discretization of fluids** list, choose **P1+P1**.

Linear elements reduce the number of degrees of freedom to be solved. Because the geometry already requires a fine mesh, using linear elements decreases computational time and memory requirements while maintaining sufficient accuracy.

Inlet 1

1 In the **Physics** toolbar, click [icon] **Boundaries** and choose **Inlet**.

2 Select Boundary 2 only.

3 In the **Settings** window for **Inlet**, locate the **Velocity** section.

4 In the U_0 text field, type u_in.

5 Locate the **Boundary Selection** section. Click [icon] **Create Selection**.

6 In the **Create Selection** dialog box, type Inlet in the **Selection name** text field.

7 Click **OK**.

Outlet 1

1 In the **Physics** toolbar, click ▬ **Boundaries** and choose **Outlet**.

2 Select Boundaries 16 and 22 only.

3 In the **Settings** window for **Outlet**, locate the **Pressure Conditions** section.

4 Select the **Normal flow** check box.

5 Locate the **Boundary Selection** section. Click ⬚ **Create Selection**.

6 In the **Create Selection** dialog box, type Outlet in the **Selection name** text field.

7 Click **OK**.

Create a few more selections to use them throughout the model set up.

DEFINITIONS

In the **Model Builder** window, expand the **Definitions** node.

Wall

1 In the **Model Builder** window, expand the **Component 1 (comp1)>Definitions>Selections** node.

2 Right-click **Component 1 (comp1)>Definitions>Selections** and choose **Explicit**.

3 In the **Settings** window for **Explicit**, type Wall in the **Label** text field.

4 Locate the **Input Entities** section. From the **Geometric entity level** list, choose **Boundary**.

5 Select Boundaries 4, 10, and 30 only.

It might be easier to select the correct boundary by using the **Selection List** window. To open this window, in the **Home** toolbar click **Windows** and choose **Selection List**. (If you are running the cross-platform desktop, you find **Windows** in the main menu.)

All boundaries

1 In the **Definitions** toolbar, click ⬚ **Explicit**.

2 In the **Settings** window for **Explicit**, locate the **Input Entities** section.

3 From the **Geometric entity level** list, choose **Boundary**.

4 Select the **All boundaries** check box.

5 In the **Label** text field, type All boundaries.

Symmetry

1 In the **Definitions** toolbar, click ⬚ **Difference**.

2 In the **Settings** window for **Difference**, type Symmetry in the **Label** text field.

3 Locate the **Geometric Entity Level** section. From the **Level** list, choose **Boundary**.

4 Locate the **Input Entities** section. Under **Selections to add**, click ✛ **Add**.

5 In the **Add** dialog box, select **All boundaries** in the **Selections to add** list.

6 Click **OK**.

7 In the **Settings** window for **Difference**, locate the **Input Entities** section.

8 Under **Selections to subtract**, click ✛ **Add**.

9 In the **Add** dialog box, in the **Selections to subtract** list, choose **Inlet**, **Outlet**, and **Wall**.

10 Click **OK**.

CREEPING FLOW (SPF)

Symmetry 1

1 In the **Physics** toolbar, click ▬ **Boundaries** and choose **Symmetry**.

2 In the **Settings** window for **Symmetry**, locate the **Boundary Selection** section.

3 From the **Selection** list, choose **Symmetry**.

MESH 1

The physics-controlled mesh is a good starting point. Modify the sequence to help the meshing algorithm and improve overall quality.

1 In the **Model Builder** window, under **Component 1 (comp1)** click **Mesh 1**.

2 In the **Settings** window for **Mesh**, locate the **Physics-Controlled Mesh** section.

3 From the **Element size** list, choose **Extra fine**.

4 Locate the **Mesh Settings** section. From the **Sequence type** list, choose **User-controlled mesh**.

Size

1 In the **Model Builder** window, under **Component 1 (comp1)>Mesh 1** click **Size**.

2 In the **Settings** window for **Size**, click to expand the **Element Size Parameters** section.

3 Locate the **Element Size** section. Click the **Custom** button.

4 Locate the **Element Size Parameters** section. In the **Maximum element size** text field, type 0.125.

Size 1

1 In the **Model Builder** window, click **Size 1**.

2 In the **Settings** window for **Size**, locate the **Element Size** section.

3 Click the **Custom** button.

4 Locate the **Element Size Parameters** section. Select the **Maximum element size** check box.

5 In the associated text field, type 0.06.

Corner Refinement 1

1 In the **Model Builder** window, right-click **Corner Refinement 1** and choose **Disable**.

2 In the **Settings** window for **Corner Refinement**, click 🔲 **Build Selected**.

Corner refinement will not improve the mesh significantly, hence it is disabled.

Free Triangular 1

1 In the **Mesh** toolbar, click △ **Boundary** and choose **Free Triangular**.

2 In the **Settings** window for **Free Triangular**, locate the **Boundary Selection** section.

3 From the **Selection** list, choose **Wall**.

4 Click 🔲 **Build Selected**.

Creating a surface mesh for the freeform surface first, helps the meshing algorithm.
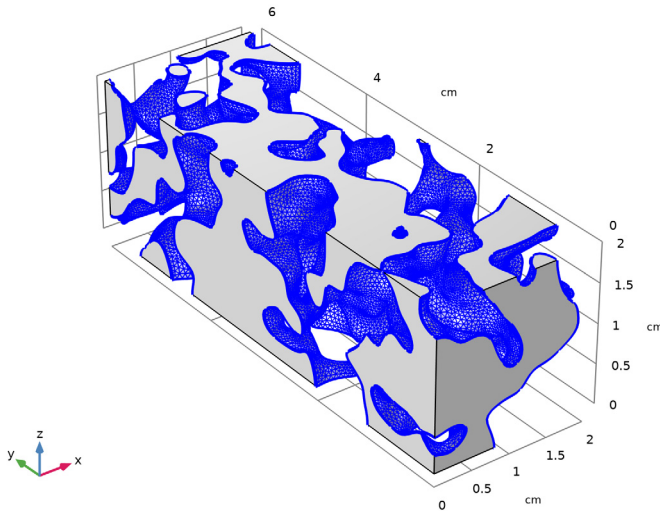
To ensure a good quality of the mesh, we use the following settings for the tetrahedral mesh.

Free Tetrahedral 1

1 In the **Model Builder** window, click **Free Tetrahedral 1**.

2 In the **Settings** window for **Free Tetrahedral**, click to expand the **Element Quality Optimization** section.

3 Select the **Avoid too large elements** check box.

4 Select the **Avoid too small elements** check box.

5 From the **Optimization level** list, choose **Medium**.

6 Click ▦ **Build All**.

7 In the **Mesh** toolbar, click ▲ **Plot**.

RESULTS

Mesh 1

Compare with Figure 2. The overall mesh quality is very good. The amount of low quality mesh elements (skewness) is low. Mesh quality is not an indication for the accuracy of the solution, but it affects the convergence behavior.

STUDY 1

1 In the **Model Builder** window, click **Study 1**.

2 In the **Settings** window for **Study**, locate the **Study Settings** section.

3 Clear the **Generate default plots** check box.

4 In the **Home** toolbar, click ▬ **Compute**.

Create the plot as shown in Figure 3.

5 In the **Results** toolbar, click ▦ **More Datasets** and choose **Surface**.

RESULTS

Surface 1

1 In the **Settings** window for **Surface**, locate the **Selection** section.

2 From the **Selection** list, choose **Wall**.

Velocity

1 In the **Results** toolbar, click ▮ **3D Plot Group**.

2 In the **Settings** window for **3D Plot Group**, type Velocity in the **Label** text field.

3 Locate the **Plot Settings** section. Clear the **Plot dataset edges** check box.

Surface 1

1 Right-click **Velocity** and choose **Surface**.

2 In the **Settings** window for **Surface**, locate the **Data** section.

3 From the **Dataset** list, choose **Surface 1**.

4 Locate the **Expression** section. In the **Expression** text field, type 1.

5 Locate the **Coloring and Style** section. From the **Coloring** list, choose **Uniform**.

6 From the **Color** list, choose **Gray**.

Line 1

1 In the **Model Builder** window, right-click **Velocity** and choose **Line**.

2 In the **Settings** window for **Line**, locate the **Data** section.

3 From the **Dataset** list, choose **Surface 1**.

4 Locate the **Coloring and Style** section. From the **Coloring** list, choose **Uniform**.

5 From the **Color** list, choose **Black**.

6 In the **Velocity** toolbar, click ⬛ **Plot**.

7 From the **Color** list, choose **Custom**. Choose a darker shade of gray.

Streamline 1

1 Right-click **Velocity** and choose **Streamline**.

2 In the **Settings** window for **Streamline**, locate the **Selection** section.

3 From the **Selection** list, choose **Inlet**.

4 Locate the **Streamline Positioning** section. In the **Number** text field, type 40.

5 Locate the **Coloring and Style** section. Find the **Line style** subsection. From the **Type** list, choose **Tube**.

6 Select the **Radius scale factor** check box.

7 In the associated text field, type 0.0075.

Color Expression 1

1 Right-click **Streamline 1** and choose **Color Expression**.

2 In the **Settings** window for **Color Expression**, locate the **Coloring and Style** section.

3 From the **Color table** list, choose **AuroraBorealis**.

Next, determine the porosity and permeability for our REV in order to perform simulations at the macroscopic level.

DEFINITIONS

Integration 1 (intop1)

1 In the **Definitions** toolbar, click ✐ **Nonlocal Couplings** and choose **Integration**.

2 In the **Settings** window for **Integration**, locate the **Source Selection** section.

3 From the **Selection** list, choose **All domains**.

Average Inlet

1 In the **Definitions** toolbar, click 🔗 **Nonlocal Couplings** and choose **Average**.

2 In the **Settings** window for **Average**, locate the **Source Selection** section.

3 From the **Geometric entity level** list, choose **Boundary**.

4 From the **Selection** list, choose **Inlet**.

5 In the **Label** text field, type Average Inlet.

Average Outlet

1 In the **Definitions** toolbar, click 🔗 **Nonlocal Couplings** and choose **Average**.

2 In the **Settings** window for **Average**, locate the **Source Selection** section.

3 From the **Geometric entity level** list, choose **Boundary**.

4 From the **Selection** list, choose **Outlet**.

5 In the **Label** text field, type Average Outlet.

Variables 1

1 In the **Model Builder** window, right-click **Definitions** and choose **Variables**.

2 In the **Settings** window for **Variables**, locate the **Variables** section.

3 In the table, enter the following settings:

Name	Expression	Unit	Description
por	intop1(1)/V_tot		Porosity
dPdL	-(aveop2(p)-aveop1(p))/ length	N/m³	Pressure drop
u_out	spf.out1.massFlowRate/ rho_f/width^2	m/s	Superficial outlet velocity
kappa	u_out*mu_f/dPdL	m²	Permeability

Since you have introduced new variables, the solution needs to be updated. It is not necessary to compute the study again.

STUDY 1

In the **Study** toolbar, click ↻ **Update Solution**.

RESULTS

Global Evaluation 1

1 In the **Results** toolbar, click (8.5) **Global Evaluation**.

2 In the **Settings** window for **Global Evaluation**, click **Add Expression** in the upper-right corner of the **Expressions** section. From the menu, choose **Component 1 (comp1)> Definitions>Variables>por - Porosity**.

3 Click **Add Expression** in the upper-right corner of the **Expressions** section. From the menu, choose **Component 1 (comp1)>Definitions>Variables>kappa - Permeability - m²**.

4 Click ▬ **Evaluate**.

The results are shown in the **Table** window. The porosity is 0.373 and the permeability is about 3e-8m^2. These results can now be used for calculations of large scale models.

Streamline 1

To make the results even more descriptive, create an animation.

1 In the **Model Builder** window, click **Streamline 1**.

2 In the **Settings** window for **Streamline**, locate the **Coloring and Style** section.

3 Find the **Point style** subsection. From the **Type** list, choose **Interactive arrow**.

4 In the **Extra release times** text field, type 2000.

Animation 1

1 In the **Velocity** toolbar, click ▦ **Animation** and choose **Player**.

You can adjust the number of frames to obtain a smooth animation of the interactive arrows. This animation visualizes very nicely that there are regions in the porous medium with both very slow and very high velocity.