

Impact Analysis of a Golf Ball

Introduction

The outcome of a golf stroke is to a large extent influenced by the characteristics of the golf ball, including both its aerodynamics and mechanical properties. The latter, for example, determine how efficiently energy is transferred form the club head to the ball during the swing. The transfer of energy is largely governed by the stiffness of the ball's core material, or in golf nomenclature, the "compression" of the ball. How well energy is transferred during the impact plays a key role in how far the ball will fly. The "backspin" is another key aspect of the golf stoke influenced by the mechanical properties of the ball. A high spin rate increases the lift, lengthening the carry distance of the shot. Also, increasing the backspin makes the ball stop more rapidly when landing. The stiffness of the cover and core materials plays an important role for the friction and spinning effects. A ball with a thin cover and a soft core will deform more when it comes in contact with the club face, thus generating more friction and a higher spin rate.

This example studies the mechanical impact of a club on a golf ball. The contact between the two parts is modeled using a viscous penalty formulation in order to stabilize this dynamic event. To properly model large deformations, the golf ball is defined using a hyperelastic material model. Additionally, the core material is viscoelastic, which causes dissipation of the elastic energy transfered by the impact. Results are compared to typical golf metrics such as ball speed and spin rate.

Model Definition

The model studies how momentum and energy are transferred form the club to the golf ball during the swing. The simulation focuses on the impact between the two objects, and it only looks at a time period of 2 ms.

Figure 1 shows the geometry of the club and golf ball. The dimensions of the club represent a typical 7 iron with a loft equal to 34°. The club head is approximately 9 cm wide, 6 cm high at the toe, and 3.5 cm high close to the shaft. The shaft is only partially included to simplify the geometry. It is assumed that the club has a dynamic loft of 22° at impact. The dynamic loft is the angle of the club face from the vertical plane at impact.

The the ball's diameter is 42.67 mm in accordance with the rules of golf (Ref. 1). A three piece design is used: an inner core of 34.67 mm in diameter, a 3 mm thick outer core (or mantle), and a 1 mm thick cover. The outer surface is also covered with 362 dimples.

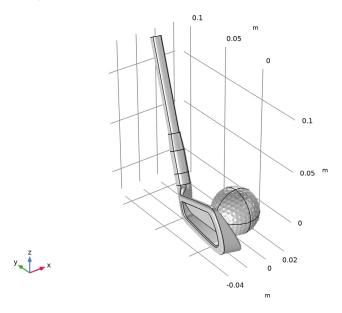


Figure 1: Model geometry

MATERIAL MODELS AND PROPERTIES

The golf club is assumed to be made of steel, with a density of 7850 kg/m³, Young's modulus of 200 GPa, and Poisson's ration of 0.3.

According to Ref. 1, the golf ball must be constructed entirely form elastomeric materials, that is, viscoelastic materials with a low stiffness. All parts of the ball are thus described using a Neo-Hookean hyperelastic material model. The cover is assumed to be compressible, while both inner and outer core are considered nearly incompressible and modeled using a mixed formulation. The Hartmann-Neff volumetric strain energy density is used with a prescribed bulk modulus of 1 GPa in order to penalize volumetric deformations. The two parts of the core are furthermore considered to be viscoelastic, and thus also include a large strain Generalized Maxwell model with three branches.

Mechanical properties of the materials used in golf balls are propriety and hard to find in the literature. Hence, the material properties summarized in Table 1 are only realistic estimates. The density is, for example, taken so that the total mass of the ball is equal to

45.93 g in accordance with Ref. 1. The other material properties have been tuned to give realistic results.

TABLE I: MATERIAL PROPERTIES OF THE GOLE BALL

Property	Symbol	Unit	Cover	Mantle	Inner core
Density	ρ	kg/m ³	1145	1145	1145
Lamé parameters	λ	MPa	1500	N/A	N/A
	μ	MPa	250	6	12
Energy factors	β_{v1}	I	N/A	0.26	0.26
	β_{v2}	I	N/A	0.19	0.19
	β_{v3}	I	N/A	0.22	0.22
Relaxation times	τ_{v1}	μs	N/A	10	10
	$\tau_{\mathrm{v}2}$	μs	N/A	100	100
	$\tau_{\mathrm{v}3}$	μs	N/A	1000	1000

CONSTRAINTS AND CONTACT CONDITIONS

The golf club impacts the ball with a velocity equal to 90 mph in a slightly downward direction, defined by an attack angle of -4.3° from the xy-plane. The end of the shaft is constrained to this velocity throughout the simulation. Both the velocity and the attack angle are rough estimates for a professional male golf player when using a 7 iron.

The interaction between the club and the golf ball is modeled using a contact condition. Dynamic effects are important since this is a time-dependent simulation of an impact event, and linear momentum and energy must be consistent during the contact interaction. To ensure this and to stabilize the contact condition, a viscous penalty formulation is added for the pressure contact. Friction is also important to properly capture the interaction between the club and the ball; since it is the effect of friction that causes the golf ball to spin after it is hit by the club head. A Coulomb friction model is added with a friction coefficient equal to 0.15.

Results and Discussion

Table 2 presents some common metrics used in golf to measure the performance of the player and the equipment. Here, the club speed and attack angle are input data to the simulation. The remaining metrics are computed by the COMSOL Multiphysics model. The *launch angle* is the angle of the ball relative to the ground after impact, and the *smash* factor is the ball speed divided by the club speed. Given the input parameters, all

computed metrics are realistic and close to typical values reported for an average professional male golf player.

TABLE 2: METRICS OF THE CLUB AND GOLF BALL.

Club speed (mph)	Attack angle (deg)	Launch angle (deg)	Ball speed (mph)	Smash factor	Spin rate (rpm)
90	-4.3	17.4	116.1	1.29	6113

Figure 2 shows four snapshots of the simulation before, during, and after the impact. One can clearly see the large deformation of the golf ball when hit by the club head, increasing the contact area between the ball and the club face. This is even more visible when looking at the cut-through image in Figure 3, that also shows the strain distribution inside the ball. Figure 3 shows the minimum principal strain which is in the order of -20% in large parts of the ball.

It is interesting to look at the velocity of the club and ball during the simulation in order to study the kinematics of the problem in detail. Figure 4 shows the velocity magnitude and how momentum is transferred form the club head to the ball during the impact. Due to the flexibility of the shaft, the velocity of the club head decreases slightly during and after the impact, even though the velocity of the shaft is prescribed to a constant value.

Figure 5 shows the variation of the total elastic and kinetic energy of the golf ball during the simulation. The duration of the impact is clearly visible as a peak in both the elastic and kinetic energy content. An interesting observation is how effectively the viscoelastic properties of the core damp out the elastic energy after the impact. In contrast, the kinetic energy reaches a constant value once the ball departures from the club face.



Figure 2: Snapshots of the club and golf ball during the simulation. From top to bottom, the timings are 0 ms, 0.15 ms, 0.30 ms and 0.45 ms.

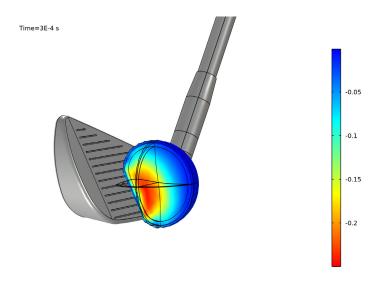


Figure 3: Deformation of the golf ball and distribution of the third principal (compressive) strain in the interior part of the ball at $0.3~\rm ms$.

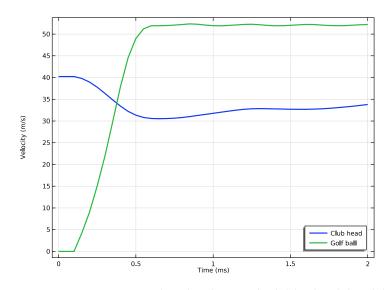


Figure 4: Average magnitude of the velocity in the club head and the golf ball.

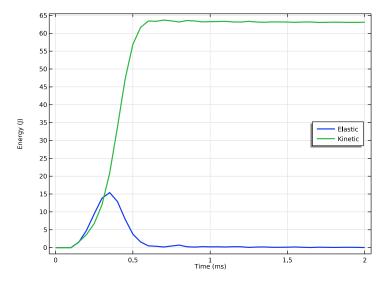


Figure 5: Total elastic and kinetic energy in the golf ball.

Notes About the COMSOL Implementation

The error estimates used by the automatic time-step control will force time steps small enough to resolve the wave propagation within the solid, which is not of primary interest in this analysis. The automatic time-step control will often lead to unnecessarily small time steps, and longer computational time. Therefore, it is often a good practice to use a manual time-step control when the focus is in the kinematics of the contact phenomenon.

The spin rate of the golf ball is determined by adding an Average Rotation node to the model. This node makes it possible to compute average rotation for a set of points in a least-squares sense for rotations that are arbitrarily large.

Reference

1. The Equipment Rules, 1st edition, The R&A and USGA, 2019.

Application Library path: Nonlinear_Structural_Materials_Module/ Viscoelasticity/golf ball impact

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click **3D**.
- 2 In the Select Physics tree, select Structural Mechanics>Solid Mechanics (solid).
- 3 Click Add.
- 4 Click Study.
- 5 In the Select Study tree, select General Studies>Time Dependent.
- 6 Click M Done.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
loft	34[deg]	0.59341 rad	Club head loft
attackAngle	-4.3[deg]	-0.075049 rad	Attack angle
dynLoft	22[deg]	0.38397 rad	Dynamic loft
vel	90[mph]	40.234 m/s	Club head speed
velx	cos(attackAngle)*vel	40.12 m/s	Club head velocity, x component
velz	sin(attackAngle)*vel	-3.0167 m/s	Club head velocity, z component

GEOMETRY I

Import I (impl)

- I In the **Home** toolbar, click **Import**.
- 2 In the Settings window for Import, locate the Import section.
- 3 Click Browse.
- **4** Browse to the model's Application Libraries folder and double-click the file golf ball impact.mphbin.
- 5 Click Import.

Rotate the golf club to the correct dynamic loft at impact.

Rotate I (rot1)

- I In the Geometry toolbar, click Transforms and choose Rotate.
- 2 Select the object impl(1) only.
- 3 In the Settings window for Rotate, locate the Rotation section.
- 4 From the Axis type list, choose y-axis.
- 5 In the Angle text field, type loft-dynLoft+attackAngle.

Form Union (fin)

- I In the Model Builder window, under Component I (compl)>Geometry I click Form Union (fin).
- 2 In the Settings window for Form Union/Assembly, locate the Form Union/Assembly section.
- 3 From the Action list, choose Form an assembly.
- 4 In the Geometry toolbar, click **Build All**.

Create selections to be used in the physics and plot creation.

DEFINITIONS

Club Head

- I In the Model Builder window, expand the Component I (compl)>Definitions node.
- 2 Right-click Definitions and choose Selections>Explicit.
- 3 In the Settings window for Explicit, type Club Head in the Label text field.
- 4 Select Domains 1 and 2 only.

Club Shaft

I In the **Definitions** toolbar, click **\(\frac{1}{2} \) Explicit**.

- 2 In the Settings window for Explicit, type Club Shaft in the Label text field.
- **3** Select Domains 5, 6, 8–12, and 14 only.

Club Head and Shaft, Boundary

- I In the **Definitions** toolbar, click **Adjacent**.
- 2 In the Settings window for Adjacent, type Club Head and Shaft, Boundary in the Label text field.
- 3 Locate the Input Entities section. Under Input selections, click + Add.
- 4 In the Add dialog box, in the Input selections list, choose Club Head and Club Shaft.
- 5 Click OK.

Club Ferrule

- I In the **Definitions** toolbar, click **\(\bigcap_{\bigcap} \) Explicit**.
- 2 In the Settings window for Explicit, type Club Ferrule in the Label text field.
- **3** Select Domains 3, 4, 7, and 13 only.

Club Ferrule, Boundary

- I In the **Definitions** toolbar, click **\bigcip_a Adjacent**.
- 2 In the Settings window for Adjacent, type Club Ferrule, Boundary in the Label text field.
- 3 Locate the Input Entities section. Under Input selections, click + Add.
- 4 In the Add dialog box, select Club Ferrule in the Input selections list.
- 5 Click OK.

Club

- I In the **Definitions** toolbar, click **Union**.
- 2 In the Settings window for Union, type Club in the Label text field.
- 3 Locate the Input Entities section. Under Selections to add, click + Add.
- 4 In the Add dialog box, in the Selections to add list, choose Club Head, Club Shaft, and Club Ferrule.
- 5 Click OK.

Golf Ball

- I In the **Definitions** toolbar, click **\(\frac{1}{2} \) Explicit**.
- 2 In the Settings window for Explicit, type Golf Ball in the Label text field.
- 3 Click the Select Box button in the Graphics toolbar.

4 Select Domains 15–38 only.

Cover

- I In the **Definitions** toolbar, click **\(\frac{1}{2} \) Explicit**.
- 2 In the Settings window for Explicit, type Cover in the Label text field.
- **3** Select Domains 15–18, 27, 28, 33, and 38 only.

Mantle

- I In the **Definitions** toolbar, click **\(\frac{1}{2} \) Explicit**.
- 2 In the Settings window for Explicit, type Mantle in the Label text field.
- **3** Select Domains 19–22, 29, 30, 34, and 37 only.

Inner Core

- I In the **Definitions** toolbar, click Difference.
- 2 In the Settings window for Difference, type Inner Core in the Label text field.
- 3 Locate the Input Entities section. Under Selections to add, click + Add.
- 4 In the Add dialog box, select Golf Ball in the Selections to add list.
- 5 Click OK.
- 6 In the Settings window for Difference, locate the Input Entities section.
- 7 Under Selections to subtract, click + Add.
- 8 In the Add dialog box, in the Selections to subtract list, choose Cover and Mantle.
- 9 Click OK.

Core

- I In the **Definitions** toolbar, click **Union**.
- 2 In the Settings window for Union, type Core in the Label text field.
- 3 Locate the Input Entities section. Under Selections to add, click + Add.
- 4 In the Add dialog box, in the Selections to add list, choose Mantle and Inner Core.
- 5 Click OK.

Club Face

- I In the **Definitions** toolbar, click 🔓 **Explicit**.
- 2 In the Settings window for Explicit, locate the Input Entities section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 In the Label text field, type Club Face.
- **5** Select Boundary 5 only.

Grooves

- I In the **Definitions** toolbar, click **\(\bigcap_{\bigcap} \) Explicit**.
- 2 In the Settings window for Explicit, type Grooves in the Label text field.
- 3 Locate the Input Entities section. From the Geometric entity level list, choose Boundary.
- **4** Select Boundaries 8–32, 34–48, 50–54, 56–59, 63, 65–69, 76–79, 85, 94–97, and 103 only.

Polished Steel

- I In the **Definitions** toolbar, click **Difference**.
- 2 In the Settings window for Difference, type Polished Steel in the Label text field.
- 3 Locate the Geometric Entity Level section. From the Level list, choose Boundary.
- 4 Locate the Input Entities section. Under Selections to add, click + Add.
- 5 In the Add dialog box, select Club Head and Shaft, Boundary in the Selections to add list.
- 6 Click OK.
- 7 In the Settings window for Difference, locate the Input Entities section.
- 8 Under Selections to subtract, click + Add.
- 9 In the Add dialog box, in the Selections to subtract list, choose Club Face and Grooves.
- IO Click OK.

Contact Pair I (b1)

- I In the **Definitions** toolbar, click **Pairs** and choose **Contact Pair**.
- 2 In the Settings window for Pair, locate the Source Boundaries section.
- 3 From the Selection list, choose Club Face.
- 4 Locate the Destination Boundaries section. Select the Activate Selection toggle button.
- **5** Select Boundaries 136, 137, 139, and 141 only.

Integration | (intob |)

- I In the Definitions toolbar, click // Nonlocal Couplings and choose Integration.
- 2 In the Settings window for Integration, locate the Source Selection section.
- 3 From the Selection list, choose Golf Ball.
- 4 Locate the Advanced section. From the Frame list, choose Material (X, Y, Z).

Average I (aveob I)

- I In the **Definitions** toolbar, click Monlocal Couplings and choose Average.
- 2 In the Settings window for Average, locate the Source Selection section.

- 3 From the Selection list, choose Club Head.
- 4 Locate the Advanced section. From the Frame list, choose Material (X, Y, Z).

Average 2 (aveob2)

- I In the **Definitions** toolbar, click Nonlocal Couplings and choose Average.
- 2 In the Settings window for Average, locate the Source Selection section.
- 3 From the Selection list, choose Golf Ball.
- 4 Locate the Advanced section. From the Frame list, choose Material (X, Y, Z).

SOLID MECHANICS (SOLID)

Hyperelastic Material I

- I In the Model Builder window, under Component I (compl) right-click Solid Mechanics (solid) and choose Material Models>Hyperelastic Material.
- 2 In the Settings window for Hyperelastic Material, locate the Domain Selection section.
- **3** From the **Selection** list, choose **Cover**.

Hyperelastic Material 2

- I In the Physics toolbar, click **Domains** and choose Hyperelastic Material.
- 2 In the Settings window for Hyperelastic Material, locate the Domain Selection section.
- **3** From the **Selection** list, choose **Core**.
- 4 Locate the Hyperelastic Material section. From the Compressibility list, choose Nearly incompressible material, Hartmann-Neff volumetric strain energy.
- **5** In the κ text field, type 1[GPa].

Viscoelasticity I

- I In the Physics toolbar, click 🕞 Attributes and choose Viscoelasticity.
- 2 In the Settings window for Viscoelasticity, locate the Viscoelasticity Model section.
- 3 Click + Add.
- 4 Click + Add.
- **5** In the table, enter the following settings:

Branch	Energy factor (I)	Relaxation time (s)
1	0.26	1e-5
2	0.19	1e-4
3	0.22	1e-3

Initial Values 2

- I In the Physics toolbar, click **Domains** and choose Initial Values.
- 2 In the Settings window for Initial Values, locate the Domain Selection section.
- **3** From the **Selection** list, choose **Club**.
- **4** Locate the **Initial Values** section. Specify the $\partial \mathbf{u}/\partial t$ vector as

velx	Χ
0	Υ
velz	Z

Prescribed Displacement 1

- I In the Physics toolbar, click **Boundaries** and choose **Prescribed Displacement**.
- **2** Select Boundaries 132–135 only.
- 3 In the Settings window for Prescribed Displacement, locate the Prescribed Displacement section.
- 4 Select the Prescribed in x direction check box.
- 5 Select the Prescribed in y direction check box.
- 6 Select the Prescribed in z direction check box.
- **7** In the u_{0x} text field, type velx*t.
- **8** In the u_{0z} text field, type velz*t.

Contact I

- I In the **Physics** toolbar, click **Pairs** and choose **Contact**.
- 2 In the Settings window for Contact, locate the Pair Selection section.
- 3 Under Pairs, click + Add.
- 4 In the Add dialog box, select Contact Pair I (pI) in the Pairs list.
- 5 Click OK.
- 6 In the Settings window for Contact, locate the Contact Method section.
- 7 From the Formulation list, choose Penalty, dynamic.
- 8 Locate the Contact Pressure Penalty Factor section. From the Penalty factor control list, choose Viscous only.
- **9** In the τ_n text field, type .025[ms].

Friction 1

I In the Physics toolbar, click **Attributes** and choose Friction.

- 2 In the Settings window for Friction, locate the Friction Parameters section.
- 3 In the μ text field, type 0.15.

Add an Average Rotation node to compute typical golf metrics.

Average Rotation 1

- I In the Physics toolbar, click A Global and choose Average Rotation.
- **2** Select Points 158, 161, 164, 166, 169, and 172 only.
- 3 In the Settings window for Average Rotation, locate the Center of Rotation section.
- 4 From the list, choose Centroid of selected entities.
- **5** From the **Entity level** list, choose **Point**.
- **6** Locate the **Rotation Model** section. From the list, choose **Finite rotations**.

Center of Rotation: Point 1

- I In the Model Builder window, click Center of Rotation: Point I.
- **2** Select Point 165 only.

MATERIALS

Club Head

- I In the Model Builder window, under Component I (compl) right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type Club Head in the Label text field.
- 3 Locate the Geometric Entity Selection section. From the Selection list, choose Club.
- **4** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	Е	200e9	Pa	Basic
Poisson's ratio	nu	0.3	I	Basic
Density	rho	7850	kg/m³	Basic

Set material appearance data for use in plot creation.

5 Click to expand the Appearance section. From the Material type list, choose Steel.

Cover

- I Right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type Cover in the Label text field.
- 3 Locate the Geometric Entity Selection section. From the Selection list, choose Cover.

4 Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Lamé parameter λ	lambLame	1.5e9	N/m²	Lamé parameters
Lamé parameter μ	muLame	0.2e9	N/m²	Lamé parameters
Density	rho	1145	kg/m³	Basic

Mantle

- I Right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type Mantle in the Label text field.
- 3 Locate the Geometric Entity Selection section. From the Selection list, choose Mantle.
- **4** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Lamé parameter μ	muLame	6e6	N/m²	Lamé parameters
Density	rho	1145	kg/m³	Basic

5 Click to expand the Appearance section. From the Color list, choose Blue.

Inner Core

- I Right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type Inner Core in the Label text field.
- 3 Locate the Geometric Entity Selection section. From the Selection list, choose Inner Core.
- **4** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Lamé parameter μ	muLame	12e6	N/m²	Lamé parameters
Density	rho	1145	kg/m³	Basic

5 Click to expand the Appearance section. From the Color list, choose Magenta.

MESH I

- I In the Model Builder window, under Component I (compl) click Mesh I.
- 2 In the Settings window for Mesh, locate the Mesh Settings section.
- **3** From the Sequence type list, choose User-controlled mesh.

Size

I In the Model Builder window, under Component I (compl)>Mesh I click Size.

- 2 In the Settings window for Size, locate the Element Size section.
- **3** Click the **Custom** button.
- 4 Locate the Element Size Parameters section. In the Maximum element size text field, type
- 5 In the Minimum element size text field, type 0.002.
- 6 In the Maximum element growth rate text field, type 1.6.
- 7 In the Curvature factor text field, type 0.3.
- 8 In the Resolution of narrow regions text field, type 0.6.

Size 1

- I In the Model Builder window, right-click Mesh I and choose Size.
- 2 Right-click Size I and choose Move Up.
- 3 In the Settings window for Size, locate the Geometric Entity Selection section.
- 4 From the Geometric entity level list, choose Domain.
- 5 From the Selection list, choose Golf Ball.
- 6 Locate the **Element Size** section. Click the **Custom** button.
- 7 Locate the Element Size Parameters section. Select the Minimum element size check box.
- 8 In the associated text field, type 0.0012.
- 9 Select the Maximum element growth rate check box.
- **IO** In the associated text field, type 1.4.

Mapped I

- I In the Mesh toolbar, click A Boundary and choose Mapped.
- **2** Select Boundaries 92, 93, 110, 128, and 132–135 only.

Distribution I

- I Right-click Mapped I and choose Distribution.
- **2** Select Edges 183, 184, 212, 242, 249, 250, 254, and 258 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 3.

Swebt 1

- I In the Mesh toolbar, click A Swept.
- 2 In the Settings window for Swept, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.

4 Select Domains 3–14 only.

Free Quad I

- I In the Mesh toolbar, click A Boundary and choose Free Quad.
- 2 Select Boundary 87 only.

Swebt 2

- I In the Mesh toolbar, click A Swept.
- 2 In the Settings window for Swept, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 Select Domain 2 only.
- 5 Click **Build All**.

STUDY I

Step 1: Time Dependent

- I In the Model Builder window, under Study I click Step I: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- 3 In the Output times text field, type 2e-3.

Modify the time-dependent solver to use a manual time step control.

Solution I (soll)

- I In the Study toolbar, click Show Default Solver.
- 2 In the Model Builder window, expand the Solution I (soll) node, then click Time-Dependent Solver I.
- 3 In the Settings window for Time-Dependent Solver, locate the General section.
- 4 From the Times to store list, choose Steps taken by solver.
- 5 In the Store every Nth step text field, type 2.
- 6 Click to expand the Time Stepping section. From the Steps taken by solver list, choose Manual.
- 7 In the Time step text field, type 2.5e-5.

Increase the number of allowed nonlinear iterations and use a stricter tolerance.

- 8 In the Model Builder window, expand the Study I>Solver Configurations> Solution I (soll)>Time-Dependent Solver I node, then click Fully Coupled I.
- 9 In the Settings window for Fully Coupled, click to expand the Method and Termination section.

10 In the Maximum number of iterations text field, type 25.

II In the Tolerance factor text field, type 0.1.

Generate datasets and default plots.

12 In the Study toolbar, click $\underset{t=0}{\cup}$ Get Initial Value.

RESULTS

Strain (solid)

- I In the Settings window for 3D Plot Group, type Strain (solid) in the Label text field.
- 2 Locate the Plot Settings section. From the Frame list, choose Spatial (x, y, z).
- 3 Click to expand the Selection section. From the Geometric entity level list, choose Domain.
- **4** Select Domains 17, 18, 21, 22, 25, 26, and 33–38 only.

Surface I

- I In the Model Builder window, expand the Strain (solid) node, then click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type solid.ep3.
- 4 Locate the Coloring and Style section. Select the Reverse color table check box.
- 5 Click to expand the Quality section. From the Smoothing list, choose Everywhere.

Surface 2

- I Right-click Results>Strain (solid)>Surface I and choose Duplicate.
- 2 In the Settings window for Surface, click to expand the Title section.
- **3** From the **Title type** list, choose **None**.

Material Appearance 1

Right-click Surface 2 and choose Material Appearance.

STUDY I

Step 1: Time Dependent

- I In the Settings window for Time Dependent, click to expand the Results While Solving section.
- **2** Select the **Plot** check box.
- 3 From the Update at list, choose Time steps taken by solver.

4 In the Study toolbar, click = Compute.

Create a material rendering plot and make an animation.

RESULTS

Material Rendering

- I In the Home toolbar, click **Add Plot Group** and choose **3D Plot Group**.
- 2 In the Settings window for 3D Plot Group, type Material Rendering in the Label text field.
- 3 Locate the Plot Settings section. Clear the Plot dataset edges check box.

Golf Ball

- I Right-click Material Rendering and choose Surface.
- 2 In the Settings window for Surface, type Golf Ball in the Label text field.
- **3** Locate the **Expression** section. In the **Expression** text field, type 1.
- 4 Locate the Title section. From the Title type list, choose None.

Deformation I

- I Right-click Golf Ball and choose Deformation.
- 2 In the Settings window for Deformation, locate the Scale section.
- 3 Select the Scale factor check box.
- 4 In the associated text field, type 1.

Selection 1

- I In the Model Builder window, right-click Golf Ball and choose Selection.
- **2** Select Boundaries 136, 137, 161, and 163 only.

Image I

- I Right-click Golf Ball and choose Image.
- 2 In the Settings window for Image, locate the File section.
- 3 Click Browse.
- **4** Browse to the model's Application Libraries folder and double-click the file golf ball impact logo.png.
- **5** Locate the Mapping section. From the Mapping list, choose Planar.
- 6 From the Plane type list, choose xz-plane.
- 7 Find the Size subsection. In the Width text field, type 0.03.
- 8 Find the Anchor point subsection. In the X text field, type -0.015.

- 9 In the Y text field, type -0.03.
- **IO** In the **Z** text field, type -0.002.
- II Find the Tiling subsection. From the Extrapolation list, choose Clamp to edge.

Material Appearance 1

- I Right-click Golf Ball and choose Material Appearance.
- 2 In the Settings window for Material Appearance, locate the Appearance section.
- 3 From the Material list, choose Cover (mat2).
- 4 Locate the Color section. Select the Use the image's color check box.

Golf Ball I

- I Right-click Golf Ball and choose Duplicate.
- 2 In the Settings window for Surface, click to expand the Inherit Style section.
- 3 From the Plot list, choose Golf Ball.

Selection 1

- I In the Model Builder window, expand the Golf Ball I node, then click Selection I.
- 2 In the Settings window for Selection, locate the Selection section.
- **3** Select the **Activate Selection** toggle button.
- **4** Select Boundaries 139, 141, 177, and 193 only.

Image I

- I In the Model Builder window, click Image I.
- 2 In the Settings window for Image, locate the Mapping section.
- 3 From the Plane type list, choose zx-plane.
- 4 Find the Anchor point subsection. In the Y text field, type 0.03.
- 5 In the X text field, type 0.015.
- 6 In the Material Rendering toolbar, click Plot.

Club Head

- I In the Model Builder window, right-click Golf Ball and choose Duplicate.
- 2 In the Settings window for Surface, type Club Head in the Label text field.
- 3 Click to expand the Inherit Style section. From the Plot list, choose Golf Ball.

Selection I

- I In the Model Builder window, expand the Club Head node, then click Selection I.
- 2 In the Settings window for Selection, locate the Selection section.

3 From the Selection list, choose Polished Steel.

Image I

In the Model Builder window, right-click Image I and choose Delete.

Material Appearance 1

- I In the Model Builder window, click Material Appearance I.
- 2 In the Settings window for Material Appearance, locate the Appearance section.
- 3 From the Material list, choose Club Head (matl).
- **4** Locate the **Color** section. Clear the **Use the plot's color** check box.

Club Face

- I In the Model Builder window, right-click Club Head and choose Duplicate.
- 2 In the Settings window for Surface, type Club Face in the Label text field.

Selection 1

- I In the Model Builder window, expand the Club Face node, then click Selection I.
- 2 In the Settings window for Selection, locate the Selection section.
- 3 From the Selection list, choose Club Face.

Material Appearance 1

- I In the Model Builder window, click Material Appearance I.
- 2 In the Settings window for Material Appearance, locate the Appearance section.
- 3 From the Appearance list, choose Custom.
- 4 From the Material type list, choose Steel (scratched).

Grooves

- I In the Model Builder window, right-click Club Face and choose Duplicate.
- 2 In the Model Builder window, click Club Face 1.
- 3 In the Settings window for Surface, type Grooves in the Label text field.

Material Appearance 1

- I In the Model Builder window, click Material Appearance I.
- 2 In the Settings window for Material Appearance, locate the Appearance section.
- 3 From the Material type list, choose Plastic.
- 4 From the Color list, choose Black.

Selection 1

I In the Model Builder window, click Selection I.

- 2 In the Settings window for Selection, locate the Selection section.
- **3** From the **Selection** list, choose **Grooves**.

Ferrule

- I In the Model Builder window, right-click Grooves and choose Duplicate.
- 2 In the Settings window for Surface, type Ferrule in the Label text field.

Selection 1

- I In the Model Builder window, expand the Ferrule node, then click Selection I.
- 2 In the Settings window for Selection, locate the Selection section.
- 3 From the Selection list, choose Club Ferrule, Boundary.
- **4** Click the **S Outdoor Environment** button in the **Graphics** toolbar.

Animation I

- I In the Material Rendering toolbar, click Animation and choose Player.
- 2 In the Settings window for Animation, locate the Frames section.
- 3 From the Frame selection list, choose All.

Energy

- I In the Home toolbar, click **Add Plot Group** and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Energy in the Label text field.
- 3 Click to expand the **Title** section. From the **Title type** list, choose **None**.
- 4 Locate the Plot Settings section. Select the y-axis label check box.
- 5 In the associated text field, type Energy (J).
- 6 Locate the Legend section. From the Position list, choose Middle right.

Global I

- I Right-click Energy and choose Global.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
intop1(solid.Ws)		Elastic
intop1(solid.Wk)		Kinetic

- 4 Locate the x-Axis Data section. From the Unit list, choose ms.
- 5 Click to expand the Coloring and Style section. In the Width text field, type 2.

6 In the **Energy** toolbar, click **Plot**.

Velocity

- I In the Home toolbar, click In Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Velocity in the Label text field.
- **3** Locate the **Title** section. From the **Title type** list, choose **None**.
- 4 Locate the Plot Settings section. Select the y-axis label check box.
- 5 In the associated text field, type Velocity (m/s).
- 6 Locate the Legend section. From the Position list, choose Lower right.

Global I

- I Right-click Velocity and choose Global.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
aveop1(solid.vel)	m/s	Club head
aveop2(solid.vel)	m/s	Golf ball

- 4 Locate the x-Axis Data section. From the Unit list, choose ms.
- 5 Locate the Coloring and Style section. In the Width text field, type 2.
- 6 In the **Velocity** toolbar, click **Plot**.

Evaluate typical golf metrics.

Golf Metrics

- I In the Results toolbar, click **Evaluation Group**.
- 2 In the Settings window for Evaluation Group, type Golf Metrics in the Label text field.
- 3 Locate the Data section. From the Time selection list, choose Last.

Point Evaluation 1

- I Right-click Golf Metrics and choose Point Evaluation.
- **2** Select Point 165 only.
- 3 In the Settings window for Point Evaluation, locate the Expressions section.
- **4** In the table, enter the following settings:

Expression	Unit	Description
atan(z/x)	deg	Launch angle

Global Evaluation 1

- I In the Model Builder window, right-click Golf Metrics and choose Global Evaluation.
- 2 In the Settings window for Global Evaluation, locate the Expressions section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
solid.avgr1.disp_t	mph	Ball speed
solid.avgr1.disp_t/vel	1	Smash factor
solid.avgr1.totrot_t/(2*pi[rad])	rpm	Spin rate

4 In the Golf Metrics toolbar, click **= Evaluate**.