



# Thermal Stress Analysis of a Turbine Stator Blade

## *Introduction*

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The conditions within gas turbines are extreme. The pressure can be as high as 40 bars, and the temperature far above 1000 K. Any new component must therefore be carefully designed to be able to withstand thermal stress and vibrations due to the rotating machinery and aerodynamic loads exerted by the fluid rushing through the turbine. If a component fails, the high rotational speeds can result in a complete rupture of the whole turbine.

The most extreme conditions are found in the high pressure part downstream of the combustion chamber where hot combustion gas flows through a cascade of rotors and stators. To prevent the parts from melting, relatively “cold” air is taken from bleeding vanes located in the high-pressure compressor casing, then led past the combustion chamber into the turbine casing in order to be used as a coolant. Directly behind the combustion chamber, both internal cooling within ducts and film cooling over the blade side surfaces are applied. Besides, a surface treatment (coating) is often added to the current blades to protect them from hot corrosion. Further downstream, where the temperature is somewhat lower, it may suffice with internal cooling. For more details on gas turbines, see [Ref. 1](#).

Since the physics within a gas turbine is very complex, simplified approaches are often used at the initial stages of the development of the new components. In this tutorial, the thermal stresses in a stator blade with only internal cooling are analyzed (coating and film cooling are not considered).

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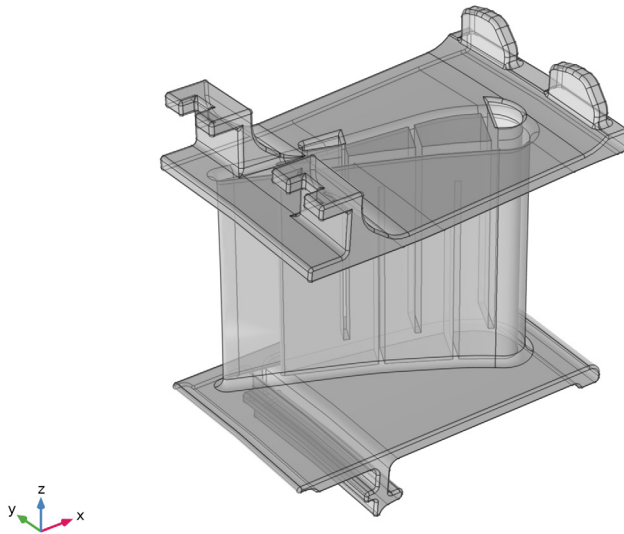
**Note:** This application requires the Structural Mechanics Module and the CFD Module or Heat Transfer Module. It also uses the Material Library.

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## *Model Definition*

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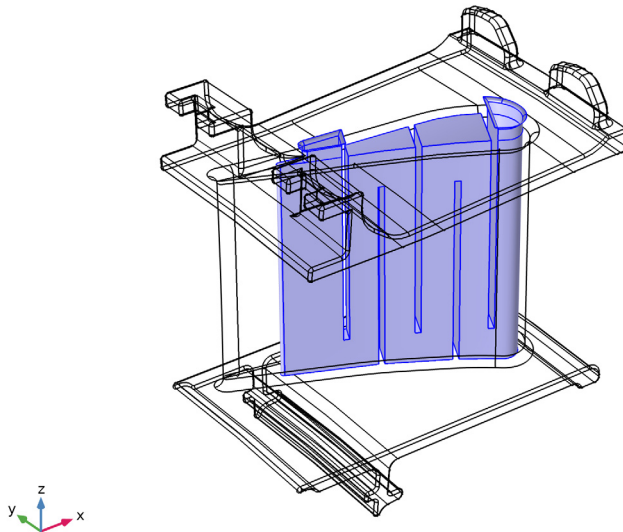
The model geometry is shown in [Figure 1](#). The stator blade profile is a modified version of a design shown in [Ref. 2](#). The model includes some generic mounting details as well as a generic internal cooling duct.



*Figure 1: A stator blade with mounting details.*

Use the Thermal Stress interface from the Structural Mechanics Module to set up the model. The blade and the mounting details are assumed to be made of the directionally solidified (DS) GTD111 alloy which is a nickel-based alloy with high tensile strength (Ref. 1). This material is available in the COMSOL Material Library. In addition to the data covered by the Material Library, the linear elastic model requires a reference temperature that is set to 300 K and a Poisson's Ratio that is set to 0.33, a number comparable to that for other stainless steels.

Figure 2 shows the cooling duct. The duct geometry is simplified and does not include details such as the ribs (Ref. 3) typical for cooling ducts. Instead of simulating the complicated flow in the duct, an average Nusselt number correlation from Ref. 3 is used to calculate a heat transfer coefficient. Assume the cooling fluid to be air at 30 bar and 600 K.



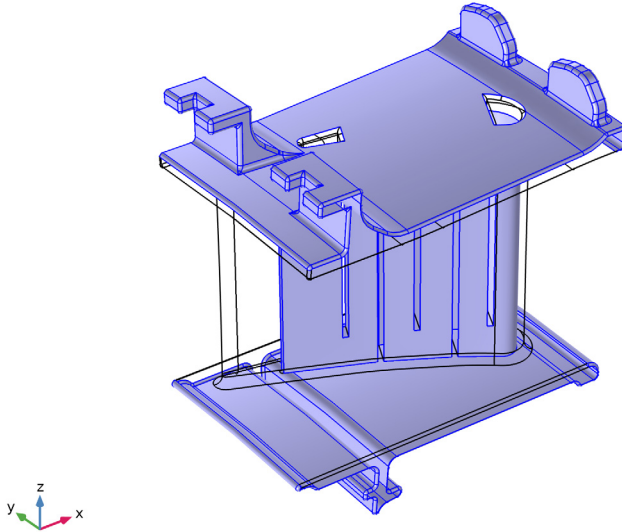
*Figure 2: The internal cooling duct.*

The heat flux on the stator blade surfaces is calculated using the heat transfer coefficient. The pressure and suction sides are approximated as two flat plates using the local heat transfer coefficient for external forced convection. The combustion gases are approximated as air at 30 bar and 1100 K. The corresponding speed of sound is approximately 650 m/s.

Ref. 4 contains a Mach number plot of stators without film cooling. A typical Mach number is 0.45 on the pressure side (the concave side) and 0.7 on the suction side (the convex side). This corresponds to approximately 300 m/s on the pressure side and 450 m/s on the suction side.

The platform walls adjacent to the stator blades are treated in the same way as the stator itself but with the free stream velocity set to 350 m/s.

The stator blade exchanges heat with the cooling air through the boundaries highlighted in [Figure 3](#). It is assumed that the turbine has a local working temperature of 900 K, and that the heat transfer coefficient to the stator is  $25 \text{ W}/(\text{m}^2 \cdot \text{K})$ .



*Figure 3: Boundaries through which heat is exchanged with the cooling air.*

The attachment of the stator element to a ring support is simulated via roller and spring foundation boundary conditions on a few boundaries. All other boundaries are free to deform as a result of thermal expansion.

### *Results and Discussion*

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[Figure 4](#) shows a temperature surface plot. The internal cooling creates significant temperature gradients within the blade. However, the trailing edge reaches a temperature close to that of the combustion gases, which indicates that the cooling might be

insufficient. The side walls also become very hot, and some additional cooling can be beneficial.

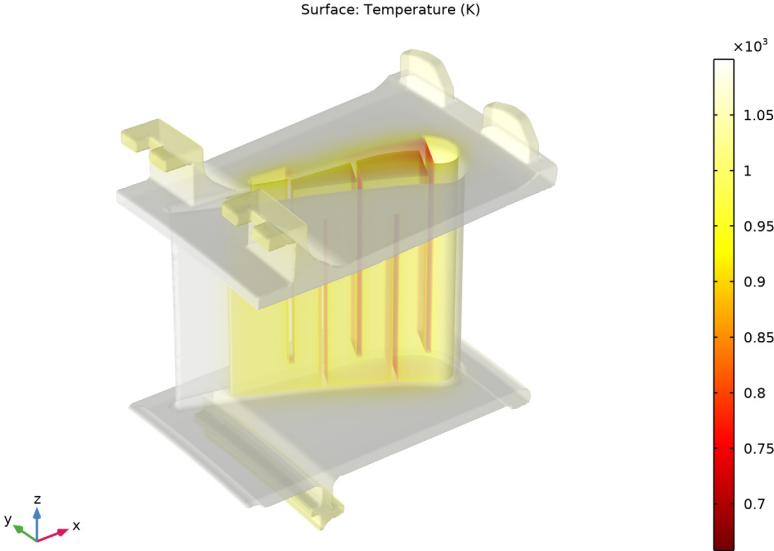


Figure 4: Surface temperature plot.

Figure 5 shows a surface plot of the von Mises stress. The maximum stress locally exceeds the yield stress of the material (Ref. 5) in some sharp geometric corners of the internal cooling duct. While this might indicate that the component is at risk for thermal fatigue,

no definite assessment can be made without conducting a more advanced analysis that includes a more detailed geometric representation of the duct.

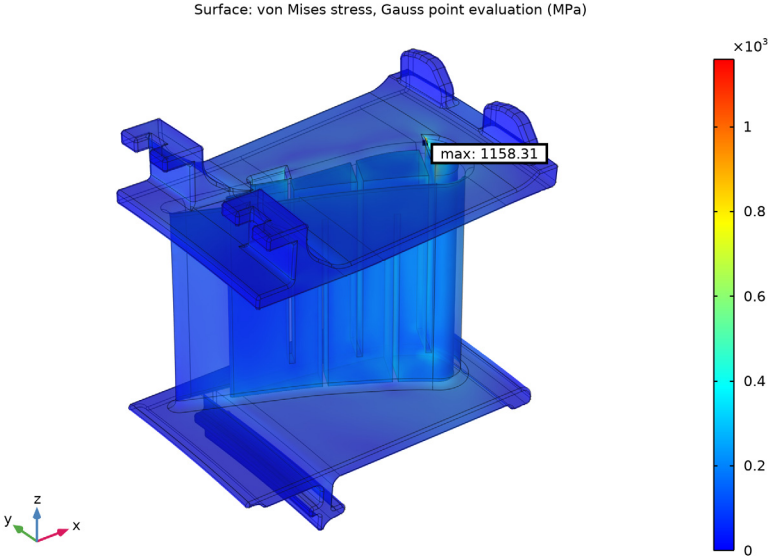


Figure 5: Surface plot of the von Mises stress.

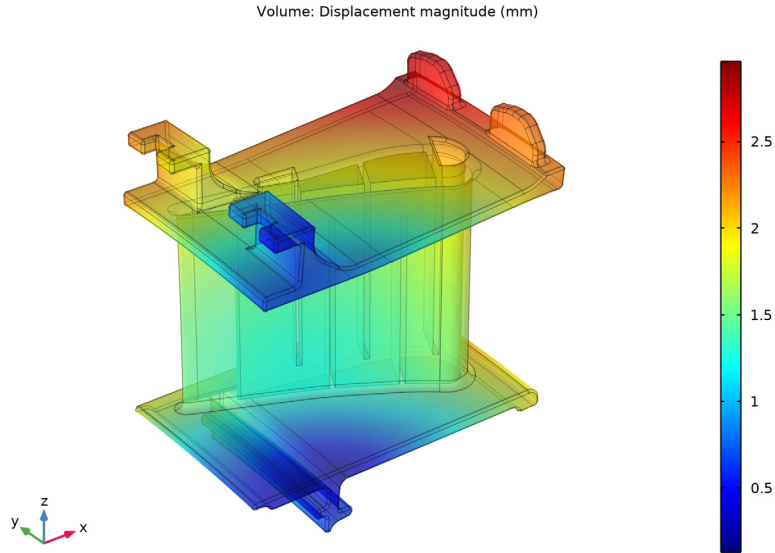


Figure 6: Surface plot of the displacement.

## References

1. M.P. Boyce, *Gas Turbine Engineering Handbook*, 2nd ed., Gulf Professional Publishing, 2001.
2. NASA, "Power Turbine", Glenn Research Center, [www.grc.nasa.gov/WWW/K-12/airplane/powturb.html](http://www.grc.nasa.gov/WWW/K-12/airplane/powturb.html).
3. J. Bredberg, "Turbulence Modelling for Internal Cooling of Gas-Turbine Blades", Thesis for the degree of doctor of philosophy, *Chalmers University of Technology*, 2002.
4. P. Dahlander, "Source Term Model Approaches to Film Cooling Simulations", Thesis for the degree of doctor of philosophy, *Chalmers University of Technology*, 2001.
5. <http://www.cnalloys.co.uk/stainless-jethete-m152>

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**Application Library path:** Heat\_Transfer\_Module/Thermal\_Stress/  
turbine\_stator

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**Note:** Instructions below require to select entities corresponding to a particular numbers list. For example:


Select Boundaries 113 and 139 only.

In most cases the easiest way to select them is to click the **Paste Selection** button  and paste the numbers as they are printed in the document (for example paste “113 and 139” for the example above).




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From the **File** menu, choose **New**.

### **NEW**

In the **New** window, click  **Model Wizard**.

### **MODEL WIZARD**

- 1 In the **Model Wizard** window, click  **3D**.
- 2 In the **Select Physics** tree, select **Structural Mechanics>Thermal-Structure Interaction>Thermal Stress, Solid**.
- 3 Click **Add**.
- 4 Click  **Study**.
- 5 In the **Select Study** tree, select **General Studies>Stationary**.
- 6 Click  **Done**.

### **GLOBAL DEFINITIONS**

#### *Parameters 1*





- 1 In the **Model Builder** window, under **Global Definitions** click **Parameters 1**.
- 2 In the **Settings** window for **Parameters**, locate the **Parameters** section.
- 3 In the table, enter the following settings:

<b>Name</b>	<b>Expression</b>	<b>Value</b>	<b>Description</b>
Pr_cool	0.72	0.72	Cooling Prandtl number
U_suction_side	450[m/s]	450 m/s	Gas velocity on stator suction side
U_pressure_side	300[m/s]	300 m/s	Gas velocity on stator pressure side

Name	Expression	Value	Description
U_platform	350[m/s]	350 m/s	Gas velocity along platform walls
T_gas	1100[K]	1100 K	Gas temperature
p_high	30[bar]	3E6 Pa	High pressure level
mu_cool	3.1e-5[Pa*s]	3.1E-5 Pa·s	Viscosity of the cooling air
Cp_cool	770[J/kg/K]	770 J/(kg·K)	Heat capacity of the cooling air
T_cool	600[K]	600 K	Cooling air temperature
H_cool	0.01[m]	0.01 m	Characteristic length scale of cooling channels
T_work	900[K]	900 K	Working temperature
Nu_cool	400	400	Average Nusselt number in cooling channel





## GEOMETRY I

### Import I (impI)

- 1 In the **Home** toolbar, click  **Import**.
- 2 In the **Settings** window for **Import**, locate the **Import** section.
- 3 Click **Browse**.
- 4 Browse to the model's Application Libraries folder and double-click the file turbine\_stator.mphbin.
- 5 Click **Import**.  
To see the interior:
- 6 Click the  **Transparency** button in the **Graphics** toolbar.  
The imported geometry should look as shown in the [Figure 1](#).
- 7 In the **Home** toolbar, click  **Build All**.
- 8 Click the  **Zoom Extents** button in the **Graphics** toolbar.  
Define a number of sections to simplify the model setup. First define the internal cooling duct boundaries.

## DEFINITIONS



### *Cooling Duct*

- 1 In the **Definitions** toolbar, click  **Explicit**.
- 2 In the **Settings** window for **Explicit**, type Cooling Duct in the **Label** text field.
- 3 Locate the **Input Entities** section. From the **Geometric entity level** list, choose **Boundary**.
- 4 Click  **Paste Selection**.
- 5 In the **Paste Selection** dialog box, type 222-225, 236, 261-266, 270-271, 278-279, 283-285, 292-305, 308-311, 313-314, 316, 321 in the **Selection** text field.  
If you are reading an electronic version of this document, you can copy the geometric entity numbers from the text.
- 6 Click **OK**.
- 7 Click the  **Transparency** button in the **Graphics** toolbar.
- 8 Click the  **Wireframe Rendering** button in the **Graphics** toolbar.



The selection is shown in [Figure 2](#).

Proceed to select the boundaries through which the heat exchange with the rest of the turbine occurs ([Figure 3](#)).

### *Exchange Boundaries*

- 1 In the **Definitions** toolbar, click  **Explicit**.
- 2 In the **Settings** window for **Explicit**, type Exchange Boundaries in the **Label** text field.
- 3 Locate the **Input Entities** section. From the **Geometric entity level** list, choose **Boundary**.
- 4 Click  **Paste Selection**.
- 5 In the **Paste Selection** dialog box, type 3-4, 9, 12, 14, 16, 19-20, 22-24, 28-96, 98-117, 122-135, 138-162, 166-221, 223, 226-231, 239-260, 267-269, 272-277, 280-282, 322-444 in the **Selection** text field.
- 6 Click **OK**.

## ADD MATERIAL

- 1 In the **Home** toolbar, click  **Add Material** to open the **Add Material** window.
- 2 Go to the **Add Material** window.
- 3 In the tree, select **Material Library>Nickel Alloys>GTD111 DS>GTD111 DS [solid]>GTD111 DS [solid,longitudinal]**.
- 4 Click **Add to Component** in the window toolbar.
- 5 In the **Home** toolbar, click  **Add Material** to close the **Add Material** window.

## MATERIALS

*GTD111 DS [solid,longitudinal] (mat1)*

- 1 In the **Settings** window for **Material**, locate the **Material Contents** section.
- 2 In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Poisson's ratio	nu	0.33	1	Young's modulus and Poisson's ratio
Thermal conductivity	k_iso ; kii = k_iso, kij = 0	k ( T [ 1 / K ] ) [ W / ( m * K ) ]	W/(m·K)	Basic


- 3 In the **Model Builder** window, expand the **GTD111 DS [solid,longitudinal] (mat1)** node.

*Piecewise (E\_solid\_longitudinal\_1)*

- 1 In the **Model Builder** window, expand the **Component 1 (comp1)>Materials>GTD111 DS [solid,longitudinal] (mat1)>Young's modulus and Poisson's ratio (Enu)** node, then click **Piecewise (E\_solid\_longitudinal\_1)**.
- 2 In the **Settings** window for **Piecewise**, locate the **Definition** section.
- 3 From the **Extrapolation** list, choose **Nearest function**.

## MULTIPHYSICS

*Thermal Expansion 1 (te1)*

- 1 In the **Model Builder** window, under **Component 1 (comp1)>Multiphysics** click **Thermal Expansion 1 (te1)**.
- 2 In the **Settings** window for **Thermal Expansion**, locate the **Model Input** section.
- 3 Click  **Go to Source**.

## GLOBAL DEFINITIONS

*Default Model Inputs*


- 1 In the **Model Builder** window, under **Global Definitions** click **Default Model Inputs**.
- 2 In the **Settings** window for **Default Model Inputs**, locate the **Browse Model Inputs** section.
- 3 Find the **Expression for remaining selection** subsection. In the **Volume reference temperature** text field, type 300[K].

## HEAT TRANSFER IN SOLIDS (HT)


### *Initial Values 1*

- 1 In the **Model Builder** window, under **Component 1 (comp1)>Heat Transfer in Solids (ht)** click **Initial Values 1**.
- 2 In the **Settings** window for **Initial Values**, locate the **Initial Values** section.
- 3 In the  $T$  text field, type  $T_{\text{gas}}$ .


### *Heat Flux 1*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Heat Flux**.
- 2 In the **Settings** window for **Heat Flux**, locate the **Boundary Selection** section.
- 3 From the **Selection** list, choose **Exchange Boundaries**.
- 4 Locate the **Heat Flux** section. Click the **Convective heat flux** button.
- 5 In the  $h$  text field, type 25.
- 6 In the  $T_{\text{ext}}$  text field, type  $T_{\text{work}}$ .


### *Heat Flux 2*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Heat Flux**.
- 2 In the **Settings** window for **Heat Flux**, locate the **Boundary Selection** section.
- 3 From the **Selection** list, choose **Cooling Duct**.
- 4 Locate the **Heat Flux** section. Click the **Convective heat flux** button.
- 5 In the  $h$  text field, type  $Nu_{\text{cool}} \cdot \mu_{\text{cool}} \cdot Cp_{\text{cool}} / 2 / Pr_{\text{cool}} / H_{\text{cool}}$ .
- 6 In the  $T_{\text{ext}}$  text field, type  $T_{\text{cool}}$ .


### *Heat Flux 3*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Heat Flux**.
- 2 Select Boundaries 137 and 163 only.
- 3 In the **Settings** window for **Heat Flux**, locate the **Heat Flux** section.
- 4 Click the **Convective heat flux** button.
- 5 From the **Heat transfer coefficient** list, choose **External forced convection**.
- 6 From the list, choose **Plate, local transfer coefficient**.
- 7 In the  $x_{\text{pl}}$  text field, type  $0.1675 - x$ .
- 8 In the  $U$  text field, type  $U_{\text{suction\_side}}$ .
- 9 In the  $p_{\Delta}$  text field, type  $p_{\text{high}}$ .
- 10 In the  $T_{\text{ext}}$  text field, type  $T_{\text{gas}}$ .

#### Heat Flux 4

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Heat Flux**.
- 2 Select Boundaries 136 and 312 only.
- 3 In the **Settings** window for **Heat Flux**, locate the **Heat Flux** section.
- 4 Click the **Convective heat flux** button.
- 5 From the **Heat transfer coefficient** list, choose **External forced convection**.
- 6 From the list, choose **Plate, local transfer coefficient**.
- 7 In the  $x_{pl}$  text field, type 0.1675-x.
- 8 In the  $U$  text field, type U\_pressure\_side.
- 9 In the  $p_A$  text field, type p\_high.
- 10 In the  $T_{ext}$  text field, type T\_gas.


#### Heat Flux 5

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Heat Flux**.
- 2 Select Boundaries 15, 21, 118–121, 164, 165, 232, 234, 235, 237, 286, 289–291, 306, 307, 315, 317, and 320 only.
- 3 In the **Settings** window for **Heat Flux**, locate the **Heat Flux** section.
- 4 Click the **Convective heat flux** button.
- 5 From the **Heat transfer coefficient** list, choose **External forced convection**.
- 6 From the list, choose **Plate, local transfer coefficient**.
- 7 In the  $x_{pl}$  text field, type 0.19-x.
- 8 In the  $U$  text field, type U\_platform.
- 9 In the  $p_A$  text field, type p\_high.
- 10 In the  $T_{ext}$  text field, type T\_gas.


### SOLID MECHANICS (SOLID)

In the **Model Builder** window, under **Component 1 (comp1)** click **Solid Mechanics (solid)**.

#### Roller 1

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Roller**.
- 2 Select Boundaries 140, 146, and 213 only.


#### Spring Foundation 1

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Spring Foundation**.
- 2 Select Boundaries 426 and 428 only.

- 3 In the **Settings** window for **Spring Foundation**, locate the **Spring** section.
- 4 From the list, choose **Diagonal**.
- 5 In the  $k_A$  table, enter the following settings:


1e9	0	0
0	0	0
0	0	0

#### *Spring Foundation 2*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Spring Foundation**.
- 2 Select Boundaries 82, 90, 192, and 255 only.
- 3 In the **Settings** window for **Spring Foundation**, locate the **Spring** section.
- 4 From the list, choose **Diagonal**.
- 5 In the  $k_A$  table, enter the following settings:

0	0	0
0	0	0
0	0	1e10

#### *Spring Foundation 3*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Spring Foundation**.
- 2 Select Boundary 17 only.
- 3 In the **Settings** window for **Spring Foundation**, locate the **Spring** section.
- 4 From the list, choose **Diagonal**.
- 5 In the  $k_A$  table, enter the following settings:

0	0	0
0	1e9	0
0	0	0

## **MESH I**

### *Size I*

In the **Model Builder** window, under **Component I (comp1)** right-click **Mesh I** and choose **Size**.

### Size

- 1 In the **Settings** window for **Size**, locate the **Element Size** section.
- 2 From the **Predefined** list, choose **Fine**.


### Size 1

- 1 In the **Model Builder** window, click **Size 1**.
- 2 In the **Settings** window for **Size**, locate the **Geometric Entity Selection** section.
- 3 From the **Geometric entity level** list, choose **Boundary**.
- 4 From the **Selection** list, choose **Cooling Duct**.
- 5 Locate the **Element Size** section. From the **Predefined** list, choose **Fine**.

### Free Tetrahedral 1

- 1 In the **Mesh** toolbar, click  **Free Tetrahedral**.
- 2 In the **Settings** window for **Free Tetrahedral**, click  **Build All**.

## STUDY 1

In the **Home** toolbar, click  **Compute**.

## RESULTS

### Stress (solid)

The first default plot shows the von Mises stress. Disable the deformation and create a max/min plot to display the critical point in the stator.

### Surface 1

- 1 In the **Model Builder** window, expand the **Stress (solid)** node, then click **Surface 1**.
- 2 In the **Settings** window for **Surface**, locate the **Expression** section.
- 3 In the **Expression** text field, type `solid.misesGp`.
- 4 From the **Unit** list, choose **MPa**.

### Deformation

- 1 In the **Model Builder** window, expand the **Surface 1** node.
- 2 Right-click **Deformation** and choose **Disable**.



### Marker 1

- 1 In the **Model Builder** window, right-click **Surface 1** and choose **Marker**.
- 2 In the **Settings** window for **Marker**, locate the **Display** section.
- 3 From the **Display** list, choose **Max**.



- 4 Locate the **Coloring and Style** section. From the **Background color** list, choose **From theme**.
- 5 Select the **Show frame** check box.



#### TABLE

- 1 Go to the **Table** window.
- 2 Click the  **Zoom Extents** button in the **Graphics** toolbar.
- 3 Click the  **Transparency** button in the **Graphics** toolbar.

The second default plot shows the temperature distribution [Figure 4](#).


#### RESULTS

##### *Temperature (ht)*



- 1 In the **Model Builder** window, under **Results** click **Temperature (ht)**.
- 2 In the **Settings** window for **3D Plot Group**, locate the **Plot Settings** section.
- 3 Clear the **Plot dataset edges** check box.
- 4 In the **Temperature (ht)** toolbar, click  **Plot**.
- 5 Click the  **Zoom Extents** button in the **Graphics** toolbar.

Finally, plot the displacement ([Figure 6](#)).

##### *Displacement*

- 1 In the **Home** toolbar, click  **Add Plot Group** and choose **3D Plot Group**.
- 2 In the **Settings** window for **3D Plot Group**, type Displacement in the **Label** text field.

##### *Volume 1*

- 1 Right-click **Displacement** and choose **Volume**.
- 2 In the **Settings** window for **Volume**, click **Replace Expression** in the upper-right corner of the **Expression** section. From the menu, choose **Component 1 (comp1)>Solid Mechanics>Displacement>solid.disp - Displacement magnitude - m**.
- 3 Locate the **Expression** section. From the **Unit** list, choose **mm**.
- 4 In the **Displacement** toolbar, click  **Plot**.
- 5 Click the  **Zoom Extents** button in the **Graphics** toolbar.

