

Magnetic Lens

Introduction

Scanning electron microscopes take images of samples by scanning with a high-energy beam of electrons. The subsequent electron interactions produce signals such as secondary and back-scattered electrons that contain information about the sample surface topography. Electromagnetic lenses are used to focus this electron beam down to a spot about 10 nm wide on the sample surface.

Note: This application requires the AC/DC Module and the Particle Tracing Module.

Model Definition

Particles (electrons) are released from near the bottom boundary of the simulation space and pass through a collimator. This collimator can typically be adjusted to remove stray electrons. A simple DC coil produces an axial magnetic field. This rotationally symmetric, inhomogeneous magnetic field results in non-axial electrons experiencing a radial force causing them to spiral about the axis. As they begin to spiral, they have a larger velocity component perpendicular to the mainly axial magnetic field, therefore the radius of their spiral/helical path decreases. Thus, a parallel beam of electrons entering the lens converges to a point.

If the region in which the magnetic field acts upon the electrons is sufficiently small, this coil acts as a 'thin' convex lens and the thin lens expression holds.

MODEL EQUATIONS

A simple model is set up to test the magnetic force within the Charged Particle Tracing interface. The equations solved are the equation of motion of a charged particle in a magnetic field (Lorentz force):

$$\frac{\mathrm{d}}{\mathrm{d}t}(m\mathbf{v}) = q(\mathbf{v} \times \mathbf{B})$$

where q (SI unit: C) is the particle charge, \mathbf{v} (SI unit: m/s) is the particle velocity, and \mathbf{B} (SI unit: T) is the magnetic flux density. The total work done on a particle by a magnetic field is zero.

The magnetic flux density is plotted in Figure 1. The strength of the lens depends upon the coil configuration and current. The lenses within electron microscopes are generally very strong, in some cases focusing the electron beam within the lens itself.

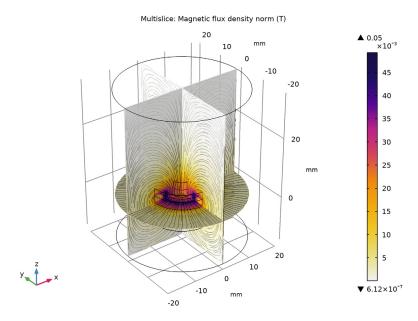


Figure 1: Plot of the magnetic flux density in the magnetic lens.

Figure 2 plots the electron trajectories as they travel through the coil. The electrons are focused at a point along the z-axis. The focal length is given by:

$$f = K \frac{V}{i^2}$$

where K is a constant based on the coil geometry and number of turns, V is the accelerating voltage and i is the coil current. The focal length increases with electron energy (that is, V) because their high velocity means they spend less time experiencing a force due the magnetic field. However, as the current increases so does the magnetic field strength, therefore the electrons spiral in tighter paths bringing the focal length closer.

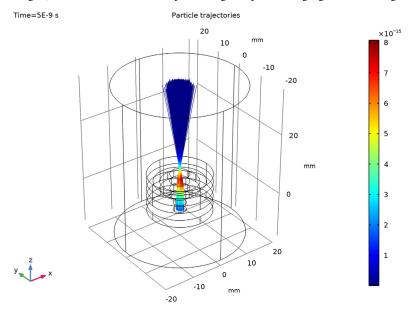


Figure 2: Plot of the electron trajectories traveling through the magnetic lens.

When charged particle beams are released, additional global variables are used to define beam properties such as the emittance and the Twiss parameters. These global variables can be used to characterize the shape of a beam and the transverse phase space distribution of the beam particles. In Figure 3 the hyperemittance is plotted along the average beam trajectory as a color expression and as a tube radius expression. The nominal trajectory reaches maximum thickness shortly after entering the lens and appears to be pinched off at the location where the beam is focused.

The ability to change the focal length of a lens is useful as it allows the focusing onto a surface in addition to adjusting the magnification. The effect of the focusing can be seen in Figure 4 which shows a Poincaré map of the particle position at three different snapshots in time. The sharpness of the cross-over can be improved using multiple lenses.

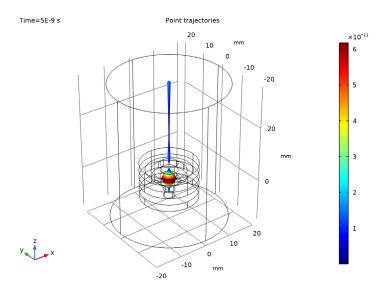


Figure 3: The nominal beam trajectory is plotted, with a color and thickness proportional to the 1-rms hyperemittance of the beam...

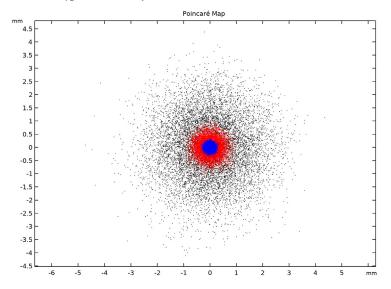


Figure 4: Poincaré maps of the particle location in the xy-plane initially (red), at the focal point of the lens (blue), and at the last time step (black).

Reference

1. M.J. Pritchard, Manipulation of Ultracold Atoms Using Magnetic and Optical Fields, PhD thesis, Durham University, September 2006, http://massey.dur.ac.uk/ resources/mjpritchard/thesis_pritchard.pdf.

Application Library path: Particle Tracing Module/ Charged_Particle_Tracing/magnetic_lens

Modeling Instructions

From the File menu, choose New.

In the **New** window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click **1** 3D.
- 2 In the Select Physics tree, select AC/DC>Electromagnetic Fields>Magnetic Fields (mf).
- 3 Click Add.
- 4 Click 🔵 Study.
- 5 In the Select Study tree, select General Studies>Stationary.
- 6 Click **Done**.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
Ic	0.32[A]	0.32 A	Coil current
Nc	1000	1000	Number of turns in coil

GEOMETRY I

The coil geometry is constructed using cylinders, and it is available as a separate file in the Application Library. Insert the prepared geometry sequence from the file. You can read the instructions for creating the geometry in the appendix.

- I In the Geometry toolbar, click Insert Sequence.
- 2 Browse to the model's Application Libraries folder and double-click the file magnetic_lens_geom_sequence.mph.

MATERIALS

Material I (mat I)

- I In the Model Builder window, under Component I (comp I) right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, locate the Material Contents section.
- 3 In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Relative permeability	mur_iso; murii = mur_iso, murij = 0	1	I	Basic
Electrical conductivity	sigma_iso; sigmaii = sigma_iso, sigmaij = 0	6e7	S/m	Basic
Relative permittivity	epsilonr_iso; epsilonrii = epsilonr_iso, epsilonrij = 0	1	I	Basic

Material 2 (mat2)

- I Right-click Materials and choose Blank Material.
- 2 Select Domain 1 only.
- 3 In the Settings window for Material, locate the Material Contents section.

4 In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Relative permeability	mur_iso; murii = mur_iso, murij = 0	1	I	Basic
Electrical conductivity	sigma_iso; sigmaii = sigma_iso, sigmaij = 0	0	S/m	Basic
Relative permittivity	epsilonr_iso; epsilonrii = epsilonr_iso, epsilonrij = 0	1	I	Basic

MAGNETIC FIELDS (MF)

Coil I

- I In the Model Builder window, under Component I (compl) right-click Magnetic Fields (mf) and choose the domain setting Coil.
- 2 Select Domain 4 only.
- 3 In the Settings window for Coil, locate the Coil section.
- 4 From the Conductor model list, choose Homogenized multiturn.
- 5 From the Coil type list, choose Circular.
- **6** Locate the **Homogenized Multiturn Conductor** section. In the N text field, type Nc.
- **7** Locate the **Coil** section. In the I_{coil} text field, type Ic.

Specify the reference edges to be used in the calculation of the current path for the circular coil. To obtain the best results, the selected edges should have a radius close to the average coil radius. In this case, select the edges created for this purpose in previous steps.

Coil Geometry 1

- I In the Model Builder window, click Coil Geometry I.
- 2 In the Settings window for Coil Geometry, locate the Edge Selection section.
- 3 Click Clear Selection.
- 4 Select Edges 22, 23, 57, and 82 only.

MESH I

Scale 1

- I In the Mesh toolbar, click A Modify and choose Mesh>Scale.
- 2 In the Settings window for Scale, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Domain.
- **4** Select Domains 2–5 only.
- **5** Locate the **Scale** section. In the **Element size scale** text field, type **0.5**.

Free Triangular I

- I In the Mesh toolbar, click A Boundary and choose Free Triangular.
- 2 Select Boundary 30 only.

Size 1

- I Right-click Free Triangular I and choose Size. Use a fine mesh on the surface where particles will be released.
- 2 In the Settings window for Size, locate the Element Size section.
- 3 From the Predefined list, choose Extremely fine.

Free Tetrahedral I

- I In the Mesh toolbar, click A Free Tetrahedral.
- 2 In the Settings window for Free Tetrahedral, click **Build All**.

STUDY I

In the **Home** toolbar, click **Compute**.

RESULTS

Cut Plane 1

- I In the Model Builder window, expand the Results>Datasets node, then click Cut Plane I.
- 2 In the Settings window for Cut Plane, locate the Plane Data section.
- 3 In the z-coordinate text field, type 0.

Multislice 1

- I In the Model Builder window, expand the Results>Magnetic Flux Density Norm (mf) node, then click Multislice 1.
- 2 In the Settings window for Multislice, locate the Multiplane Data section.
- **3** Find the **z-planes** subsection. In the **Coordinates** text field, type **0**.

- **4** Click the **Zoom Extents** button in the **Graphics** toolbar.
- 5 In the Magnetic Flux Density Norm (mf) toolbar, click Plot. Compare the resulting image to Figure 1.

ADD PHYSICS

- I In the Home toolbar, click open the Add Physics window.
- 2 Go to the Add Physics window.
- 3 In the tree, select AC/DC>Particle Tracing>Charged Particle Tracing (cpt).
- 4 Find the Physics interfaces in study subsection. In the table, clear the Solve check box for Study 1.
- **5** Click **Add to Component I** in the window toolbar.
- 6 In the Home toolbar, click and Physics to close the Add Physics window.

ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies> Time Dependent.
- **4** Find the **Physics interfaces in study** subsection. In the table, clear the **Solve** check box for Magnetic Fields (mf).
- 5 Click Add Study in the window toolbar.
- 6 In the Home toolbar, click Add Study to close the Add Study window.

GEOMETRY I

In the Model Builder window, collapse the Component I (compl)>Geometry I node.

CHARGED PARTICLE TRACING (CPT)

- I In the Model Builder window, under Component I (compl) click Charged Particle Tracing (cpt).
- 2 In the Settings window for Charged Particle Tracing, locate the Domain Selection section.
- 3 Click Clear Selection.
- 4 Select Domain 1 only.

Particle Properties 1

In the Model Builder window, under Component I (compl)>Charged Particle Tracing (cpt) click Particle Properties I.

- 2 In the Settings window for Particle Properties, locate the Particle Species section.
- 3 From the Particle species list, choose Electron.

You need to provide the forces acting on the particles; in this case, the magnetic (Lorentz) force.

Magnetic Force 1

- I In the Physics toolbar, click **Domains** and choose Magnetic Force.
- 2 Select Domain 1 only.
- 3 In the Settings window for Magnetic Force, locate the Magnetic Force section.
- 4 From the B list, choose Magnetic flux density (mf).

Particle Beam 1

- I In the Physics toolbar, click **Boundaries** and choose Particle Beam.
- 2 Select Boundary 30 only.
- 3 In the Settings window for Particle Beam, locate the Initial Position section.
- 4 In the N text field, type 10000.
- **5** Locate the **Initial Transverse Velocity** section. In the ε_{rms} text field, type 0.1[um].
- **6** Locate the **Initial Longitudinal Velocity** section. In the E text field, type 0.5 [keV].

STUDY 2

Step 1: Time Dependent

- I In the Model Builder window, under Study 2 click Step 1: Time Dependent.
- 2 In the Settings window for Time Dependent, click to expand the Values of Dependent Variables section.
- 3 Find the Values of variables not solved for subsection. From the Settings list, choose User controlled.
- **4** From the **Method** list, choose **Solution**.
- 5 From the Study list, choose Study I, Stationary.
- 6 Locate the Study Settings section. Click Range.
- 7 In the Range dialog box, choose Number of values from the Entry method list.
- 8 In the **Stop** text field, type 5e-9.
- 9 In the Number of values text field, type 50.
- 10 Click Replace.
- II In the **Home** toolbar, click **Compute**.

RESULTS

Particle Trajectories (cpt)

In the Model Builder window, expand the Particle Trajectories (cpt) node.

Particle Trajectories 1

- I In the Model Builder window, expand the Results>Particle Trajectories (cpt)> Particle Trajectories I node, then click Particle Trajectories I.
- 2 In the Settings window for Particle Trajectories, locate the Coloring and Style section.
- **3** Find the **Line style** subsection. From the **Type** list, choose **Line**.
- **4** Find the **Point style** subsection. From the **Type** list, choose **None**.

Color Expression 1

- I In the Model Builder window, click Color Expression I.
- 2 In the Settings window for Color Expression, locate the Expression section.
- 3 In the Expression text field, type sqrt(cpt.Ftx^2+cpt.Fty^2+cpt.Ftz^2).
- 4 In the Particle Trajectories (cpt) toolbar, click Plot.
- 5 Click the Toom Extents button in the Graphics toolbar. Compare the resulting image to Figure 2.

Now observe the beam hyperemittance along the nominal beam trajectory.

Average Beam Position and Hyperemittance

- I In the Model Builder window, under Results click Average Beam Position (cpt).
- 2 In the Settings window for 3D Plot Group, type Average Beam Position and Hyperemittance in the Label text field.

Point Trajectories I

- I In the Model Builder window, expand the Average Beam Position and Hyperemittance node, then click Point Trajectories 1.
- 2 In the Settings window for Point Trajectories, locate the Coloring and Style section.
- **3** Find the **Line style** subsection. From the **Type** list, choose **Tube**.
- 4 Click **Replace Expression**.
- 5 From the menu, choose Component I (compl)>Charged Particle Tracing> Beam properties>cpt.elhrms - I-RMS beam hyperemittance - m2.
- 6 Select the Radius scale factor check box.
- 7 In the associated text field, type 4E10.
- 8 From the Interpolation list, choose Uniform.

9 In the **Average Beam Position and Hyperemittance** toolbar, click **Plot**. Compare the resulting image to Figure 3.

Now construct a **Poincaré Map** to visualize the radial distribution of particles initially, at the focal point, and at the exit of the modeling domain.

Cut Plane 4

- I In the Results toolbar, click Cut Plane.
- 2 In the Settings window for Cut Plane, locate the Plane Data section.
- 3 From the Plane list, choose xy-planes.
- 4 In the **z-coordinate** text field, type -6.
- 5 Locate the Data section. From the Dataset list, choose Particle 1.

Cut Plane 5

- I Right-click Cut Plane 4 and choose Duplicate.
- 2 In the Settings window for Cut Plane, locate the Plane Data section.
- **3** In the **z-coordinate** text field, type 7.

Cut Plane 6

- I Right-click Cut Plane 5 and choose Duplicate.
- 2 In the Settings window for Cut Plane, locate the Plane Data section.
- 3 In the z-coordinate text field, type 34.

Poincaré Maps

- I In the Results toolbar, click **2D Plot Group**.
- 2 In the Settings window for 2D Plot Group, type Poincaré Maps in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Particle 1.
- 4 Click to expand the **Title** section. From the **Title type** list, choose **Manual**.
- 5 In the **Title** text area, type Poincaré Map.

Poincaré Map I

- I In the Poincaré Maps toolbar, click More Plots and choose Poincaré Map.
- 2 In the Settings window for Poincaré Map, locate the Data section.
- 3 From the Cut plane list, choose Cut Plane 6.
- 4 Locate the Coloring and Style section. From the Color list, choose Black.
- **5** Click the **Zoom Extents** button in the **Graphics** toolbar.

Poincaré Mab 2

- I Right-click Poincaré Map I and choose Duplicate.
- 2 In the Settings window for Poincaré Map, locate the Data section.
- 3 From the Cut plane list, choose Cut Plane 4.
- 4 Locate the Coloring and Style section. From the Color list, choose Red.

Poincaré Mab 3

- I Right-click Poincaré Map 2 and choose Duplicate.
- 2 In the Settings window for Poincaré Map, locate the Data section.
- 3 From the Cut plane list, choose Cut Plane 5.
- 4 Locate the Coloring and Style section. From the Color list, choose Blue.
- 5 In the Poincaré Maps toolbar, click **Plot**.
- 6 Click the **Zoom Extents** button in the **Graphics** toolbar. Compare the resulting image to Figure 4.

Appendix A - Geometry Instructions

ADD COMPONENT

In the **Home** toolbar, click **Add Component** and choose **3D**.

GEOMETRY I

- I In the Settings window for Geometry, locate the Units section.
- 2 From the Length unit list, choose mm.

Cylinder I (cyl1)

- I In the Geometry toolbar, click Cylinder.
- 2 In the Settings window for Cylinder, locate the Size and Shape section.
- **3** In the **Radius** text field, type 10.
- 4 In the Height text field, type 2.5.

Cylinder 2 (cyl2)

- I In the Geometry toolbar, click (Cylinder.
- 2 In the Settings window for Cylinder, locate the Size and Shape section.
- 3 In the Radius text field, type 6.

- 4 In the Height text field, type 2.5.
- 5 Click | Build Selected.

Cylinder 3 (cyl3)

- I In the Model Builder window, under Component I (compl)>Geometry I right-click

 Cylinder I (cyll) and choose Duplicate.
- 2 In the Settings window for Cylinder, locate the Position section.
- 3 In the z text field, type -7.5.

Cylinder 4 (cyl4)

- I In the Geometry toolbar, click (Cylinder.
- 2 In the Settings window for Cylinder, locate the Size and Shape section.
- 3 In the Radius text field, type 2.
- 4 In the **Height** text field, type 2.5.
- **5** Locate the **Position** section. In the **z** text field, type -7.5.

Cylinder 5 (cyl5)

- I Right-click Cylinder I (cyll) and choose Duplicate.
- 2 In the Settings window for Cylinder, locate the Position section.
- 3 In the z text field, type -2.5.

Cylinder 6 (cyl6)

- I In the Geometry toolbar, click (Cylinder.
- 2 In the Settings window for Cylinder, locate the Size and Shape section.
- 3 In the Radius text field, type 3.
- 4 In the **Height** text field, type 2.5.
- **5** Locate the **Position** section. In the **z** text field, type -2.5.

Cylinder 7 (cyl7)

- I Right-click Cylinder I (cyll) and choose Duplicate.
- 2 In the Settings window for Cylinder, locate the Position section.
- 3 In the z text field, type 2.5.

Cylinder 8 (cyl8)

- I In the **Geometry** toolbar, click **Cylinder**.
- 2 In the Settings window for Cylinder, locate the Size and Shape section.
- 3 In the Radius text field, type 3.

- 4 In the Height text field, type 2.5.
- 5 Locate the **Position** section. In the z text field, type 2.5.

Cylinder 9 (cyl9)

- I In the Geometry toolbar, click Cylinder.
- 2 In the Settings window for Cylinder, locate the Size and Shape section.
- 3 In the Radius text field, type 20.
- 4 In the Height text field, type 50.
- 5 Locate the **Position** section. In the **z** text field, type -15.

Difference I (dif1)

- I In the Geometry toolbar, click Booleans and Partitions and choose Difference.
- 2 Select the objects cyll, cyl3, cyl5, and cyl7 only.
- 3 In the Settings window for Difference, locate the Difference section.
- **4** Find the **Objects to subtract** subsection. Select the **Activate Selection** toggle button.
- 5 Select the objects cyl2, cyl4, cyl6, and cyl8 only.
- 6 Click **Pauld Selected**.
- 7 Click the Go to Default View button in the Graphics toolbar.

Work Plane I (wbl)

- I In the Geometry toolbar, click Work Plane.
- 2 Click the Wireframe Rendering button in the Graphics toolbar.
- 3 In the Settings window for Work Plane, locate the Plane Definition section.
- 4 From the Plane type list, choose Face parallel.
- 5 On the object dif1, select Boundary 3 only.
- 6 Click Show Work Plane.

Work Plane I (wp I)>Plane Geometry

Click the Zoom Extents button in the Graphics toolbar.

Work Plane I (wbl)>Circle I (cl)

- I In the Work Plane toolbar, click (Circle.
- 2 In the Settings window for Circle, locate the Size and Shape section.
- 3 In the Radius text field, type 2.
- 4 Click | Build Selected.

Last, create a circular edge to be used in the **Coil** feature as a reference edge.

Work Plane 2 (wp2)

- I In the Model Builder window, right-click Geometry I and choose Work Plane.
- 2 In the Settings window for Work Plane, locate the Plane Definition section.
- 3 From the Plane type list, choose Face parallel.
- 4 On the object dif1, select Boundary 13 only.
- 5 Click Show Work Plane.

Work Plane 2 (wp2)>Circle 1 (c1)

- I In the Work Plane toolbar, click Circle.
- 2 In the Settings window for Circle, locate the Object Type section.
- **3** From the **Type** list, choose **Curve**.
- 4 Locate the Size and Shape section. In the Radius text field, type 8.
- 5 In the Work Plane toolbar, click **Build All**.