

Microresistor Beam

Introduction

This example illustrates the ability to couple thermal, electrical, and structural analysis in one model. This particular application moves a beam by passing a current through it; the current generates heat, and the temperature increase leads to displacement through thermal expansion. The model estimates how much current and increase in temperature are necessary to displace the beam.

Although the model involves a rather simple 3D geometry and straightforward physics, it provides a good example of multiphysics modeling.



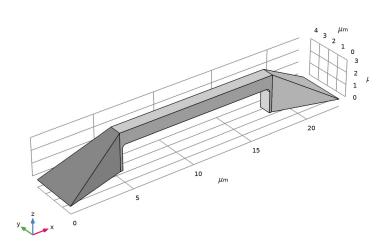


Figure 1: Microbeam geometry.

A copper microbeam has a length of $13 \,\mu\text{m}$ with a height and width of $1 \,\mu\text{m}$. Feet at both ends bond it rigidly to a substrate. An electric potential of $0.2 \,\text{V}$ applied between the feet induces an electric current. Due to the material's resistivity, the current heats up the structure. Because the beam operates in the open, the generated heat dissipates into the air. The thermally induced stress loads the material and deforms the beam.

As a first approximation, you can assume that the electrical conductivity is constant. However, a conductor's resistivity increases with temperature. In the case of copper, the relationship between resistivity and temperature is approximately linear over a wide range of temperatures:

$$\rho = \rho_0 (1 + \alpha (T - T_0))$$
(1)

 α is the temperature coefficient. You obtain the conductor's temperature dependency from the relationship that defines electric resistivity; conductivity is simply its reciprocal ($\sigma = 1/\rho$).

For the heat transfer equations, set the base boundaries facing the substrate to a constant temperature of 323 K. You model the convective air cooling in other boundaries using a heat flux boundary condition with a heat transfer coefficient, h, of 5 W/(m²·K) and an external temperature, T_{inf} , of 298 K. Standard constraints handle the bases' rigid connection to the substrate.

Results and Discussion

Figure 2 shows the temperature field on the microbeam surface when solving the model using a temperature-dependent resistivity as in Equation 1. Based on the color scale, the maximum temperature is about 710 K.

Figure 3 shows the microbeam's deformation. The displacement for the temperaturedependent case is 48 nm compared to the maximum displacement for constant electrical conductivity, which is 88 nm (the plot scales the deformation by a factor of around 20). Surface: Temperature (K)

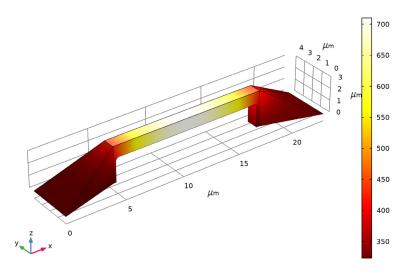


Figure 2: Surface temperature with temperature-dependent electrical conductivity.

Surface: Displacement magnitude (nm)

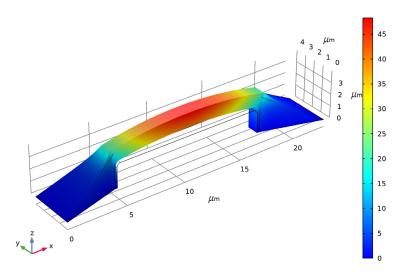


Figure 3: Microbeam deformation with temperature-dependent electrical conductivity.

In this example you create the 3D geometry by starting with two 2D work planes. The first one views the geometry from above, and the second does so from the side. You create cross sections on the work planes, which you then extrude into 3D. As the final step you create the resistor beam geometry as the intersection of the extruded objects. You can also skip the step-by-step instructions for the geometry creation and import the ready-made geometry directly from the Application Libraries.

By using the *Joule Heating and Thermal Expansion* predefined multiphysics interface you automatically add the equations for three physics including the necessary multiphysics couplings. In this case the physics equations describe the current and heat conduction and structural mechanics problems. The interface also provides suitable defaults for the solver.

Application Library path: MEMS_Module/Actuators/microresistor_beam

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click <u>Model Wizard</u>.

MODEL WIZARD

- I In the Model Wizard window, click 间 3D.
- 2 In the Select Physics tree, select Structural Mechanics>Thermal-Structure Interaction> Joule Heating and Thermal Expansion.
- 3 Click Add.
- 4 Click 🔿 Study.
- 5 In the Select Study tree, select General Studies>Stationary.
- 6 Click 🗹 Done.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.

Name	Expression	Value	Description
V0	0.2[V]	0.2 V	Applied voltage
то	323[K]	323 K	Heat sink temperature
Text	298[K]	298 K	External temperature
k	5[W/(m^2*K)]	5 W/(m²·K)	Heat transfer coefficient

3 In the table, enter the following settings:

GEOMETRY I

- I In the Model Builder window, under Component I (compl) click Geometry I.
- 2 In the Settings window for Geometry, locate the Units section.
- 3 From the Length unit list, choose µm.

Work Plane I (wp1)

- I In the Geometry toolbar, click 🖶 Work Plane.
- 2 In the Settings window for Work Plane, click Show Work Plane.

Work Plane I (wpI)>Plane Geometry

In the Model Builder window, click Plane Geometry.

Work Plane I (wpl)>Polygon I (poll)

- I In the Work Plane toolbar, click / Polygon.
- 2 In the Settings window for Polygon, locate the Coordinates section.
- 3 From the Data source list, choose Vectors.
- **4** In the **xw** text field, type 0 5 5 18 18 23 23 23 23 18 18 5 5 0 0 0.
- 5 In the yw text field, type 0 1.5 1.5 1.5 1.5 0 0 4 4 2.5 2.5 2.5 2.5 4 4 0.

Extrude I (extI)

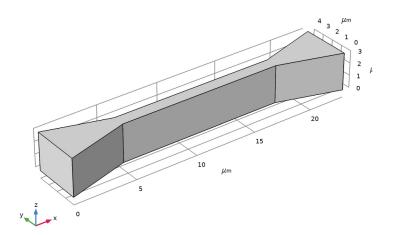
- In the Model Builder window, under Component I (compl)>Geometry I right-click
 Work Plane I (wpl) and choose Extrude.
- 2 In the Settings window for Extrude, locate the Distances section.
- **3** In the table, enter the following settings:

Distances (µm)

3

4 Click 🟢 Build All Objects.

5 Click the **Graphics** toolbar.

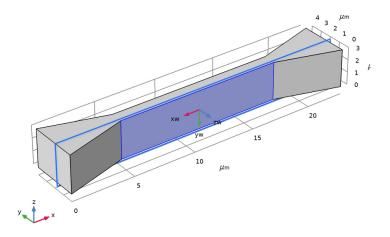


Work Plane 2 (wp2)

- I In the Geometry toolbar, click 🖶 Work Plane.
- 2 In the Settings window for Work Plane, locate the Plane Definition section.
- 3 From the Plane type list, choose Face parallel.

4 On the object extl, select Boundary 6 only.

It might be easier to select the correct boundary by using the **Selection List** window. To open this window, in the **Home** toolbar click **Windows** and choose **Selection List**. (If you are running the cross-platform desktop, you find **Windows** in the main menu.)



- 5 In the Offset in normal direction text field, type -1.5.
- 6 Select the Reverse normal direction check box.
- 7 Click 📥 Show Work Plane.

Work Plane 2 (wp2)>Plane Geometry

- I In the Settings window for Plane Geometry, locate the Visualization section.
- **2** Find the **In-plane visualization of 3D geometry** subsection. Clear the **Intersection (green)** check box.
- 3 Clear the Coincident entities (blue) check box.

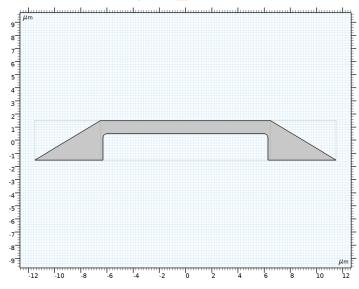
Work Plane 2 (wp2)>Polygon 1 (poll)

- I In the Work Plane toolbar, click / Polygon.
- 2 In the Settings window for Polygon, locate the Coordinates section.
- 3 From the Data source list, choose Vectors.
- **4** In the **xw** text field, type -11.5 -6.3 -6.3 -6.3 -6.3 6.3 6.3 6.3 6.3 11.5 11.5 6.5 6.5 -6.5 -6.5 -11.5.

- **5** In the **yw** text field, type -1.5 -1.5 -1.5 0.5 0.5 0.5 0.5 -1.5 -1.5 -1.5 -1.5 1.5 1.5 1.5 1.5 -1.5.
- 6 Click the + Zoom Extents button in the Graphics toolbar.

Work Plane 2 (wp2)>Fillet 1 (fil1)

- I In the Work Plane toolbar, click / Fillet.
- 2 On the object **poll**, select Points 4 and 6 only.
- 3 In the Settings window for Fillet, locate the Radius section.
- 4 In the Radius text field, type 0.3.
- 5 In the Work Plane toolbar, click 📳 Build All.



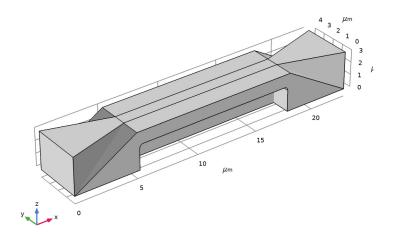
Extrude 2 (ext2)

- In the Model Builder window, under Component I (compl)>Geometry I right-click
 Work Plane 2 (wp2) and choose Extrude.
- 2 In the Settings window for Extrude, locate the Distances section.
- **3** In the table, enter the following settings:

Distances (µm)

4

4 Click **Build All Objects**.



Intersection 1 (int1)

- I In the Geometry toolbar, click 📕 Booleans and Partitions and choose Intersection.
- 2 Click in the Graphics window and then press Ctrl+A to select both objects.
- **3** In the Settings window for Intersection, click **H** Build All Objects.

Form Union (fin)

- I In the Model Builder window, click Form Union (fin).
- 2 In the Settings window for Form Union/Assembly, click 📳 Build Selected.

The model geometry is now complete.

DEFINITIONS

Add a set of selections that you can use later when applying boundary conditions.

connector l

- I In the Definitions toolbar, click 🗞 Explicit.
- 2 Right-click Explicit I and choose Rename.
- 3 In the Rename Explicit dialog box, type connector1 in the New label text field.
- 4 Click OK.
- 5 In the Settings window for Explicit, locate the Input Entities section.
- 6 From the Geometric entity level list, choose Boundary.

7 Select Boundary 1 only.

connector2

- I In the **Definitions** toolbar, click **here Explicit**.
- 2 In the Model Builder window, right-click Explicit 2 and choose Rename.
- 3 In the Rename Explicit dialog box, type connector2 in the New label text field.
- 4 Click OK.
- 5 In the Settings window for Explicit, locate the Input Entities section.
- 6 From the Geometric entity level list, choose Boundary.
- 7 Select Boundary 13 only.

connectors

- I In the Definitions toolbar, click 嘴 Explicit.
- 2 Right-click Explicit 3 and choose Rename.
- 3 In the Rename Explicit dialog box, type connectors in the New label text field.
- 4 Click OK.
- 5 In the Settings window for Explicit, locate the Input Entities section.
- 6 From the Geometric entity level list, choose Boundary.
- 7 Select Boundaries 1 and 13 only.

ADD MATERIAL

- I In the Home toolbar, click 🙀 Add Material to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select MEMS>Metals>Cu Copper.
- 4 Click Add to Component in the window toolbar.
- 5 In the Home toolbar, click 🙀 Add Material to close the Add Material window.

MATERIALS

Cu - Copper (mat1)

I In the Settings window for Material, locate the Material Contents section.

2 In the table, enter the following settings:

Property	Variable	Value	Unit	P roperty group
Relative permittivity	epsilonr_iso ; epsilonrii = epsilonr_iso, epsilonrij = 0	1	I	Basic

- 3 Click to expand the Material Properties section. In the Material properties tree, select Electromagnetic Models>Linearized resistivity>Reference resistivity (rho0).
- 4 Click + Add to Material.
- **5** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group	
Reference resistivity	rho0	1.72e-8[ohm* m]	Ω·m	Linearized resistivity	
Resistivity temperature coefficient	alpha	0.0039[1/K]	I/K	Linearized resistivity	
Reference temperature	Tref	293[K]	К	Linearized resistivity	

ELECTRIC CURRENTS (EC)

Current Conservation 1

- I In the Model Builder window, under Component I (compl)>Electric Currents (ec) click Current Conservation I.
- **2** In the **Settings** window for **Current Conservation**, locate the **Constitutive Relation Jc-E** section.
- 3 From the Conduction model list, choose Linearized resistivity.

Before solving the two-way coupled model with a temperature-dependent resistivity, use a constant resistivity for later comparison:

4 From the α list, choose **User defined**. Keep the default zero value for α .

Ground I

- I In the Physics toolbar, click 🔚 Boundaries and choose Ground.
- 2 In the Settings window for Ground, locate the Boundary Selection section.
- **3** From the **Selection** list, choose **connector2**.

Electric Potential I

- I In the Physics toolbar, click 📄 Boundaries and choose Electric Potential.
- 2 In the Settings window for Electric Potential, locate the Electric Potential section.
- **3** In the V_0 text field, type V0.
- 4 Locate the Boundary Selection section. From the Selection list, choose connector I.

MULTIPHYSICS

Thermal Expansion 1 (tel)

- I In the Model Builder window, under Component I (compl)>Multiphysics click Thermal Expansion I (tel).
- 2 In the Settings window for Thermal Expansion, locate the Model Input section.
- 3 Click **Go to Source**.

GLOBAL DEFINITIONS

Default Model Inputs

- I In the Model Builder window, under Global Definitions click Default Model Inputs.
- 2 In the Settings window for Default Model Inputs, locate the Browse Model Inputs section.
- **3** Find the **Expression for remaining selection** subsection. In the **Volume reference temperature** text field, type Text.

HEAT TRANSFER IN SOLIDS (HT)

Initial Values 1

- I In the Model Builder window, under Component I (compl)>Heat Transfer in Solids (ht) click Initial Values I.
- 2 In the Settings window for Initial Values, locate the Initial Values section.
- **3** In the T text field, type T0.

Heat Flux 1

- I In the Physics toolbar, click 🔚 Boundaries and choose Heat Flux.
- 2 In the Settings window for Heat Flux, locate the Boundary Selection section.
- 3 From the Selection list, choose All boundaries.

Select all boundaries for simplicity; next you will add a node that overrides this boundary condition for the connectors.

4 Locate the Heat Flux section. Click the Convective heat flux button.

- **5** In the *h* text field, type k.
- **6** In the T_{ext} text field, type Text.

Temperature I

- I In the Physics toolbar, click 📄 Boundaries and choose Temperature.
- 2 In the Settings window for Temperature, locate the Temperature section.
- **3** In the T_0 text field, type T0.
- 4 Locate the Boundary Selection section. From the Selection list, choose connectors.

SOLID MECHANICS (SOLID)

In the Model Builder window, under Component I (compl) click Solid Mechanics (solid).

Fixed Constraint I

- I In the Physics toolbar, click 🔚 Boundaries and choose Fixed Constraint.
- 2 In the Settings window for Fixed Constraint, locate the Boundary Selection section.
- **3** From the **Selection** list, choose **connectors**.

MESH I

Free Tetrahedral I In the Mesh toolbar, click 🖟 Free Tetrahedral.

Size

- I In the Model Builder window, click Size.
- 2 In the Settings window for Size, locate the Element Size section.
- 3 From the Predefined list, choose Finer.
- 4 In the Model Builder window, right-click Mesh I and choose Build All.

STUDY I

You can use the default solver settings for this model.

I In the **Home** toolbar, click **= Compute**.

RESULTS

Displacement - Study 1

The first default plot presents a surface plot of the von Mises stress. Modify it to show the displacement magnitude.

I Right-click Results>Stress (solid) and choose Rename.

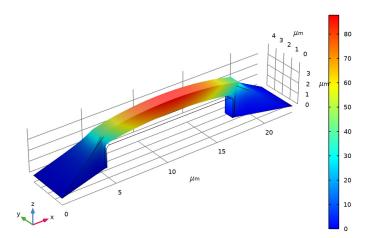
- 2 In the Rename 3D Plot Group dialog box, type Displacement Study 1 in the New label text field.
- 3 Click OK.

Surface 1

- I In the Model Builder window, expand the Displacement Study I node, then click Surface I.
- 2 In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>Solid Mechanics> Displacement>solid.disp - Displacement magnitude - m.
- **3** Locate the **Expression** section. From the **Unit** list, choose **nm**.
- **4** In the **Displacement Study I** toolbar, click **O** Plot.

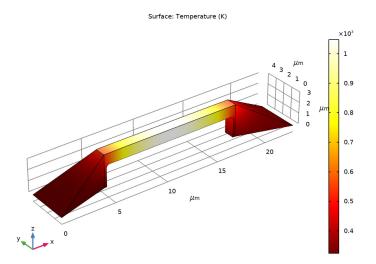
As the color legend shows, the maximum displacement is roughly 88 nm with a constant resistivity.

Surface: Displacement magnitude (nm)



Temperature (ht)

The second default surface plot shows the temperature field. Note the maximum temperature of roughly 1048 K.



Now restore the temperature-dependence of the resistivity that you temporarily disabled and then add a new study and solve the model again.

ELECTRIC CURRENTS (EC)

Current Conservation 1

- I In the Model Builder window, under Component I (comp1)>Electric Currents (ec) click Current Conservation I.
- **2** In the Settings window for Current Conservation, locate the Constitutive Relation Jc-E section.
- **3** From the α list, choose **From material**.

ADD STUDY

- I In the Home toolbar, click \sim_1° Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies>Stationary.
- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click \sim Add Study to close the Add Study window.

STUDY 2

In the **Home** toolbar, click **= Compute**.

RESULTS

Temperature (ht) I

As you can see from the plot, using the more realistic material model with a temperaturedependent resistivity has a significant effect on the solution. The maximum temperature is now almost 340 K lower.

Displacement - Study 2

- I In the Model Builder window, right-click Stress (solid) and choose Rename.
- 2 In the Rename 3D Plot Group dialog box, type Displacement Study 2 in the New label text field.
- 3 Click OK.

Surface 1

- I In the Model Builder window, expand the Displacement Study 2 node, then click Surface I.
- 2 In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>Solid Mechanics> Displacement>solid.disp - Displacement magnitude - m.
- **3** Locate the **Expression** section. From the **Unit** list, choose **nm**.
- 4 In the Displacement Study 2 toolbar, click 💽 Plot.

Similarly, the maximum displacement has been reduced from 88 nm to around 50 nm.