

Dynamics of a Cylindrical Roller Bearing

Introduction

Bearings are used in machines to reduce the friction between moving parts and thereby smoothen their relative motion. Rolling element bearing is one of the widely used bearings, where rolling elements or rollers are used to support the load. These rollers can be of different shapes- for instance- spherical, cylindrical, or tapered cylindrical.

This model simulates the dynamics of a cylindrical roller bearing. Here, multiple cylindrical rollers are inserted between the outer and inner race, and held in place with the help of the cage. The inner race is connected to a rotating shaft and the outer race to a fixed foundation. All components of the bearing are assumed rigid. Frictional contact is modeled between rollers and races using rigid body contact with friction. The connection between rollers and the cage is simplified using hinge joints. An external load is applied on the inner race and a transient study is performed to analyze the lateral dynamics of inner race, dynamics of rollers and cage, contact and friction forces, and energy dissipation due to friction.

Model Definition

The model geometry consists of twelve identical cylindrical rollers of radius 6 mm, inserted between two concentric cylindrical races of thickness 4.875 mm each.



Figure 1: Model geometry of the cylindrical roller bearing.

The inner radius of outer race is 45.125 mm and the outer radius of inner race is 32.875 mm. As shown in Figure 1, a slotted cylindrical ring called cage is used to hold the rollers in place and keep them separated. All components of the bearing are assumed rigid and use the material data for structural steel.

The connection between rollers and cage is modeled through hinge joints, having only one rotational degree of freedom about their axes (*y*-axis). The outer race is assumed to be connected to a fixed foundation without any translational or rotational motion. The inner race is connected to a shaft rotating with an angular speed of 5000 rpm. Additionally, a bearing load of 100 N is acting on inner race along *-z* direction.

For each rigid roller, a line of contact exists with both inner and outer races. Using the rigid body contact with friction functionality, the interaction between each roller and races are modeled as frictional contacts. The coefficient of friction between the rollers and races is assumed as 0.1.

A time dependent study is performed for 0.06 s, which corresponds to five cycles of rotation of shaft or inner race, to analyze the dynamics of inner race, cage and rollers. The contact and frictional forces between races and rollers are also studied.

Results and Discussion

Figure 2 shows the displacement in the inner race, rollers, and cage. As rollers are in contact with inner race, the rotation of inner race also leads to the rotation of rollers and cage. Figure 3 shows the velocity of rollers and cage. The contact force between rollers and inner race is also plotted here.

As rollers are free to rotate about their own axes, they exhibit an additional spinning motion about their axes. This can be visualized by plotting the relative velocity of rollers with respect to cage as shown in Figure 4.



Figure 2: Displacement of different components in cylindrical roller bearing at t = 0.06 s.



Time=0.06 s Surface: Velocity magnitude (m/s) Arrow Surface: Contact force (N)

Figure 3: Velocity of rollers and cage at t = 0.06 s. Arrow plot shows the contact force between the rollers and inner race.



Figure 4: Relative velocity of rollers with respect to cage at t = 0.06 s.

The dynamics of the system is controlled by the inner race moving with a constant angular speed of 5000 rpm. This motion is transmitted to the contacting rollers and cage. Figure 5 shows the angular speed of inner race and cage.

Due to the contact with the rotating inner race, the direction of spin of rollers would be opposite to that of inner race. Angular speed of three sample rollers is shown in Figure 6. Contact and friction forces between the inner race and one of these sample rollers are shown in Figure 7. Frictional energy dissipation rate due to the contact between the three sample rollers and inner race is shown in Figure 8. Orbital motion of inner race is shown in Figure 9.



Figure 5: Angular speed of inner race and cage, as a function of time.



Figure 6: Angular speed of three sample rollers, as a function of time.

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Figure 7: Contact and friction forces between a sample roller and inner race, as a function of time.



Figure 8: Frictional energy dissipation rate between three sample rollers and inner race, as a function of time.



Figure 9: Orbital motion of inner race.

Notes About the COMSOL Implementation

- In this model, all components are modeled as rigid elements using the **Rigid Domain** nodes which can be created automatically using the **Create Rigid Domains** button in the **Automated Model Setup** section at the physics interface.
- Joint nodes between rollers and cage can also be created automatically using the **Create** Joints button in the **Automated Model Setup** section at the physics interface. The automatic joint creation requires the geometry to be in assembly mode and **Identity Boundary Pair** nodes to be available in the **Definitions**.

Application Library path: Multibody_Dynamics_Module/Tutorials/ roller_bearing_dynamics

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click 🔗 Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click 间 3D.
- 2 In the Select Physics tree, select Structural Mechanics>Multibody Dynamics (mbd).
- 3 Click Add.
- 4 Click 🔿 Study.
- 5 In the Select Study tree, select General Studies>Time Dependent.
- 6 Click 🗹 Done.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click 📂 Load from File.
- **4** Browse to the model's Application Libraries folder and double-click the file roller_bearing_dynamics_parameters.txt.

If you do not want to import the geometry and create selections, you can load the geometry sequence from the stored model. In the **Model Builder** window, under **Component I (comp1)** right-click **Geometry I** and choose **Insert Sequence**. Browse to the model's Application Libraries folder and double-click the file roller_bearing_dynamics.mph. You can then continue to the **Definitions** section below.

To import the geometry and create selections from scratch, continue here.

GEOMETRY I

Import I (imp1)

- I In the Model Builder window, expand the Component I (compl)>Geometry I node.
- 2 Right-click Geometry I and choose Import.
- 3 In the Settings window for Import, locate the Import section.
- 4 Click Browse.
- **5** Browse to the model's Application Libraries folder and double-click the file roller_bearing_dynamics.mphbin.
- 6 Click Import.

Cage

- I In the Geometry toolbar, click 💁 Selections and choose Explicit Selection.
- 2 In the Settings window for Explicit Selection, type Cage in the Label text field.
- 3 On the object impl(2), select Domain 1 only.
- 4 Locate the Color section. From the Color list, choose Color 18.
- 5 Click 틤 Build Selected.

Races

- I In the Geometry toolbar, click 🖣 Selections and choose Explicit Selection.
- 2 In the Settings window for Explicit Selection, type Races in the Label text field.
- **3** On the object **imp1(1)**, select Domain 1 only.
- 4 On the object impl(15), select Domains 1–4 only.
- **5** Locate the **Color** section. From the **Color** list, choose **Custom**.
- 6 On Windows, click the colored bar underneath, or if you are running the crossplatform desktop — the **Color** button.
- 7 Click Define custom colors.
- 8 Set the RGB values to 128, 128, and 128, respectively.
- 9 Click Add to custom colors.
- **IO** Click **Show color palette only** or **OK** on the cross-platform desktop.

II Click 📄 Build Selected.

Rollers

- I In the Geometry toolbar, click 🐚 Selections and choose Complement Selection.
- 2 In the Settings window for Complement Selection, type Rollers in the Label text field.
- 3 Locate the Input Entities section. Click + Add.
- 4 In the Add dialog box, in the Selections to invert list, choose Cage and Races.
- 5 Click OK.
- 6 In the Settings window for Complement Selection, locate the Color section.
- 7 From the Color list, choose Color 3.
- 8 Click 틤 Build Selected.

Cage & Rollers

- I In the Geometry toolbar, click 🛯 Selections and choose Union Selection.
- 2 In the Settings window for Union Selection, type Cage & Rollers in the Label text field.

- **3** Locate the **Input Entities** section. Click + **Add**.
- 4 In the Add dialog box, in the Selections to add list, choose Cage and Rollers.
- 5 Click OK.
- 6 In the Settings window for Union Selection, click 📳 Build Selected.

Cage & Rollers Boundaries

- I In the Geometry toolbar, click 🐚 Selections and choose Adjacent Selection.
- **2** In the **Settings** window for **Adjacent Selection**, type **Cage & Rollers Boundaries** in the **Label** text field.
- 3 Locate the Input Entities section. Click + Add.
- 4 In the Add dialog box, select Cage & Rollers in the Input selections list.
- 5 Click OK.
- 6 In the Settings window for Adjacent Selection, click 📒 Build Selected.

Outer Race

- I In the Geometry toolbar, click 🐚 Selections and choose Explicit Selection.
- 2 In the Settings window for Explicit Selection, type Outer Race in the Label text field.
- 3 On the object impl(15), select Domains 1–4 only.
- 4 Click 🔚 Build Selected.

Outer Race Boundaries

- I In the Geometry toolbar, click 🖓 Selections and choose Adjacent Selection.
- 2 In the Settings window for Adjacent Selection, type Outer Race Boundaries in the Label text field.
- 3 Locate the Input Entities section. Click + Add.
- 4 In the Add dialog box, select Outer Race in the Input selections list.
- 5 Click OK.
- 6 In the Settings window for Adjacent Selection, locate the Output Entities section.
- 7 Select the Interior boundaries check box.
- 8 Click 틤 Build Selected.

Boundaries without Outer Race

- I In the Geometry toolbar, click 🖷 Selections and choose Complement Selection.
- 2 In the Settings window for Complement Selection, type Boundaries without Outer Race in the Label text field.
- **3** Locate the **Geometric Entity Level** section. From the **Level** list, choose **Boundary**.

- 4 Locate the Input Entities section. Click + Add.
- 5 In the Add dialog box, select Outer Race Boundaries in the Selections to invert list.
- 6 Click OK.
- 7 In the Settings window for Complement Selection, click 틤 Build Selected.

Form Union (fin)

- I In the Model Builder window, under Component I (compl)>Geometry I click Form Union (fin).
- 2 In the Settings window for Form Union/Assembly, locate the Form Union/Assembly section.
- 3 From the Action list, choose Form an assembly.
- 4 Click 📄 Build Selected.

For better visualization, you can hide the top part of the outer race.

- **5** Click the 🔌 Click and Hide button in the Graphics toolbar.
- 6 Click the 🔚 Select Domains button in the Graphics toolbar.
- 7 On the object fin, select Domain 1 only.

DEFINITIONS

Variables I

- I In the Model Builder window, under Component I (compl) right-click Definitions and choose Variables.
- 2 In the Settings window for Variables, locate the Variables section.
- 3 Click 📂 Load from File.
- **4** Browse to the model's Application Libraries folder and double-click the file roller_bearing_dynamics_variables.txt.

Ramp I (rm I)

- I In the Home toolbar, click f(X) Functions and choose Local>Ramp.
- 2 In the Settings window for Ramp, locate the Parameters section.
- 3 In the Slope text field, type 1000.
- 4 Select the **Cutoff** check box.

ADD MATERIAL

- I In the Home toolbar, click 🙀 Add Material to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select **Built-in>Structural steel**.

- 4 Click Add to Component in the window toolbar.
- 5 In the Home toolbar, click 🙀 Add Material to close the Add Material window.

MULTIBODY DYNAMICS (MBD)

Do as follows to generate Rigid Domain nodes for all components.

- I In the Model Builder window, under Component I (comp1) click Multibody Dynamics (mbd).
- 2 In the Settings window for Multibody Dynamics, click Physics Node Generation in the upper-right corner of the Automated Model Setup section. From the menu, choose Create Rigid Domains.

Rigid Domain 1: Outer Race

- I In the Model Builder window, expand the Rigid Domains (All) node, then click Rigid Domain I.
- 2 In the Settings window for Rigid Domain, type Rigid Domain 1: Outer Race in the Label text field.

Fixed Constraint I

In the Physics toolbar, click 📃 Attributes and choose Fixed Constraint.

Rigid Domain 3: Cage

- I In the Model Builder window, click Rigid Domain 3.
- 2 In the Settings window for Rigid Domain, type Rigid Domain 3: Cage in the Label text field.

Prescribed Displacement/Rotation 1

- I In the Physics toolbar, click 📃 Attributes and choose Prescribed Displacement/Rotation.
- 2 In the Settings window for Prescribed Displacement/Rotation, locate the Prescribed Displacement at Center of Rotation section.
- **3** Select the **Prescribed in y direction** check box.
- 4 Locate the Prescribed Rotation section. From the By list, choose Constrained rotation.
- **5** Select the **Constrain rotation around x-axis** check box.
- 6 Select the Constrain rotation around z-axis check box.

Rigid Domain 6: Inner Race

- I In the Model Builder window, click Rigid Domain 6.
- 2 In the Settings window for Rigid Domain, type Rigid Domain 6: Inner Race in the Label text field.

Prescribed Displacement/Rotation 1

- I In the Physics toolbar, click 🗁 Attributes and choose Prescribed Displacement/Rotation.
- 2 In the Settings window for Prescribed Displacement/Rotation, locate the Prescribed Displacement at Center of Rotation section.
- 3 Select the Prescribed in y direction check box.
- 4 Locate the Prescribed Rotation section. From the By list, choose Prescribed rotation.
- **5** Specify the Ω vector as

0	x
1	у
0	z

6 In the ϕ_0 text field, type omega*t.

Rigid Domain 6: Inner Race

In the Model Builder window, click Rigid Domain 6: Inner Race.

Applied Force 1

- I In the Physics toolbar, click 📃 Attributes and choose Applied Force.
- 2 In the Settings window for Applied Force, locate the Applied Force section.
- **3** Specify the **F** vector as

0	x
0	у
-load*rm1(t[1/s])	z

Do as follows to generate Hinge Joint nodes between rollers and cage.

- 4 In the Model Builder window, click Multibody Dynamics (mbd).
- **5** In the **Settings** window for **Multibody Dynamics**, click **Physics Node Generation** in the upper-right corner of the **Automated Model Setup** section. From the menu, choose **Create Joints**.

Rigid Body Contact 1

- I In the Physics toolbar, click 🖗 Global and choose Rigid Body Contact.
- 2 In the Settings window for Rigid Body Contact, locate the Source section.
- 3 From the Source list, choose Rigid Domain 2.
- **4** In the $r_{\rm s}$ text field, type rr.

- 5 Locate the Destination section. From the Destination list, choose Rigid Domain I: Outer Race.
- **6** In the r_d text field, type ro.
- 7 Select the Use inside boundaries for contact check box.
- **8** Locate the **Contact Settings** section. In the f_p text field, type fp.
- 9 In the τ_n text field, type 1[ms]*10.

Friction 1

- I In the Physics toolbar, click 层 Attributes and choose Friction.
- 2 In the Settings window for Friction, locate the Friction section.
- **3** In the μ text field, type mu.
- 4 In the v_0 text field, type mbd.diag*1e-3[1/s]*10.

Roller-Outer Race Contact

Similarly create eleven more **Rigid Body Contact** nodes between rollers and outer race by duplicating **Rigid Body Contact I** and resetting the inputs using the information given in the table below.

Name	Source	Destination
Rigid Body Contact 2	Rigid Domain 4	Rigid Domain I: Outer Race
Rigid Body Contact 3	Rigid Domain 5	Rigid Domain I: Outer Race
Rigid Body Contact 4	Rigid Domain 7	Rigid Domain I: Outer Race
Rigid Body Contact 5	Rigid Domain 8	Rigid Domain I: Outer Race
Rigid Body Contact 6	Rigid Domain 9	Rigid Domain I: Outer Race
Rigid Body Contact 7	Rigid Domain 10	Rigid Domain I: Outer Race
Rigid Body Contact 8	Rigid Domain 11	Rigid Domain I: Outer Race
Rigid Body Contact 9	Rigid Domain 12	Rigid Domain I: Outer Race
Rigid Body Contact 10	Rigid Domain 13	Rigid Domain I: Outer Race
Rigid Body Contact II	Rigid Domain 14	Rigid Domain I: Outer Race
Rigid Body Contact 12	Rigid Domain 15	Rigid Domain I: Outer Race

Rigid Body Contact I, Rigid Body Contact I0, Rigid Body Contact II, Rigid Body Contact I2, Rigid Body Contact 2, Rigid Body Contact 3, Rigid Body Contact 4, Rigid Body Contact 5, Rigid Body Contact 6, Rigid Body Contact 7, Rigid Body Contact 8, Rigid Body Contact 9

I In the Model Builder window, under Component I (compl)>Multibody Dynamics (mbd), Ctrl-click to select Rigid Body Contact I, Rigid Body Contact 2, Rigid Body Contact 3, Rigid Body Contact 4, Rigid Body Contact 5, Rigid Body Contact 6, Rigid Body Contact 7, Rigid Body Contact 8, Rigid Body Contact 9, Rigid Body Contact 10, Rigid Body Contact 11, and Rigid Body Contact 12.

2 Right-click and choose Group.

Roller-Outer Race Contact

In the **Settings** window for **Group**, type Roller-Outer Race Contact in the **Label** text field.

Add **Rigid Body Contact** nodes between rollers and inner race by duplicating **Roller-Outer Race Contact** and resetting the input values.

Roller-Inner Race Contact

- I Right-click Roller-Outer Race Contact and choose Duplicate.
- 2 In the Settings window for Group, type Roller-Inner Race Contact in the Label text field.

Rigid Body Contact 13

- I In the Model Builder window, expand the Roller-Inner Race Contact node, then click Rigid Body Contact 13.
- 2 In the Settings window for Rigid Body Contact, locate the Destination section.
- 3 From the Destination list, choose Rigid Domain 6: Inner Race.
- 4 Clear the Use inside boundaries for contact check box.
- **5** In the r_d text field, type ri.

Roller-Inner Race Contact

I Similar to the changes done for **Rigid Body Contact 13**, reset the inputs of other eleven **Rigid Body Contact** nodes using the information given in the table below.

Name	Source	Destination
Rigid Body Contact 14	Rigid Domain 4	Rigid Domain 6: Inner Race
Rigid Body Contact 15	Rigid Domain 5	Rigid Domain 6: Inner Race
Rigid Body Contact 16	Rigid Domain 7	Rigid Domain 6: Inner Race
Rigid Body Contact 17	Rigid Domain 8	Rigid Domain 6: Inner Race
Rigid Body Contact 18	Rigid Domain 9	Rigid Domain 6: Inner Race
Rigid Body Contact 19	Rigid Domain 10	Rigid Domain 6: Inner Race
Rigid Body Contact 20	Rigid Domain 11	Rigid Domain 6: Inner Race
Rigid Body Contact 21	Rigid Domain 12	Rigid Domain 6: Inner Race
Rigid Body Contact 22	Rigid Domain 13	Rigid Domain 6: Inner Race
Rigid Body Contact 23	Rigid Domain 14	Rigid Domain 6: Inner Race
Rigid Body Contact 24	Rigid Domain 15	Rigid Domain 6: Inner Race

In order to visualize the motion of the system with respect to the cage frame, you can use the option of defining a reference frame available in the **Multibody Dynamics** interface and plot the postprocessing variables for velocity with respect to the reference frame.

- 2 In the Model Builder window, click Multibody Dynamics (mbd).
- 3 In the Settings window for Multibody Dynamics, click to expand the Results section.
- 4 From the Body defining reference frame list, choose Rigid Domain 3: Cage.

MESH I

- I In the Model Builder window, under Component I (compl) click Mesh I.
- 2 In the Settings window for Mesh, locate the Physics-Controlled Mesh section.
- 3 From the Element size list, choose Finer.
- 4 Click 🏢 Build All.

STUDY I

- Step 1: Time Dependent
- I In the Model Builder window, under Study I click Step I: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- 3 In the **Output times** text field, type range(0,T/500,5*T).

Solution I (soll)

- I In the Study toolbar, click The Show Default Solver.
- 2 In the Model Builder window, expand the Solution I (soll) node.
- 3 In the Model Builder window, expand the Study I>Solver Configurations> Solution I (soll)>Time-Dependent Solver I node, then click Fully Coupled I.
- **4** In the **Settings** window for **Fully Coupled**, click to expand the **Method and Termination** section.
- 5 In the Maximum number of iterations text field, type 15.
- 6 In the Model Builder window, click Time-Dependent Solver I.
- 7 In the Settings window for Time-Dependent Solver, click to expand the Time Stepping section.
- 8 From the Steps taken by solver list, choose Intermediate.
- **9** In the **Study** toolbar, click **= Compute**.

RESULTS

Click the **Show Grid** button in the **Graphics** toolbar.

Follow the instructions below to plot system displacement as shown in Figure 2.

Displacement (mbd)

- I In the Model Builder window, under Results click Displacement (mbd).
- 2 In the Settings window for 3D Plot Group, locate the Plot Settings section.
- **3** Select the **Propagate hiding to lower dimensions** check box.
- 4 In the Model Builder window, expand the Displacement (mbd) node.

Selection 1

- I In the Model Builder window, expand the Results>Displacement (mbd)>Surface node.
- 2 Right-click Surface and choose Selection.
- 3 In the Settings window for Selection, locate the Selection section.
- 4 From the Selection list, choose Boundaries without Outer Race.

Surface 2

- I In the Model Builder window, right-click Surface and choose Duplicate.
- 2 In the Settings window for Surface, click to expand the Title section.
- 3 From the Title type list, choose None.
- 4 Locate the Coloring and Style section. From the Coloring list, choose Uniform.

5 From the Color list, choose Gray.

Transparency I

Right-click Surface 2 and choose Transparency.

Selection 1

- I In the Settings window for Selection, locate the Selection section.
- 2 Select the 🔲 Activate Selection toggle button.
- 3 From the Selection list, choose Outer Race Boundaries.
- **4** In the **Displacement (mbd)** toolbar, click **O** Plot.

Follow the instructions below to plot contact force and velocity. The resulting plot should match the one shown in Figure 3.

Contact Force & Velocity

- I In the Model Builder window, under Results click Velocity (mbd).
- 2 In the Settings window for 3D Plot Group, type Contact Force & Velocity in the Label text field.
- **3** Click to expand the **Selection** section. Locate the **Plot Settings** section. From the **View** list, choose **New view**.

Arrow Line

- I In the Model Builder window, expand the Contact Force & Velocity node.
- 2 Right-click Arrow Line and choose Delete.

Volume

- I In the Model Builder window, click Volume.
- 2 In the Settings window for Volume, locate the Coloring and Style section.
- 3 From the Coloring list, choose Uniform.
- 4 From the **Color** list, choose **Gray**.
- 5 Click to expand the Title section. From the Title type list, choose None.

Transparency I

Right-click Volume and choose Transparency.

Selection 1

- I Right-click Volume and choose Selection.
- 2 In the Settings window for Selection, locate the Selection section.
- **3** From the **Selection** list, choose **Races**.

4 In the list, choose 2 and 3.

5 Click — **Remove from Selection**.

6 Select Domains 1, 4, and 9 only.

Surface 1

- I In the Model Builder window, right-click Contact Force & Velocity and choose Surface.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type mbd.vel.
- 4 Locate the Coloring and Style section. From the Color table list, choose HeatCameraLight.

Deformation I

- I Right-click Surface I and choose Deformation.
- 2 In the Settings window for Deformation, locate the Scale section.
- **3** Select the **Scale factor** check box.
- **4** In the associated text field, type **1**.

Selection 1

- I In the Model Builder window, right-click Surface I and choose Selection.
- 2 In the Settings window for Selection, locate the Selection section.
- **3** From the Selection list, choose Cage & Rollers Boundaries.

Arrow Surface 1

- I In the Model Builder window, right-click Contact Force & Velocity and choose Arrow Surface.
- 2 In the Settings window for Arrow Surface, locate the Expression section.
- **3** In the **X** component text field, type Fnx.
- **4** In the **Y** component text field, type Fny.
- **5** In the **Z** component text field, type Fnz.
- 6 Select the **Description** check box.
- 7 In the associated text field, type Contact force (N).
- 8 Locate the Coloring and Style section. Select the Scale factor check box.
- 9 In the associated text field, type 5e-4.
- **IO** From the **Color** list, choose **Green**.

Deformation I

I Right-click Arrow Surface I and choose Deformation.

- 2 In the Settings window for Deformation, locate the Scale section.
- **3** Select the **Scale factor** check box.
- 4 In the associated text field, type 1.

Selection 1

- I In the Model Builder window, right-click Arrow Surface I and choose Selection.
- 2 In the Settings window for Selection, locate the Selection section.
- 3 From the Selection list, choose Cage & Rollers Boundaries.
- **4** In the **Contact Force & Velocity** toolbar, click **O Plot**.

Follow the instructions below to plot the velocity with respect to cage frame. The resulting plot should match the one shown in Figure 4.

Velocity [Cage Frame]

- I In the Model Builder window, right-click Contact Force & Velocity and choose Duplicate.
- 2 In the Settings window for 3D Plot Group, type Velocity [Cage Frame] in the Label text field.

Surface 1

- I In the Model Builder window, expand the Velocity [Cage Frame] node, then click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type mbd.vel_ref.

Arrow Surface 1

In the Model Builder window, right-click Arrow Surface I and choose Delete.

Velocity [Cage Frame]

Follow the instructions below to plot angular speed of inner race and cage. The resulting plot should match the one shown in Figure 5.

Angular Speed [Inner Race & Cage]

- I In the Home toolbar, click 🚛 Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Angular Speed [Inner Race & Cage] in the Label text field.
- 3 Click to expand the Title section. From the Title type list, choose Label.

Global I

- I Right-click Angular Speed [Inner Race & Cage] and choose Global.
- 2 In the Settings window for Global, locate the y-Axis Data section.

3 In the table, enter the following settings:

Expression	Unit	Description
mbd.rd6.th_ty	rad/s	Rigid body angular velocity, y component
mbd.rd3.th_ty	rad/s	Rigid body angular velocity, y component

4 Click to expand the Legends section. From the Legends list, choose Manual.

5 In the table, enter the following settings:

Legend	ls
Inner	race
Cage	

6 In the Angular Speed [Inner Race & Cage] toolbar, click 💽 Plot.

Follow the instructions below to plot angular speed of rollers. The resulting plot should match the one shown in Figure 6.

Angular Speed [Rollers]

- I In the Model Builder window, right-click Angular Speed [Inner Race & Cage] and choose Duplicate.
- 2 In the Settings window for ID Plot Group, type Angular Speed [Rollers] in the Label text field.

Global I

- I In the Model Builder window, expand the Angular Speed [Rollers] node, then click Global I.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
mbd.rd11.th_ty	rad/s	Rigid body angular velocity, y component
mbd.rd15.th_ty	rad/s	Rigid body angular velocity, y component
mbd.rd10.th_ty	rad/s	Rigid body angular velocity, y component

4 In the Angular Speed [Rollers] toolbar, click 💽 Plot.

5 Locate the Legends section. In the table, enter the following settings:

Legends A B C

6 In the Angular Speed [Rollers] toolbar, click 🗿 Plot.

Follow the instructions below to plot contact and friction force between roller and inner race. The resulting plot should match the one shown in Figure 7.

Contact & Friction Force [Roller-Inner Race]

- I In the Model Builder window, right-click Angular Speed [Rollers] and choose Duplicate.
- 2 In the Settings window for ID Plot Group, type Contact & Friction Force [Roller-Inner Race] in the Label text field.

Global I

- I In the Model Builder window, expand the Contact & Friction Force [Roller-Inner Race] node, then click Global I.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- 3 Click **Clear Table**.
- **4** In the table, enter the following settings:

Expression	Unit	Description
mbd.rbc20.Fn	Ν	Contact force
mbd.rbc20.Ff	Ν	Friction force

5 Locate the Legends section. From the Legends list, choose Automatic.

Contact & Friction Force [Roller-Inner Race]

- I In the Model Builder window, click Contact & Friction Force [Roller-Inner Race].
- 2 In the Settings window for ID Plot Group, locate the Plot Settings section.
- 3 Select the y-axis label check box.
- **4** In the associated text field, type Force (N).
- 5 In the Contact & Friction Force [Roller-Inner Race] toolbar, click 🗿 Plot.

Follow the instructions below to plot frictional energy dissipation rate between rollers and inner race. The resulting plot should match the one shown in Figure 8.

Frictional Energy Dissipation Rate [Roller-Inner Race]

- I Right-click Contact & Friction Force [Roller-Inner Race] and choose Duplicate.
- 2 In the Settings window for ID Plot Group, type Frictional Energy Dissipation Rate [Roller-Inner Race] in the Label text field.

Global I

- I In the Model Builder window, expand the Frictional Energy Dissipation Rate [Roller-Inner Race] node, then click Global I.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- 3 Click **Clear Table**.
- **4** In the table, enter the following settings:

Expression	Unit	Description
mbd.rbc20.Qf	W	Frictional energy dissipation rate
mbd.rbc24.Qf	W	Frictional energy dissipation rate
mbd.rbc19.Qf	W	Frictional energy dissipation rate

5 Locate the Legends section. From the Legends list, choose Manual.

6 In the table, enter the following settings:

Legends	_
А	
В	
С	

Frictional Energy Dissipation Rate [Roller-Inner Race]

- I In the Model Builder window, click Frictional Energy Dissipation Rate [Roller-Inner Race].
- 2 In the Settings window for ID Plot Group, locate the Plot Settings section.
- **3** Clear the **y-axis label** check box.
- 4 In the Frictional Energy Dissipation Rate [Roller-Inner Race] toolbar, click 💽 Plot.

Follow the instructions below to plot inner race orbit. The resulting plot should match the one shown in Figure 9.

Inner Race Orbit

- I Right-click Frictional Energy Dissipation Rate [Roller-Inner Race] and choose Duplicate.
- 2 In the Settings window for ID Plot Group, type Inner Race Orbit in the Label text field.

Global I

- I In the Model Builder window, expand the Inner Race Orbit node, then click Global I.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- 3 Click **Clear Table**.

4 In the table, enter the following settings:

Expression	Unit	Description
mbd.rd6.w	mm	Rigid body displacement, z component

- 5 Locate the Legends section. Clear the Show legends check box.
- 6 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- 7 In the **Expression** text field, type mbd.rd6.u.
- 8 From the Unit list, choose mm.

Inner Race Orbit

- I In the Model Builder window, click Inner Race Orbit.
- **2** In the Inner Race Orbit toolbar, click **OD** Plot.

Displacement (mbd)

- I In the **Results** toolbar, click **Main Animation** and choose **Player**.
- 2 In the Settings window for Animation, type Displacement (mbd) in the Label text field.
- 3 Locate the Frames section. In the Number of frames text field, type 100.

Contact Force & Velocity

- I Right-click **Displacement (mbd)** and choose **Duplicate**.
- 2 In the Settings window for Animation, type Contact Force & Velocity in the Label text field.
- 3 Locate the Scene section. From the Subject list, choose Contact Force & Velocity.

Velocity [Cage Frame]

- I Right-click Contact Force & Velocity and choose Duplicate.
- 2 In the Settings window for Animation, type Velocity [Cage Frame] in the Label text field.
- 3 Locate the Scene section. From the Subject list, choose Velocity [Cage Frame].