

# Residual Stress in a Thin-Film Resonator — 2D

Almost all surface-micromachined thin films experience residual stress as a result of the fabrication process. The most common source of residual stress is thermal stress, which is caused by a change in temperature experienced during the fabrication sequence and also due to the difference in the coefficient of thermal expansion between the film and the substrate. This tutorial shows how to model thermal residual stress due to a temperature difference and how it changes the resonant frequency of a thin-film resonator. The substrate is not included in the model and it is also assumed that at a given state (which indicates a particular step of the process sequence), the temperature is uniform throughout the cantilever.

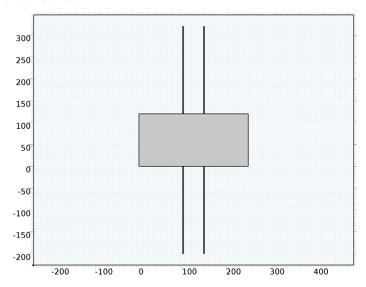


Figure 1: A thin-film resonator with four straight cantilever beam springs.

The tutorial investigates two design choices; a resonator with straight cantilevers (Figure 1) and another one with folded cantilevers (Figure 2). For each of the designs, the resonant frequency is computed for the cases when the structure is unstressed and when it is subjected to a residual thermal stress. The results obtained are compared with analytical solutions.

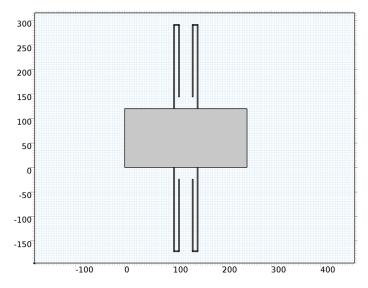


Figure 2: A thin-film resonator with four folded cantilever beam springs.

## Model Definition

This tutorial uses the dimensions and material properties presented in Table 1 and Table 2. These values were obtained from the example in Chapter 27.2.5 in Ref. 1. It calculates the length of the folded cantilever using the equivalent spring-constant relationship discussed later.

This simulation models thermal residual stress using the Thermal Expansion feature in the Solid Mechanics interface. The coefficient of thermal expansion is computed by assuming a residual stress of 50 MPa in the straight cantilevers, a film deposition temperature of 605°C (see Chapter 16.13.2.3 in Ref. 1) and a room temperature of 25°C.

TABLE I: DIMENSIONS OF THE STRUCTURE.

PARAMETER	STRAIGHT	FOLDED CANTILEVERS			PLATE
	CANTILEVERS	LI	L2	L3	
Length	<b>200</b> μm	170 μm	10 μm	146 μm	250 μm
Width	2 μm	2 μm	2 μm	2 μm	120 μm
Thickness	2.25 μm	2.25 μm	2.25 μm	2.25 μm	2.25 μm

TABLE 2: MATERIAL PROPERTIES OF THE STRUCTURE.

PROPERTY	VALUE
Material	polysilicon
Young's modulus	155 GPa
Poisson's ratio	0.23
Density	2330 kg/m <sup>3</sup>
T <sub>0</sub>	605°C
T <sub>I</sub>	25°C

In order to determine the eigenfrequencies for the case with residual stress, a Prestressed-Eigenfrequency Study is used. This predefined study type first solves for a static thermal expansion problem to compute the residual stress. The solution of this static problem is then used to create a shift in the linearization point around which the eigenfrequencies are then computed. This approach accurately computes the shift in eigenfrequency by accounting for the stress-stiffening effect.

#### **2D ANALYTICAL MODEL**

For a lateral resonator with four cantilever-beam springs, the first in-plane bending resonant frequency is given by Equation 1.

$$f_0 \approx \frac{1}{2\pi} \sqrt{\frac{4Etb^3}{mL^3} + \frac{24\sigma_r tb}{5mL}} \tag{1}$$

Here m is the mass of the resonator plate, E is Young's modulus, L is the length of each cantilever arm, b is its width, t is its thickness, and  $\sigma_r$  is the residual stress in each cantilever. In this tutorial, the stress is assumed to be purely because of temperature difference but in reality it could be a sum of external stresses, the thermal stress, and intrinsic components. Assuming the material is isotropic, the stress is constant through the film thickness, and the stress component in the direction normal to the substrate is zero (i.e. plane stress). The stress-strain relationship is then given by Equation 2. Here v is the Poisson's ratio.

$$\sigma_{\mathbf{r}} = \left(\frac{E}{1 - \nu}\right) \varepsilon \tag{2}$$

The strain comes from  $\varepsilon = \alpha \Delta T$  where  $\alpha$  is the thermal-expansion coefficient of the cantilever material and  $\Delta T$  is the difference between the deposition temperature and the normal operating temperature.

Thermal residual stress in thin-film spring structures is typically relieved by folding the flexures as shown in Figure 2. The flexures relieve axial stress because each is free to expand or contract in the axial direction.

The basic folded structure is a U-shaped spring. For springs in series, the equivalent spring constant is given by Equation 3.

$$\frac{1}{k_{\rm eq}} = \frac{1}{k_1} + \frac{1}{k_2} + \frac{1}{k_3} \tag{3}$$

The first and third springs are cantilever beams. The equivalent spring constant for these can be computed as  $k = 3EI/L^3$ , where I is the moment of inertia. For a beam with rectangular cross-section and for a rotation about the local y-axis of the beam (the axis parallel to the in-plane width), the moment of inertia is  $I = bt^3/12$ , where b is the width and t is the structure's thickness. You can treat the second spring as a column with a spring constant of k = AE/L, where A is the cross-sectional area A = bt. Assuming the spring thickness (t) and width (b) are the same everywhere, Equation 3 can be used to find the equivalent length of each set of folded springs. The equivalent length can be expressed in terms of the out-of-plane thickness (t) and the length of each of the three sections of a folded cantilever as shown in Equation 4.

$$L_{\text{eq}}^3 = L_1^3 + \frac{t^2 L_2}{4} + L_3^3, \tag{4}$$

Using the information provided in Table 1 and Table 2 and by using Equation 1 and Equation 2, one could compute the resonant frequency for the unstressed and stressed thin-film resonator with straight cantilever. Additionally by using Equation 4 along with the other information, one could also find the resonant frequency for the unstressed resonator with folded cantilevers. Note that the residual stress in the folded cantilevers are negligible by design and hence there is no need to compute the resonant frequency for this scenario. A summary of the analytical results are shown in Table 3 where they are compared with the solution obtained from the 2D plane-stress COMSOL model.

## Results and Discussion

Table 3 summarizes the resonant frequencies for the first in-plane bending eigenmode. For the 2D COMSOL models this is the lowest (first) eigenmode. As the table shows, the resonant frequency for the straight cantilevers increases significantly when the model includes residual stress. The model results agree closely with the analytical estimates. As

expected, the stress sensitivity of the resonant frequency is reduced by folding the cantilevers.

TABLE 3: RESONANT FREQUENCIES WITH AND WITHOUT RESIDUAL STRESS.

	STRAIGHT CAN	STRAIGHT CANTILEVERS		FOLDED CANTILEVERS	
	ANALYTICAL	2D MODEL	ANALYTICAL	2D MODEL	
Without stress	14.99 kHz	14.82 kHz	14.97 kHz	14.11 kHz	
With residual stress	33.08 kHz	32.05 kHz	-	14.22 kHz	

Figure 3 and Figure 4 show the first in-plane bending resonance mode for the unstressed resonator with straight and folded cantilevers respectively.

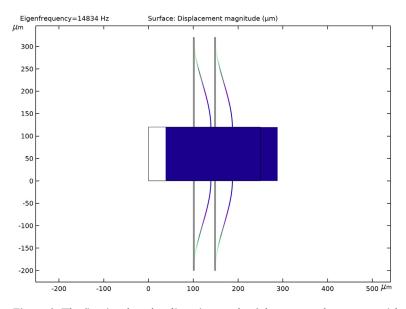


Figure 3: The first in-plane bending eigenmode of the unstressed resonator with straight cantilevers.

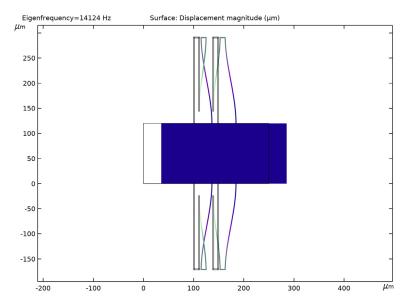


Figure 4: The first in-plane bending eigenmode of the unstressed resonator with folded cantilevers.

Figure 5 and Figure 6 show the first in-plane bending resonance mode for the resonator with straight and folded cantilevers respectively when they have a residual thermal stress.

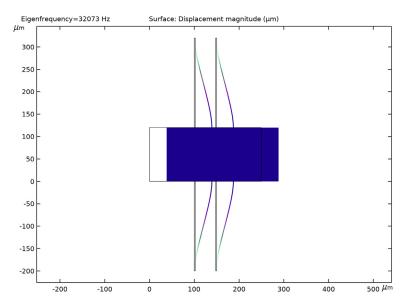


Figure 5: The first in-plane bending eigenmode of the resonator with straight cantilevers having residual thermal stress.

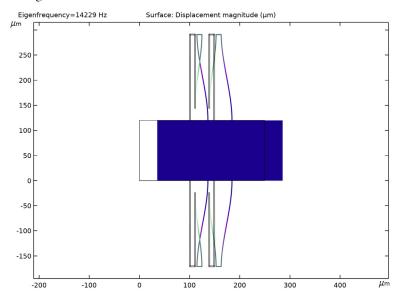


Figure 6: The first in-plane bending eigenmode of the resonator with folded cantilevers having residual thermal stress.

Figure 7 and Figure 8 show the residual thermal stress (von Mises stress) distribution in the resonator with straight and folded cantilevers respectively when they are cooled from 605°C to 25°C. Figure 7 shows that the residual stress is almost uniform in the straight cantilever and is about 49 MPa. The maximum stress is about 55 MPa at the two ends of the cantilevers. Figure 8 shows that the folded configuration significantly reduces the residual stress build-up. In this case the residual stress is around 2 MPa in most part of the cantilever except near the fixed end where it is close to 39 MPa.

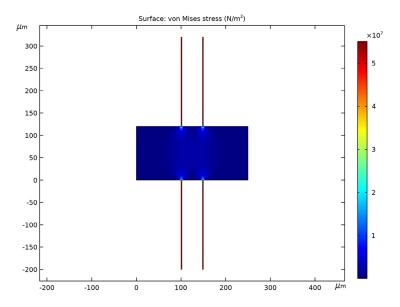


Figure 7: Residual thermal stress in the resonator with straight cantilevers when it is cooled from  $605^{\circ}C$  to  $25^{\circ}C$ .

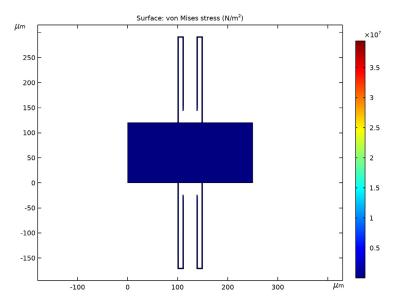


Figure 8: Residual thermal stress in the resonator with folded cantilevers when it is cooled from 605°C to 25°C.

## Reference

1. M. Gad-el-Hak, ed., The MEMS Handbook, CRC Press, London, 2002, ch. 16.12 and 27.2.5.

Application Library path: MEMS\_Module/Actuators/ residual\_stress\_resonator\_2d

## Modeling Instructions

From the File menu, choose New.

## NEW

In the New window, click Model Wizard.

#### MODEL WIZARD

- I In the Model Wizard window, click **2** 2D.
- 2 In the Select Physics tree, select Structural Mechanics>Solid Mechanics (solid).
- 3 Click Add.
- 4 Click Study.
- 5 In the Select Study tree, select General Studies>Eigenfrequency.
- 6 Click M Done.

#### **GEOMETRY I**

Load in the required global parameters. As well as defining some model variables, these values are used later for comparison between the model and the analytical solution.

#### **GLOBAL DEFINITIONS**

#### Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click Load from File.
- **4** Browse to the model's Application Libraries folder and double-click the file residual stress resonator 2d parameters.txt.

First create a component to model the resonator with straight cantilevers. For convenience, the device geometry will be inserted from an existing file. You can read the instructions for creating the geometry in the Appendix — Geometry Instructions.

#### GEOMETRY I

- I In the Geometry toolbar, click Insert Sequence.
- 2 Browse to the model's Application Libraries folder and double-click the file residual\_stress\_resonator\_2d\_geom\_sequence.mph.
- 3 In the Insert Sequence from File dialog box, click OK.
- 4 In the Geometry toolbar, click 📑 Build All.

Next set up the required solid mechanics physics for the problem by adding a **Thermal Expansion** sub-feature and specifying the fixed boundaries.

## SOLID MECHANICS (SOLID)

- I In the Model Builder window, under Component I (compl) click Solid Mechanics (solid).
- 2 In the Settings window for Solid Mechanics, locate the 2D Approximation section.

- 3 From the list, choose Plane stress.
- **4** Locate the **Thickness** section. In the d text field, type thickness.

Linear Elastic Material I

In the Model Builder window, under Component I (compl)>Solid Mechanics (solid) click Linear Elastic Material I.

Thermal Expansion 1

- I In the Physics toolbar, click Attributes and choose Thermal Expansion.
- 2 In the Settings window for Thermal Expansion, locate the Model Input section.
- **3** From the T list, choose **User defined**. In the associated text field, type T0.
- 4 Click Go to Source.

### GLOBAL DEFINITIONS

Default Model Inputs

- I In the Model Builder window, under Global Definitions click Default Model Inputs.
- 2 In the Settings window for Default Model Inputs, locate the Browse Model Inputs section.
- 3 Find the Expression for remaining selection subsection. In the Volume reference temperature text field, type T1.

The reference strain for thermal expansion is now T1. This value will be common to all thermal expansion features in the model.

## SOLID MECHANICS (SOLID)

Fixed Constraint I

- I In the Physics toolbar, click Boundaries and choose Fixed Constraint.
- 2 In the Settings window for Fixed Constraint, locate the Boundary Selection section.
- 3 Click Paste Selection.
- 4 In the Paste Selection dialog box, type 5,9,15,19 in the Selection text field.
- 5 Click OK.

Now add a new material to the component in order to define the required physical properties of the device.

#### MATERIALS

Material I (mat1)

- I In the Model Builder window, under Component I (compl) right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, locate the Material Contents section.
- **3** In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	E	E1	Pa	Basic
Poisson's ratio	nu	nu1	I	Basic
Density	rho	rho1	kg/m³	Basic
Coefficient of thermal expansion	alpha_iso; alphaii = alpha_iso, alphaij = 0	daT	I/K	Basic

Configure a suitable mesh, a **Mapped** mesh is appropriate for this device geometry.

#### MESH I

## Mapped I

In the Mesh toolbar, click Mapped.

## Distribution I

- I Right-click Mapped I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Boundary Selection section.
- 3 Click Paste Selection.
- 4 In the Paste Selection dialog box, type 6, 8, 16, 18 in the Selection text field.
- 5 Click OK.
- 6 In the Settings window for Distribution, locate the Distribution section.
- 7 In the Number of elements text field, type 2.

#### Size

- I In the Model Builder window, click Size.
- 2 In the Settings window for Size, locate the Element Size section.
- 3 From the Predefined list, choose Extra fine.

## 4 Click III Build All.

Add a second component to model the resonator with folded cantilevers. As with the first component, the device geometry will be imported for convenience.

#### ADD COMPONENT

In the Model Builder window, right-click the root node and choose Add Component>2D.

#### **GEOMETRY 2**

- I In the Geometry toolbar, click Insert Sequence.
- 2 Browse to the model's Application Libraries folder and double-click the file residual\_stress\_resonator\_2d\_geom\_sequence.mph.
- 3 In the Insert Sequence from File dialog box, select Geometry 2 in the Select geometry sequence to insert list.
- 4 Click OK.
- 5 In the Geometry toolbar, click **Build All**.

Now the solid mechanics physics can be configured, as with the first component. In addition, a material will be added to define the required properties of the second device and an appropriate mesh will be created.

#### ADD PHYSICS

- I In the Home toolbar, click Add Physics to open the Add Physics window.
- 2 Go to the Add Physics window.
- 3 In the tree, select Structural Mechanics>Solid Mechanics (solid).
- 4 Click Add to Component 2 in the window toolbar.
- 5 In the Home toolbar, click Add Physics to close the Add Physics window.

## SOLID MECHANICS 2 (SOLID2)

- I In the Settings window for Solid Mechanics, locate the 2D Approximation section.
- 2 From the list, choose Plane stress.
- **3** Locate the **Thickness** section. In the d text field, type thickness.

Linear Elastic Material I

In the Model Builder window, under Component 2 (comp2)>Solid Mechanics 2 (solid2) click Linear Elastic Material I.

Thermal Expansion 1

I In the Physics toolbar, click — Attributes and choose Thermal Expansion.

- 2 In the Settings window for Thermal Expansion, locate the Model Input section.
- **3** From the T list, choose **User defined**. In the associated text field, type T0.

#### Fixed Constraint I

- I In the Physics toolbar, click Boundaries and choose Fixed Constraint.
- 2 In the Settings window for Fixed Constraint, locate the Boundary Selection section.
- 3 Click Paste Selection.
- 4 In the Paste Selection dialog box, type 28,30,42,44 in the Selection text field.
- 5 Click OK.

#### MATERIALS

Material 2 (mat2)

- I In the Model Builder window, under Component 2 (comp2) right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, locate the Material Contents section.
- **3** In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	E	E1	Pa	Basic
Poisson's ratio	nu	nu1	I	Basic
Density	rho	rho1	kg/m³	Basic
Coefficient of thermal expansion	alpha_iso; alphaii = alpha_iso, alphaij = 0	daT	I/K	Basic

#### MESH 2

## Mapped I

In the Mesh toolbar, click Mapped.

#### Distribution I

- I Right-click Mapped I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Boundary Selection section.
- 3 Click Paste Selection.

- 4 In the Paste Selection dialog box, type 4,8,10,11,28,30,38,42,44,45,60,62 in the Selection text field.
- 5 Click OK.
- 6 In the Settings window for Distribution, locate the Distribution section.
- 7 In the Number of elements text field, type 2.

#### Size

- I In the Model Builder window, click Size.
- 2 In the Settings window for Size, locate the Element Size section.
- 3 From the Predefined list, choose Extra fine.
- 4 Click III Build All.

In order to perform the required computations four studies are required. The first two studies, one for each of the components, are for the case of zero-stress. These studies require one Eigenfrequency solver step, which will be used to calculate the eigenfrequency and mode of each resonator.

## STUDY I - STRAIGHT CANTILEVER, NO STRESS

- I In the Model Builder window, right-click Study I and choose Rename.
- 2 In the Rename Study dialog box, type Study 1 Straight Cantilever, No Stress in the New label text field.
- 3 Click OK.

#### Step 1: Eigenfrequency

- I In the Model Builder window, under Study I Straight Cantilever, No Stress click Step 1: Eigenfrequency.
- 2 In the Settings window for Eigenfrequency, locate the Physics and Variables Selection section.
- 3 In the table, clear the Solve for check box for Solid Mechanics 2 (solid2).

#### ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies> Eigenfrequency.
- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

#### STUDY 2

Step 1: Eigenfrequency

- I In the Settings window for Eigenfrequency, locate the Physics and Variables Selection section.
- 2 In the table, clear the Solve for check box for Solid Mechanics (solid).
- 3 In the Model Builder window, right-click Study 2 and choose Rename.
- 4 In the Rename Study dialog box, type Study 2 Folded Cantilever, No Stress in the New label text field.
- 5 Click OK.

The second two studies require two study steps: an initial **Stationary** study step is used to calculate the residual thermal stress due to the difference between the fabrication and operation temperatures; the solution to this step is then used to shift the linerization point around which the eigenfrequenies are computed in a subsequent Eigenfrequency study step. Eigenfrequency, Prestressed studies are used as this study type contains the required study steps by default.

#### ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select Preset Studies for Selected Physics Interfaces>Eigenfrequency, Prestressed.
- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

#### STUDY 3

Step 1: Stationary

- I In the Settings window for Stationary, locate the Physics and Variables Selection section.
- 2 In the table, clear the Solve for check box for Solid Mechanics 2 (solid2).

Step 2: Eigenfrequency

- I In the Model Builder window, click Step 2: Eigenfrequency.
- 2 In the Settings window for Eigenfrequency, locate the Physics and Variables Selection section.
- 3 In the table, clear the Solve for check box for Solid Mechanics 2 (solid2).
- 4 In the Model Builder window, right-click Study 3 and choose Rename.

- 5 In the Rename Study dialog box, type Study 3 Straight Cantilever, Residual Stress in the New label text field.
- 6 Click OK.

#### ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- **2** Go to the **Add Study** window.
- 3 Find the Studies subsection. In the Select Study tree, select Preset Studies for Selected Physics Interfaces>Eigenfrequency, Prestressed.
- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

#### STUDY 4

Step 1: Stationary

- I In the Settings window for Stationary, locate the Physics and Variables Selection section.
- 2 In the table, clear the Solve for check box for Solid Mechanics (solid).

Step 2: Eigenfrequency

- I In the Model Builder window, click Step 2: Eigenfrequency.
- 2 In the Settings window for Eigenfrequency, locate the Physics and Variables Selection section.
- 3 In the table, clear the Solve for check box for Solid Mechanics (solid).
- 4 In the Model Builder window, right-click Study 4 and choose Rename.
- 5 In the Rename Study dialog box, type Study 4 Folded Cantilever, Residual Stress in the New label text field.
- Click OK.

The studies can now be solved and the results visualized.

#### STUDY I - STRAIGHT CANTILEVER, NO STRESS

In the **Home** toolbar, click **Compute**.

#### RESULTS

Straight Cantilever, No Stress

I Right-click Results>Mode Shape (solid) and choose Rename.

- 2 In the Rename 2D Plot Group dialog box, type Straight Cantilever, No Stress in the New label text field
- 3 Click OK.
- 4 In the Straight Cantilever, No Stress toolbar, click Plot.

#### STUDY 2 - FOLDED CANTILEVER, NO STRESS

In the **Home** toolbar, click **Compute**.

#### RESULTS

Folded Cantilever, No Stress

- I Right-click Results>Mode Shape (solid2) and choose Rename.
- 2 In the Rename 2D Plot Group dialog box, type Folded Cantilever, No Stress in the New label text field.
- 3 Click OK.
- 4 In the Folded Cantilever, No Stress toolbar, click Plot.

#### STUDY 3 - STRAIGHT CANTILEVER, RESIDUAL STRESS

In the **Home** toolbar, click **Compute**.

#### RESULTS

Straight Cantilever, Residual Stress

- I Right-click Results>Mode Shape (solid) and choose Rename.
- 2 In the Rename 2D Plot Group dialog box, type Straight Cantilever, Residual Stress in the New label text field.
- 3 Click OK.

## STUDY 4 - FOLDED CANTILEVER, RESIDUAL STRESS

In the **Home** toolbar, click **Compute**.

## RESULTS

Folded Cantilever, Residual Stress

- I Right-click Results>Mode Shape (solid2) and choose Rename.
- 2 In the Rename 2D Plot Group dialog box, type Folded Cantilever, Residual Stress in the New label text field.

- 3 Click OK.
- 4 In the Folded Cantilever, Residual Stress toolbar, click **Tool** Plot.

#### Residual Stress in Straight Cantilever

- I In the Home toolbar, click <a>[</a> <a>Add Plot Group</a> and choose 2D Plot Group.
- 2 Right-click 2D Plot Group 5 and choose Rename.
- 3 In the Rename 2D Plot Group dialog box, type Residual Stress in Straight Cantilever in the New label text field.
- 4 Click OK.
- 5 In the Settings window for 2D Plot Group, locate the Data section.
- 6 From the Dataset list, choose Study 3 Straight Cantilever, Residual Stress/ Solution Store I (7) (sol4).

#### Surface I

- I Right-click Residual Stress in Straight Cantilever and choose Surface.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type solid.mises.
- 4 In the Residual Stress in Straight Cantilever toolbar, click **Tool** Plot.

#### Residual Stress in Folded Cantilever

- I In the Home toolbar, click <a> Add Plot Group</a> and choose 2D Plot Group.
- 2 Right-click 2D Plot Group 6 and choose Rename.
- 3 In the Rename 2D Plot Group dialog box, type Residual Stress in Folded Cantilever in the New label text field.
- 4 Click OK.
- 5 In the Settings window for 2D Plot Group, locate the Data section.
- 6 From the Dataset list, choose Study 4 Folded Cantilever, Residual Stress/ Solution Store 2 (12) (sol6).

## Surface I

- I Right-click Residual Stress in Folded Cantilever and choose Surface.
- 2 In the Settings window for Surface, locate the Expression section.
- **3** In the **Expression** text field, type solid2.mises.

From the File menu, choose New.

#### NEW

In the New window, click Model Wizard.

#### MODEL WIZARD

- I In the Model Wizard window, click **2** 2D.
- 2 In the Select Physics tree, select Structural Mechanics>Solid Mechanics (solid).
- 3 Click Add.
- 4 Click Done.

#### GEOMETRY I

- I In the Model Builder window, under Component I (compl) click Geometry I.
- 2 In the Settings window for Geometry, locate the Units section.
- 3 From the Length unit list, choose  $\mu m$ .

## Rectangle I (rI)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 250.
- 4 In the Height text field, type 120.

## Rectangle 2 (r2)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 2.
- 4 In the **Height** text field, type 200.
- **5** Locate the **Position** section. In the **x** text field, type 100.
- 6 In the y text field, type 120.

- I In the Geometry toolbar, click Transforms and choose Array.
- 2 Select the object **r2** only.
- 3 In the Settings window for Array, locate the Size section.
- 4 In the x size text field, type 2.

- 5 In the y size text field, type 2.
- **6** Locate the **Displacement** section. In the **x** text field, type 48.
- 7 In the y text field, type -320.
- 8 Click Build All Objects.

#### ADD COMPONENT

In the Model Builder window, right-click the root node and choose Add Component>2D.

#### **GEOMETRY 2**

- I In the Settings window for Geometry, locate the Units section.
- 2 From the Length unit list, choose µm.

Rectangle I (rI)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 250.
- 4 In the Height text field, type 120.

Rectangle 2 (r2)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 2.
- **4** In the **Height** text field, type 172.
- **5** Locate the **Position** section. In the **x** text field, type 100.
- 6 In the y text field, type 120.

Rectangle 3 (r3)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 12.
- 4 In the **Height** text field, type 2.
- **5** Locate the **Position** section. In the **x** text field, type 100.
- 6 In the y text field, type 290.

Rectangle 4 (r4)

I In the Geometry toolbar, click Rectangle.

- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 2.
- **4** In the **Height** text field, type 148.
- **5** Locate the **Position** section. In the **x** text field, type 110.
- 6 In the y text field, type 144.

### Mirror I (mir I)

- I In the Geometry toolbar, click Transforms and choose Mirror.
- 2 Click the Zoom Extents button in the Graphics toolbar.
- 3 Select the objects r2, r3, and r4 only.
- 4 In the Settings window for Mirror, locate the Input section.
- **5** Select the **Keep input objects** check box.
- 6 Locate the Point on Line of Reflection section. In the x text field, type 125.

## Mirror 2 (mir2)

- I In the Geometry toolbar, click Transforms and choose Mirror.
- 2 Select the objects mirl(1), mirl(2), mirl(3), r2, r3, and r4 only.
- 3 In the Settings window for Mirror, locate the Input section.
- 4 Select the **Keep input objects** check box.
- **5** Locate the **Point on Line of Reflection** section. In the **y** text field, type **60**.
- 6 Locate the Normal Vector to Line of Reflection section. In the x text field, type 0.
- 7 In the y text field, type 1.
- 8 Click **Build All Objects**.