

# INTRODUCTION TO Acoustics Module

# Introduction to the Acoustics Module

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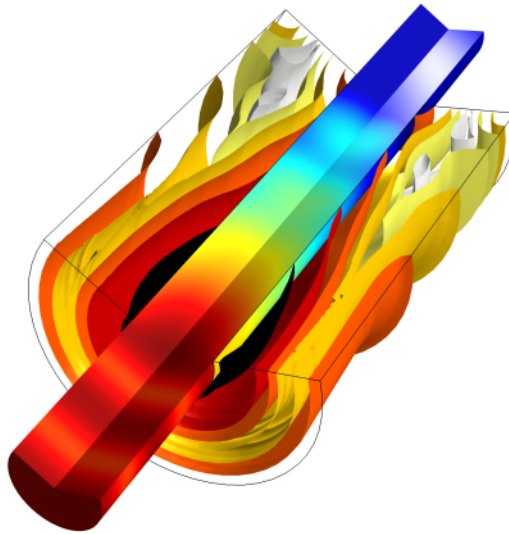
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## Introduction

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The Acoustics Module consists of a set of physics interfaces that enable you to simulate the propagation of sound in fluids and solids in a fully multiphysics-enabled environment. The available physics interfaces include pressure acoustics, elastic waves, acoustic-solid interaction, aeroacoustics (detailed convected acoustic models), thermoviscous acoustics, ultrasound, geometrical acoustics, and pipe acoustics. For acoustic analysis, covering the frequency range from infrasound to ultrasonics as well as many formulations of the underlying equations, the Acoustics Module incorporates four numerical methods, including finite elements (FEM), boundary elements (BEM), discontinuous Galerkin (dG-FEM), and ray tracing.



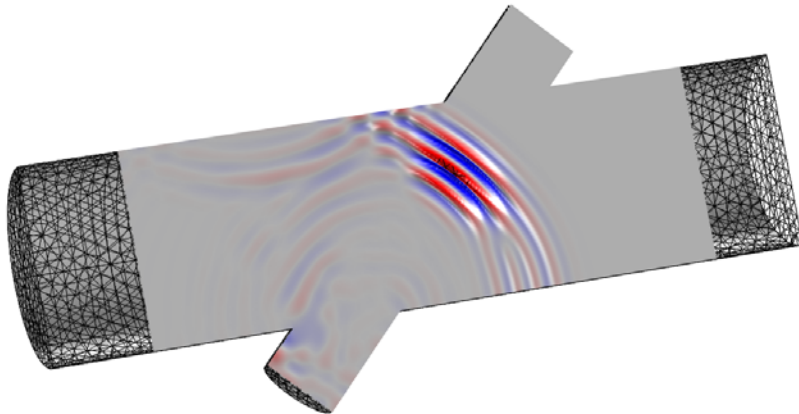
*Figure 1: COMSOL model of the sound pressure level distribution in a muffler system.*

Acoustic simulations using this module can easily solve classical problems such as scattering, diffraction, emission, radiation, and transmission of sound. These problems are relevant to muffler design, loudspeaker construction, sound insulation for absorbers and diffusers, the evaluation of directional acoustic patterns like directivity, noise radiation problems, and much more. The acoustic-structure multiphysics couplings enable modeling problems involving structure- and fluid-borne sound and their interaction. For example, acoustic-structure interaction is simulated for detailed muffler design, ultrasound piezo-actuators, sonar technology, and noise and vibration analysis of machinery

in the automotive industry. Using the capabilities of COMSOL Multiphysics it is also possible to analyze and design electroacoustic transducers such as loudspeakers, sensors, microphones, and hearing aid receivers. The propagation of elastic waves can be modeled in solids and porous materials as well as in coupled problems.

Aeroacoustic problems can be analyzed and modeled by solving the linearized potential flow equations, the linearized Euler equations, or the linearized Navier-Stokes equations. These equations are used to model the one-way interaction between an external flow and an acoustic field, so-called convected acoustics. Applications range from jet-engine noise analysis to simulating acoustic flow sensors, liner systems with bias and/or grazing flow, and mufflers with flow. The Thermoviscous Acoustics interfaces can accurately model systems having small geometrical dimensions where thermal and viscous boundary layer losses are important. This is relevant to the mobile phone and hearing aid industries, for all transducer designers, and for modeling the true properties of metamaterials. In the time domain nonlinear effects can also be included.

The Ultrasound branch includes two interfaces. The Convected Wave Equation, Time Explicit interface used to compute the transient propagation of linear ultrasound acoustic waves over large distances (relative to the wavelengths). The Nonlinear Pressure Acoustics, Time Explicit interface can be used to model the propagation of high amplitude nonlinear acoustic waves. The interfaces under the ultrasound branch are not restricted to high-frequency propagation but can, in general, be applied to any acoustically large problem.



*Figure 2: COMSOL model of an ultrasound flowmeter modeled using the Convected Wave Equation interface. The model includes interaction with a steady state background flow.*

Geometrical Acoustics includes the Ray Acoustics and the Acoustic Diffusion Equation interfaces. The physics are valid in the high-frequency limit where the

acoustic wavelength is much smaller than the characteristic geometric features. Both interfaces are suited for modeling acoustics in rooms and concert halls. The Ray Acoustics interface can also be used, for example, in outdoor scenarios.

- ▲ ))) Acoustics
  - ▲ ))) Pressure Acoustics
    - Pressure Acoustics, Frequency Domain (acpr)
    - Pressure Acoustics, Transient (actd)
    - Pressure Acoustics, Boundary Mode (acbm)
    - Pressure Acoustics, Boundary Elements (pabe)
    - Pressure Acoustics, Time Explicit (pate)
  - ▲ Elastic Waves
    - Solid Mechanics (Elastic Waves)
    - Poroelectric Waves (pelw)
    - Elastic Waves, Time Explicit (elte)
  - ▲ ))) Acoustic-Structure Interaction
    - Acoustic-Solid Interaction, Frequency Domain
    - Acoustic-Solid Interaction, Transient
    - Acoustic-Shell Interaction, Frequency Domain
    - Acoustic-Shell Interaction, Transient
    - Acoustic-Piezoelectric Interaction, Frequency Domain
    - Acoustic-Piezoelectric Interaction, Transient
    - Acoustic-Poroelastic Waves Interaction
    - Acoustic-Solid-Poroelastic Waves Interaction
    - Acoustic-Solid Interaction, Time Explicit
  - ▲ ))) Aeroacoustics
    - Linearized Euler, Frequency Domain (lef)
    - Linearized Euler, Transient (let)
    - Linearized Navier-Stokes, Frequency Domain (lnsf)
    - Linearized Navier-Stokes, Transient (lnst)
    - Linearized Potential Flow, Frequency Domain (ae)
    - Linearized Potential Flow, Transient (aetd)
    - Linearized Potential Flow, Boundary Mode (aebm)
    - Compressible Potential Flow (cpf)
  - ▲ ))) Thermoviscous Acoustics
    - Thermoviscous Acoustics, Frequency Domain (ta)
    - Thermoviscous Acoustics, Transient (tatd)
    - Thermoviscous Acoustics, Boundary Mode (tabm)
    - Acoustic-Thermoviscous Acoustic Interaction, Frequency Domain
    - Thermoviscous Acoustic-Solid Interaction, Frequency Domain
    - Thermoviscous Acoustic-Shell Interaction, Frequency Domain
  - ▲ ))) Ultrasound
    - Convected Wave Equation, Time Explicit (cwe)
    - Nonlinear Pressure Acoustics, Time Explicit (nate)
  - ▲ Ray Acoustics
    - Ray Acoustics (rac)
    - Acoustic Diffusion Equation (ade)
  - ▲ ))) Pipe Acoustics
    - Pipe Acoustics, Frequency Domain (pafd)
    - Pipe Acoustics, Transient (patd)

Figure 3: The Acoustics Module physics interfaces. Some physics interfaces require additional modules — both of the Acoustic-Shell Interaction interfaces and the Thermoviscous Acoustic-Shell Interaction interface require the Structural Mechanics Module.

The Acoustics Module is of great benefit for engineers. By using 3D simulations, existing products can be optimized and new products more quickly designed with virtual prototypes. Simulations also help designers, researchers, and engineers to gain insight into problems that are difficult to handle experimentally. Also, by optimizing a design virtually before real-life testing and manufacturing it, companies save time and money.

The physics interfaces available with this module are shown in [Figure 3](#) and are located under the Acoustics branch in the Model Wizard. The next section [The Acoustics Module Physics Interfaces](#) provides an overview of the physics interface functionality.

There are many application areas where these physics interfaces are used — from modeling simple pressure waves in air to examining complex interactions between elastic waves and pressure waves in porous materials. For a brief introduction to the basic concepts and theory of acoustics see the [Basics of Acoustics](#).

The Acoustics Module application library has many examples of applications ranging from modeling sound insulation lining, loudspeakers and microphones, to mufflers. These examples show, among other things, how to simulate acoustic losses. The loss models range from homogenized empirical fluid models for fibrous materials to those that include thermal and viscous losses in detail using the Thermoviscous Acoustics interface.







Predefined couplings can be used to model the interaction between acoustic, structural, and electric fields in piezoelectric materials (see [The Application Libraries Window](#) for information about accessing these files). You can also get started with your own COMSOL modeling by going to the tutorial [Example: Absorptive Muffler](#).

# The Acoustics Module Physics Interfaces

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There are eight main branches — Pressure Acoustics, Elastic Waves, Acoustic-Structure Interaction, Aeroacoustics, Thermoviscous Acoustics, Ultrasound, Geometrical Acoustics, and Pipe Acoustics — and each of the physics interfaces is briefly described here, followed by the [Physics Interface Guide by Space Dimension and Study Type](#) listing the physics interface availability by space dimension and preset study types.

## PRESSURE ACOUSTICS

The Pressure Acoustics branch (  ) has interfaces where the sound field is described the pressure  $p$ . The physics interface solves acoustic problems in the frequency domain using the Pressure Acoustics, Frequency Domain interface (  ), where the Helmholtz equation is solved. Transient systems are modeled using the Pressure Acoustics, Transient interface (  ), where the classical wave equation is solved. Nonlinear effects can be included here using the Nonlinear Acoustics (Westervelt) feature. The Boundary Mode Acoustics interface (  ) is used to study propagating modes in waveguides and ducts (at a given frequency only a finite set of wave shapes can propagate over a long distance). To efficiently solve large radiation and scattering problems the Pressure Acoustics, Boundary Element interface (  ) solves the Helmholtz equation using the boundary element method (BEM). The interface is fully multiphysics enabled and couples seamlessly with the finite element based interfaces, both acoustic and structural. The Pressure Acoustics, Time Explicit (  ) interface uses a time explicit method based on discontinuous Galerkin finite elements to efficiently solve large transient problems, it can be coupled to the Elastic Waves, Time Explicit interface.

A large variety of boundary conditions are available, including sound hard walls and conditions for applying sources. There are radiation, symmetry, periodic, and port conditions for modeling open boundaries. Impedance conditions include models for different parts of the human ear, human skin, simple RCL circuit models, and more. The physics interfaces also have several fluid models, which, in a homogenized way, mimic the behavior of sound propagation in more complex media. This includes the propagation in porous or fibrous materials (the Poroacoustics domain feature), the propagation in narrow structures of constant cross section (the Narrow Region Acoustics domain feature), and fluid models for defining bulk absorption behavior. Monopole, dipole, and quadrupole point sources can also be applied. So-called perfectly matched layers (PMLs) are also available to truncate an unbounded computational domain in both time and frequency domain. Finally, the exterior field calculation feature can be used to determine the pressure in any point outside the computational domain. Dedicated

results and analysis capabilities exist for visualizing the radiation pattern of the exterior field (near and far-field) in polar, 2D, and 3D plots.

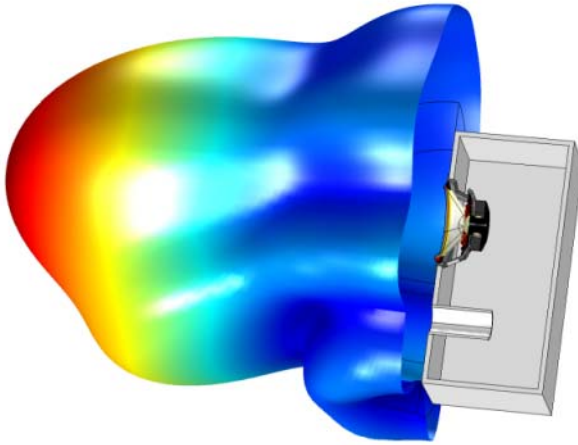






Figure 4: A 3D bubble plot of the loudspeaker radiation pattern at 3000 Hz. From the Vented Loudspeaker Enclosure model found in the application library.


## ELASTIC WAVES

The Elastic Waves branch (  ) includes single physics interfaces for modeling the propagation of linear elastic waves in solids and porous materials. If necessary, the interfaces are readily coupled to fluid domains using the built-in multiphysics couplings.










The physics interfaces under this branch are the:

- Solid Mechanics (Elastic Waves) (  ), for modeling elastic waves in solids. The Port boundary condition is specifically implemented to model and handle various propagating modes in elastic waveguide structures.
- Poroelectric Waves (  ), for precisely modeling the propagation of sound in a porous material. It includes the two-way coupling between deformation of the solid porous matrix and the pressure waves in the saturating fluid. The physics interface solves Biot's equations in the frequency domain. It includes two formulations for the loss mechanisms. The Biot (viscous losses) for modeling rocks and soils and the Biot–Allard (thermal and viscous losses) for sound absorbing materials in air.
- Elastic Waves, Time Explicit (  ), for modeling the propagation of linear elastic waves in solids using the discontinuous Galerkin, time explicit formulation. The interface is suited for modeling large problems with a memory efficient method.

## ACOUSTIC-STRUCTURE INTERACTION


The Acoustic-Structure Interaction branch () has interfaces that apply to phenomena where the fluid pressure causes a load on the solid domain, and the structural acceleration affects the fluid domain across the fluid-solid boundary.





The physics interfaces under this branch are the:

- Acoustic-Solid Interaction, Frequency Domain () and Acoustic-Solid Interaction, Transient () multiphysics interfaces.
- Acoustic-Shell Interaction, Frequency Domain () and Acoustic-Shell Interaction, Transient () multiphysics interfaces.
- Acoustic-Piezoelectric Interaction, Frequency Domain () and Acoustic-Piezoelectric Interaction, Transient () multiphysics interfaces, which support solving and modeling the electric field in a piezoelectric material. The piezoelectric coupling can be in stress-charge or strain-charge form.
- Acoustic-Solid-Poroelastic Waves Interaction () and Acoustic-Poroelastic Waves Interaction () multiphysics interfaces.
- Acoustic-Solid Interaction, Time Explicit () multiphysics interface.





The multiphysics interfaces consist of two or more single physics, for example, Pressure Acoustics, Frequency Domain and Solid Mechanics together with a multiphysics coupling, here the Acoustic-Structure Boundary coupling. Many more couplings are supported, for example, coupling Pressure Acoustics to Membrane or Multibody Dynamics interfaces.

## AEROACOUSTICS


Detailed convected acoustics (flow borne noise/sound) that simulates the one-way interaction of a background fluid flow with an acoustic field is modeled using the physics interfaces found under the Aeroacoustics branch (). The coupling between the fluid mechanics and the acoustics is based on solving the set of linearized governing equations using stabilized finite elements methods. In this way, you solve for the acoustic variations of the acoustic variables on top of a stationary background mean flow. Different physics interfaces exist that solve the governing equations under various physical approximations.

- The Linearized Navier-Stokes, Frequency Domain () and Linearized Navier-Stokes, Transient () interfaces are used for aeroacoustic simulations that can be described by the linearized Navier-Stokes equations solving for the acoustic variations in pressure, velocity, and temperature.
- The Linearized Euler, Frequency Domain interface () and the Linearized Euler, Transient interface () solve the Linearized Euler equations. They are used to compute the acoustic variations in density, velocity, and pressure




in the presence of a stationary background mean-flow that is well approximated by an ideal gas flow.


- The Linearized Potential Flow, Frequency Domain (  ) and the Linearized Potential Flow, Transient (  ) interfaces model the interaction of a stationary background potential flow with an acoustic field. These physics interfaces are only suited for cases where the flow is inviscid and, being irrotational, has no vorticity. The background flow is typically solved for using the Compressible Potential Flow interface (  ).
- The Linearized Potential Flow, Boundary Mode interface (  ) is used to study boundary mode acoustic problems in a background flow field. It is typically used to define sources at the inlet of ducts.

## THERMOVISCOUS ACOUSTICS



The physics interfaces under the Thermoviscous Acoustics branch (  ) are used to accurately model acoustics in geometries with small dimensions. Near walls viscous and thermal boundary layers (penetration depths) exist. Here, viscous losses due to shear and thermal conduction become important because of large gradients. For this reason, it is necessary to include thermal conduction effects and viscous losses explicitly in the governing equations. Thermoviscous acoustics is, for example, used when modeling the response of small transducers like microphones and receivers. Other applications include analyzing feedback in hearing aids and in mobile devices, or studying the damped vibrations of MEMS structures. In the time domain nonlinear effects can be modeled using the Nonlinear Thermoviscous Acoustics Contributions feature.

Because a detailed description is needed to model thermoviscous acoustics, the physics interface simultaneously solves for the acoustic pressure  $p$ , the particle velocity vector  $\mathbf{u}$ , and the acoustic temperature variation  $T$ .

In the Thermoviscous Acoustics, Frequency Domain interface (  ), the governing equations are implemented in the time-harmonic formulation and solved in the frequency domain. The interface is given in the scattered field formulation. Both mechanical and thermal boundary conditions exist. The interface exists in a time domain formulation, the Thermoviscous Acoustics, Transient interface (  ). The Thermoviscous Acoustics, Boundary Mode interface (  ) is used to compute and identify propagating and non-propagating modes in waveguides and ducts. The interface performs a boundary mode analysis on a boundary, inlet, or cross section of a waveguide or duct of small dimensions. Several multiphysics interfaces involving thermoviscous acoustics also exist:

- Acoustic-Thermoviscous Acoustic Interaction, Frequency Domain multiphysics interface (  ) that includes Pressure Acoustics, Frequency Domain and the Acoustics-Thermoviscous Acoustics Boundary coupling

feature. Coupling the thermoviscous acoustics domain to a pressure acoustics domain is also straightforward, with the predefined multiphysics condition.

- A Thermoviscous Acoustic-Solid Interaction, Frequency Domain multiphysics interface (  ) is available to solve coupled vibro-acoustic problems. This can, for example, be used to model small electroacoustic transducers or damping in MEMS devices. It includes Solid Mechanics and the predefined multiphysics coupling to Thermoviscous Acoustics.
- The Thermoviscous Acoustic-Shell Interaction, Frequency Domain multiphysics interface (  ) is used for modeling the interactions between shells and acoustics in small dimensions. This can, for example, be used to analyze the damped vibrations of shells in hearing aids and prevent feedback problems.

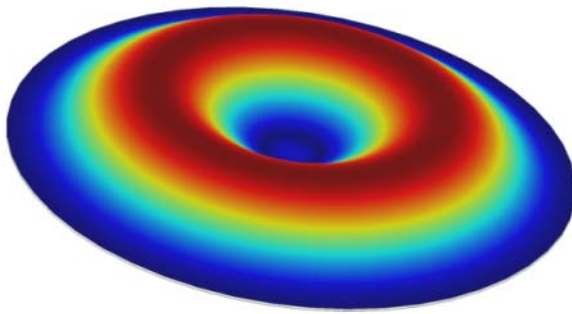





Figure 5: Deformation of the diaphragm (or membrane) at 12 kHz in the Axisymmetric Condenser Microphone model found in the application library.

## ULTRASOUND

Two dedicated interfaces exist under the Ultrasound branch (  ).

- The Convected Wave Equation, Time Explicit (  ) interface which is used to solve large transient linear acoustic problems containing many wavelengths in a stationary background flow. In general, the interface is suited for modeling the propagation of acoustic signals over large distances relative to the wavelength, for example, linear ultrasound problems. Application areas include ultrasound flowmeters and other ultrasound sensors where time of flight is an important parameter.
- The Nonlinear Pressure Acoustics, Time Explicit (  ) interface is used to model the propagation of high amplitude nonlinear acoustic waves. Special functionality exists to capture shocks. Application areas include biomedical

applications, for instance, ultrasonic imaging and high-intensity focused ultrasound (HIFU). The applications are not restricted to ultrasound.

Both interfaces include absorbing layers that are used to set up effective nonreflecting like boundary conditions. The interfaces are based on the discontinuous Galerkin method and uses a time explicit solver. The method is very memory lean.



## GEOMETRICAL ACOUSTICS

Two physics interfaces exist under the Geometrical Acoustics branch: the Acoustic Diffusion Equation interface and the Ray Acoustics interface. Both are used to model acoustics in the high frequency limit where the wavelength is significantly smaller than the characteristic geometrical features.

The Ray Acoustics physics interface is used to compute the trajectories, phase, and intensity of acoustic rays. The interface can be used to model room acoustic problems like concert halls, lecture halls, or car cabins, and many outdoor and underwater environments. The interface has a dedicated receiver dataset that is used to create an impulse response plot. Objective room acoustic metrics like clarity, definition, and reverberation time can be analyzed.








The Acoustic Diffusion Equation interface solves a diffusion equation for the acoustic energy density distribution for modeling indoor room acoustics in buildings and concert halls. It is also known as energy finite elements.








## PIPE ACOUSTICS













The Pipe Acoustics, Transient () and the Pipe Acoustics, Frequency Domain () interfaces are used to model the propagation of sound waves in 1D flexible pipe systems. The equations are formulated in a general way to include the effects of the pipe wall compliance and allow the possibility of a stationary background flow. The pipe interfaces can be coupled to pressure acoustics domains using the built-in Acoustic-Pipe Acoustics Connection multiphysics coupling.

## Physics Interface Guide by Space Dimension and Study Type












The table below lists the physics interfaces available specifically with this module in addition to those in the COMSOL Multiphysics basic license.



PHYSICS INTERFACE	ICON	TAG	SPACE DIMENSION	AVAILABLE STUDY TYPE
 <b>Acoustics</b>				
 <b>Pressure Acoustics</b>				
Pressure Acoustics, Frequency Domain <sup>1</sup>		acpr	all dimensions	eigenfrequency; frequency domain; frequency domain, modal; mode analysis (2D and 1D axisymmetric models only); boundary mode analysis (3D and 2D axisymmetric models only)
Pressure Acoustics, Transient		actd	all dimensions	eigenfrequency; frequency domain; frequency domain, modal; time dependent; time dependent, modal; mode analysis (2D and 1D axisymmetric models only)
Pressure Acoustics, Boundary Mode		acbm	3D, 2D axisymmetric	mode analysis
Pressure Acoustics, Boundary Elements		pabe	3D, 2D	frequency domain
Pressure Acoustics, Time Explicit		pate	3D, 2D, 2D axisymmetric	time dependent

PHYSICS INTERFACE	ICON	TAG	SPACE DIMENSION	AVAILABLE STUDY TYPE
 <b>Elastic Waves</b>				
Solid Mechanics (Elastic Waves) <sup>1</sup>		solid	3D, 2D, 2D axisymmetric	stationary; eigenfrequency; eigenfrequency, prestressed; mode analysis; time dependent; time dependent, modal; time dependent, prestressed, modal; time dependent, modal reduced-order model; frequency domain; frequency domain, modal; frequency domain, prestressed; frequency domain, prestressed, modal; frequency domain, modal reduced-order model; frequency domain, AWE reduced-order model; modal reduced-order model
Poroelectric Waves		pelw	3D, 2D, 2D axisymmetric	eigenfrequency; frequency domain; frequency domain, modal
Elastic Waves, Time Explicit		elte	3D, 2D, 2D axisymmetric	time dependent
 <b>Acoustic-Structure Interaction</b>				
Acoustic-Solid Interaction, Frequency Domain <sup>3</sup>		—	3D, 2D, 2D axisymmetric	eigenfrequency; frequency domain; frequency domain, modal
Acoustic-Solid Interaction, Transient <sup>3</sup>		—	3D, 2D, 2D axisymmetric	eigenfrequency; frequency domain; frequency domain, modal; time dependent; time dependent, modal

PHYSICS INTERFACE	ICON	TAG	SPACE DIMENSION	AVAILABLE STUDY TYPE
Acoustic-Shell Interaction, Frequency Domain <sup>2,3</sup>		—	3D, 2D axisymmetric	eigenfrequency; frequency domain; frequency domain, modal
Acoustic-Shell Interaction, Transient <sup>2, 3</sup>		—	3D, 2D axisymmetric	eigenfrequency; frequency domain; frequency domain, modal; time dependent; time dependent, modal
Acoustic-Piezoelectric Interaction, Frequency Domain <sup>3</sup>		—	3D, 2D, 2D axisymmetric	eigenfrequency; frequency domain; frequency domain, modal
Acoustic-Piezoelectric Interaction, Transient <sup>3</sup>		—	3D, 2D, 2D axisymmetric	eigenfrequency; frequency domain; frequency domain, modal; time dependent; time dependent, modal
Acoustic-Solid-Poroelastic Waves Interaction <sup>3</sup>		—	3D, 2D, 2D axisymmetric	eigenfrequency; frequency domain; frequency domain, modal
Acoustic-Poroelastic Waves Interaction <sup>3</sup>		—	3D, 2D, 2D axisymmetric	eigenfrequency; frequency domain; frequency domain, modal
Acoustic-Solid Interaction, Time Explicit		—	3D, 2D	time domain
 <b>Aeroacoustics</b>				
Linearized Euler, Frequency Domain		lef	3D, 2D, 2D axisymmetric, 1D	frequency domain; eigenfrequency
Linearized Euler, Transient		let	3D, 2D, 2D axisymmetric, 1D	time dependent
Linearized Potential Flow, Frequency Domain		ae	all dimensions	frequency domain; mode analysis (2D and 1D axisymmetric models only)
Linearized Potential Flow, Transient		aetd	all dimensions	frequency domain; time dependent; mode analysis (2D and 1D axisymmetric models only)

PHYSICS INTERFACE	ICON	TAG	SPACE DIMENSION	AVAILABLE STUDY TYPE
Linearized Potential Flow, Boundary Mode		aebm	3D, 2D axisymmetric	mode analysis
Compressible Potential Flow		cpf	all dimensions	stationary; time dependent
Linearized Navier-Stokes, Frequency Domain		lnsf	3D, 2D, 2D axisymmetric, 1D	frequency domain; eigenfrequency
Linearized Navier-Stokes, Transient		lnst	3D, 2D, 2D axisymmetric, and 1D	time dependent
<b>))) Thermoviscous Acoustics</b>				
Thermoviscous Acoustics, Frequency Domain		ta	all dimensions	eigenfrequency; frequency domain; frequency domain, modal; mode analysis (2D and 1D axisymmetric models only)
Thermoviscous Acoustics, Transient		tatd	all dimensions	time dependent
Thermoviscous Acoustics, Boundary Mode		tabm	3D, 2D axisymmetric	mode analysis
Acoustic-Thermoviscous Acoustic Interaction, Frequency Domain <sup>3</sup>		—	3D, 2D, 2D axisymmetric	eigenfrequency; frequency domain; frequency domain, modal; boundary mode analysis (3D and 2D axisymmetric only); mode analysis (2D only)
Thermoviscous Acoustic-Solid Interaction, Frequency Domain <sup>3</sup>		—	3D, 2D, 2D axisymmetric	eigenfrequency; frequency domain; frequency domain, modal; mode analysis (2D only)
Thermoviscous Acoustic-Shell Interaction, Frequency Domain <sup>2,3</sup>		—	3D	eigenfrequency; frequency domain; frequency domain, modal

PHYSICS INTERFACE	ICON	TAG	SPACE DIMENSION	AVAILABLE STUDY TYPE
 <b>Ultrasound</b>				
Convected Wave Equation, Time Explicit		cwe	3D, 2D, 2D axisymmetric	time dependent
Nonlinear Acoustics, Time Explicit		nate	3D, 2D, 2D axisymmetric	time dependent
 <b>Geometrical Acoustics</b>				
Ray Acoustics		rac	3D, 2D, 2D axisymmetric	ray tracing; time dependent
Acoustic Diffusion Equation		ade	3D	eigenvalue; stationary; time dependent
 <b>Pipe Acoustics</b>				
Pipe Acoustics, Frequency Domain		pafd	3D, 2D	eigenfrequency; frequency domain
Pipe Acoustics, Transient		patd	3D, 2D	time dependent
 <b>Structural Mechanics</b>				
Solid Mechanics <sup>1</sup>		solid	3D, 2D, 2D axisymmetric	stationary; eigenfrequency; eigenfrequency, prestressed; mode analysis; time dependent; time dependent, modal; time dependent, prestressed, modal; time dependent, modal reduced-order model; frequency domain; frequency domain, modal; frequency domain, prestressed; frequency domain, prestressed, modal; frequency domain, modal reduced-order model; frequency domain, AWE reduced-order model

PHYSICS INTERFACE	ICON	TAG	SPACE DIMENSION	AVAILABLE STUDY TYPE
Piezoelectricity <sup>3</sup>		—	3D, 2D, 2D axisymmetric	stationary; eigenfrequency; eigenfrequency, prestressed; time dependent; time dependent, modal; time dependent, prestressed, modal; frequency domain; frequency domain, modal; frequency domain, prestressed; frequency domain, prestressed, modal; small-signal analysis, frequency domain
Magnetostriction <sup>3,4</sup>		—	3D, 2D, 2D axisymmetric	stationary; eigenfrequency; time dependent; frequency domain; small-signal analysis, frequency domain; eigenfrequency, prestressed; frequency domain, prestressed

<sup>1</sup> This physics interface is included with the core COMSOL package but has added functionality for this module.




<sup>2</sup> Requires both the Structural Mechanics Module and the Acoustics Module.








<sup>3</sup> This physics interface is a predefined multiphysics coupling that automatically adds all the physics interfaces and coupling features required.


<sup>4</sup> Requires the addition of the AC/DC Module.


## The Application Libraries Window

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To open an Acoustics Module application library model or tutorial, in the File menu click Application Libraries . In the Application Libraries window that opens, expand the Acoustics Module folder and browse or search the contents. Click Open Application  to open it in COMSOL Multiphysics or click Open PDF Document  to read background information including the step-by-step instructions to build it. The MPH-files in the COMSOL application library can have three formats — solved, compact, or preview MPH-files.

- Solved MPH-files, including all meshes and solutions. In the Application Libraries window these appear with the  icon. If the MPH-file's size exceeds 25MB, a tip with the text “Large file” and the file size appears when you position the cursor at the model's node in the Application Libraries tree.
- Compact MPH-files with all settings for the model but without built meshes and solution data to save space (a few MPH-files have no solutions for other reasons). You can open these to study the settings and to mesh and re-solve the applications. It is also possible to download the full versions — with meshes and solutions — of most of these when you update your application library. These appear in the Application Libraries window with the  icon and for runnable applications, this icon (  ). If you position the cursor at a compact file in the Application Libraries window, a No solutions stored message appears. If a full MPH-file is available for download, the corresponding node's context menu includes a Download File with Solutions (  ) option.
- Preview MPH-files (  ) are not actual model MPH-files. They just contain the information needed to present a model in the Application Libraries window. To get the actual model, choose Download File with Solutions (  ) or Download File Without Solutions (  ) from the node's context menu.

To check all available Application Libraries updates, select Update COMSOL Application Library (  ) either from the top of the Application Libraries window, from the File>Help menu (Windows users), or from the Help menu (Mac and Linux users).

To find further examples, available on the COMSOL homepage, click the Application Galley (  ) button. The gallery contains all the library models and many more. It is a great location for finding resources on various acoustic topics.

Get started with the [Example: Absorptive Muffler](#). The last section, [Additional Examples from the Application Libraries](#), provides a brief overview of some of the other models also available in the Acoustics Module Application Libraries.

## Basics of Acoustics

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Acoustics is the physics of sound. Sound is the sensation, as detected by the ear, of very small rapid changes in the acoustic pressure  $p$  above and below a static value  $p_0$ . This static value is the atmospheric pressure (about 100,000 pascals).

The amplitude of the small pressure variations that can be detected by the human ear vary from roughly  $2 \cdot 10^{-5}$  Pa at the hearing threshold to 20 Pa for jet engine noise. The amplitude at normal speech levels is about 0.02 Pa. The amplitudes described here are often given on a logarithmic decibel scale, relative to the hearing threshold value of  $2 \cdot 10^{-5}$  Pa, in units of dB SPL.

The acoustic pressure variations are typically described as pressure waves propagating in space and time. The wave crests are the pressure maxima while the troughs represent the pressure minima.

In more general terms, sound is created when the fluid is disturbed by a source. An example is a vibrating object, such as a speaker cone in a sound system. It is possible to see the movement of a bass speaker cone when it generates sound at a very low frequency. As the cone moves forward it compresses the air in front of it, causing an increase in air pressure. Then it moves back past its resting position and causes a reduction in air pressure. This process continues, radiating a wave of alternating high and low pressure at the speed of sound.

The frequency  $f$  (SI unit: Hz = 1/s) is the number of vibrations (pressure peaks) perceived per second and the wavelength  $\lambda$  (SI unit: m) is the distance between two such peaks. The speed of sound  $c$  (SI unit: m/s) is given as the product of the frequency and the wavelength,  $c = \lambda f$ . It is often convenient to define the angular frequency  $\omega$  (SI unit: rad/s) of the wave, which is  $\omega = 2\pi f$ , and relates the frequency to a full  $360^\circ$  phase shift. The wave number  $k$  (SI unit: rad/m) is defined as  $k = 2\pi/\lambda$ . The wave number, which is the number of waves over a specific distance, is also usually defined as a vector  $\mathbf{k}$ , such that it also contains information about the direction of propagation of the wave, with  $|\mathbf{k}| = k$ . In general, the relation between the angular frequency  $\omega$  and the wave number  $k$  is called the dispersion relation; for simple fluids it is  $\omega/k = c$ .

### Governing Equations

The equations that describe the propagation of sound in fluids are derived from the governing equations of fluid flow. That is, conservation of mass, which is described by the continuity equation; the conservation of momentum, which is often referred to as the Navier-Stokes equations; an energy conservation equation; the constitutive equations of the model; and an equation of state to describe the relation between thermodynamic variables. In the classical case of pressure acoustics, which describes most acoustic phenomena accurately, the flow is

assumed lossless and adiabatic, viscous effects are neglected, and a linearized isentropic equation of state is used.

Under these assumptions, the acoustic field is described by one variable, the pressure  $p$  (SI unit: Pa), and is governed by the wave equation

$$\frac{1}{\rho_0 c^2} \frac{\partial^2 p}{\partial t^2} + \nabla \cdot \left( -\frac{1}{\rho_0} \nabla p \right) = 0$$

where  $t$  is time (SI unit: s),  $\rho_0$  is the density of the fluid (SI unit: kg/m<sup>3</sup>), and  $c$  is the (adiabatic) speed of sound (SI unit: m/s).

Acoustic problems often involve simple harmonic waves such as sinusoidal waves. More generally, any signal may be expanded into harmonic components via its Fourier series. The wave equation can then be solved in the frequency domain for one frequency at a time. A harmonic solution has the form

$$p(\mathbf{x}, t) = p(\mathbf{x}) \sin(\omega t)$$

where the spatial  $p(\mathbf{x})$  and temporal  $\sin(\omega t)$  components are split. The pressure may be written in a more general way using complex variables

$$p(\mathbf{x}, t) = p(\mathbf{x}) e^{i\omega t} \quad (1)$$

where the actual (instantaneous) physical value of the pressure is the real part of [Equation 1](#). Using this assumption for the pressure field, the time-dependent wave equation reduces to the well-known Helmholtz equation

$$\nabla \cdot \left( -\frac{1}{\rho_0} \nabla p \right) - \frac{\omega^2}{\rho_0 c^2} p = 0 \quad (2)$$

In the homogeneous case, one simple solution to the Helmholtz equation ([Equation 2](#)) is the plane wave

$$p = P_0 e^{i(\omega t - \mathbf{k} \cdot \mathbf{x})} \quad (3)$$

where  $P_0$  is the wave amplitude, and it is moving in the  $\mathbf{k}$  direction with angular frequency  $\omega$  and wave number  $k = |\mathbf{k}|$ .

In most practical situations, an exact analytical solution to [Equation 2](#) does not exist. Solving the equation requires a numerical approach using simulations.

## Numerical Methods

As mentioned, solving the governing equations for the acoustic problems analytically — like, for example, the Helmholtz equation ([Equation 2](#)) — is only possible in a few simple situations. In order to solve real-life industrial problems,

which can very well be multiphysics problems involving several coupled physics, numerical methods are necessary. This is the job of COMSOL Multiphysics. In the Acoustics Module, most of the physics interfaces are based on the finite element method (FEM). In order to extend the range of models that can be solved, the Acoustics Module also includes the Pressure Acoustics, Boundary Elements interface based on BEM, two interfaces based on the discontinuous Galerkin (dG-FEM) method, and Ray Acoustics that uses a ray tracing method.

Solving a model using FEM requires a computational mesh. The solution is approximated on each mesh element (the finite elements) by a shape function (a local basis or interpolation function). Setting up this system of mesh elements and local shape functions leads to a discrete vector-matrix problem that needs to be solved. After solving the matrix problem with an adequate method, the solution to the original problem can be reconstructed. When solving wave problems numerically, one should be aware of the time and length scales involved in the problem, as will be discussed below.

### *Length and Time Scales*

When solving acoustic problems, it is important to think about the different basic length and time scales involved in the system. Some of the scales are set by the physics of the problem, while others are set by the numerical solution method. The relative size of these scales may influence the accuracy of the solution but also the selection of the physics interface used to model the problem.

When working with acoustics in the frequency domain, that is, solving the Helmholtz equation, only one time scale  $T$  exists (the period) and it is set by the frequency,  $T = 1/f$ . Several length scales exist: the wavelength  $\lambda = c/f$ , the smallest geometric dimension  $L_{\min}$ , the mesh size  $h$ , and the thickness of the acoustic boundary layer  $\delta$  (the latter is discussed in [Models with Losses](#)). In order to get an accurate solution, the mesh should be fine enough to both resolve the geometric features and the wavelength. As a rule of thumb, the maximal mesh size should be less than or equal to  $\lambda/N$ , where  $N$  is a number between 5 and 10, and depends on the spatial discretization.

Note that when the wavelength becomes smaller than the characteristic length scale in the model, the two interfaces in Geometrical Acoustics can be used. The equations solved here do not require the same mesh constraints and can be used to model much larger systems (measured in wavelengths) compared to solving, for example, the Helmholtz equation.

For transient acoustic problems the same considerations apply. However, several new time scales are also introduced. One is given by the frequency contents of the signal and by the desired maximal frequency resolution:  $T = 1/f_{\max}$ . The other is given by the size of the time step  $\Delta t$  used by the numerical solver. A condition on

the so-called CFL condition dictates the relation between the time step size and the minimal mesh size  $h_{\min}$ , the Courant number is defined as

$$C_{\text{CLF}} = \frac{c \Delta t}{h_{\min}} \quad (4)$$

where  $c$  is the speed of sound in the system. For all the transient interfaces available with the Acoustics Module the solver is automatically set up to fulfill this criterion. For the interfaces based on FEM the condition is interpreted to achieve an adequate balance between resolution in time and space. The user is only required to enter the maximal frequency  $f_{\max}$  to be resolved by the model. For the dG-FEM based interfaces the condition is used explicitly to achieve both accuracy and stability.

In order to run accurate acoustic simulations, it is important to think about these physical and numerical scales and about their influence on the convergence and correctness of the numerical solution. A good practical approach is to test the robustness of a solution compared to changes in the mesh in all cases and the numerical time stepping in the transient problems. If some measure of the solution, within a given accuracy range, changes when the mesh is refined then the mesh was probably not good enough.

### ***Boundary Conditions***

Boundary conditions define the nature of the boundaries of the computational domain. Some define real physical obstacles, like a sound hard wall or a moving interface. Others, called artificial boundary conditions, are used to truncate the domain. The artificial boundary conditions are, for example, used to simulate an open boundary where no sound is reflected. It may also mimic a reacting boundary such as a perforated plate.

### ***Elastic Waves***

The propagation of sound in solids happens through small-amplitude elastic oscillations of the solids shape and structure. These elastic waves are transmitted to surrounding fluids as ordinary sound waves. Through acoustic-structure interaction, the fluid pressure causes a fluid load on the solid domain, and the structural acceleration affects the fluid domain as a normal acceleration across the fluid-solid boundary.

The Acoustics Module has the Poroelastic Waves interface available to model poroelastic waves that propagate in porous materials. These waves result from the complex interaction between acoustic pressure variations in the saturating fluid and the elastic deformation of the solid porous matrix.

## Models with Losses

In order to accurately model acoustics in geometries with small dimensions, it is necessary to include thermal conduction effects and viscous losses explicitly in the governing equations. Near walls, viscosity and thermal conduction become important because the acoustic field creates viscous and thermal boundary layers where losses are significant. A detailed description is needed to model these phenomena; the dedicated Thermoviscous Acoustics, Frequency Domain interface solves the full linearized Navier-Stokes, continuity, and energy equations simultaneously. The physics interface solves for the acoustic pressure  $p$ , the particle velocity vector  $\mathbf{u}$ , and the acoustic temperature variation  $T$ . These are the acoustic variations on top of the mean background values.

The length scale at which the thermoviscous acoustic description is necessary is given by the thickness of the viscous (v) and thermal (th) boundary layers

$$\delta_v = \sqrt{\frac{\mu}{\pi f \rho}} \quad \delta_{th} = \sqrt{\frac{k}{\pi f \rho C_p}}$$

where  $\mu$  is the dynamic viscosity,  $k$  is the coefficient of thermal conduction, and  $C_p$  is the specific heat capacity at constant pressure. These two length scales define an acoustic boundary layer that needs to be resolved by the computational mesh.

Another way to introduce losses in the governing equations is to use the equivalent fluid models available in the pressure acoustics interfaces. In a homogenized way, this introduces attenuation properties to the bulk fluid that mimic different loss mechanisms. This is in contrast to the thermoviscous acoustics interfaces that model losses explicitly where they happen, that is, in the acoustic boundary layer near walls. The fluid models include losses due to bulk thermal conduction and viscosity (in the main Pressure Acoustics domain feature), models for simulating the damping in certain porous materials (in the Poroacoustics domain feature), and models to mimic the boundary absorption losses in long narrow ducts (the Narrow Region Acoustics domain feature). When applicable, the equivalent fluid models are computationally much less heavy than, for example, solving a corresponding full poroelastic model.

## Geometrical Acoustics

At high frequencies when the wavelength is much smaller than the characteristic geometric features, it is impractical to solve acoustic problems using pressure acoustics. Here, other methods are used like, for example, ray methods or energy diffusion analogies. These are known as geometrical acoustics methods and are used for modeling room acoustics, concert hall acoustics, and outdoor

propagation over large distances. The Geometrical Acoustics branch includes the Ray Acoustics and the Acoustic Diffusion Equation interfaces.

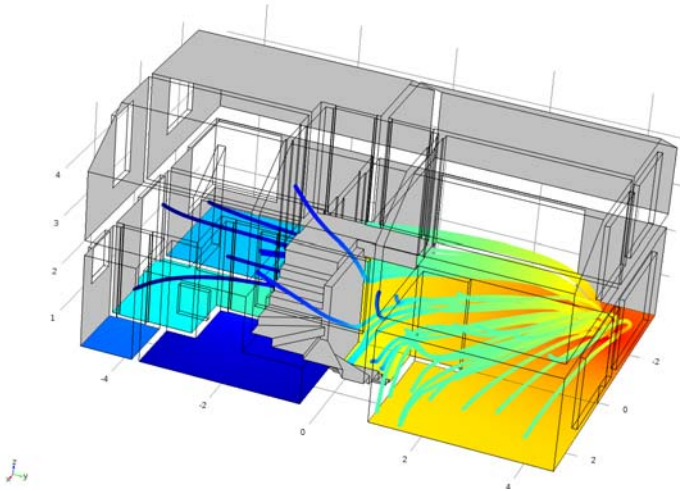


Figure 6: Sound pressure level and energy flux inside a two story house modeled using the Acoustic Diffusion Equation physics interface. Figure taken from the One-Family House Acoustics model found in the Application Gallery on comsol.com.

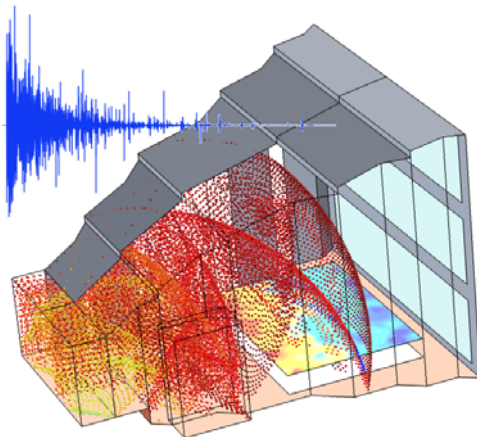


Figure 7: Ray tracing model of a small concert hall including the ray location at 0.02 s, the SPL distribution at the seat locations, and a schematic plot of the impulse response (inset). Figure taken from the Small Concert Hall Acoustics model found in the Application Gallery on comsol.com.

## Example: Absorptive Muffler

This example describes the pressure-wave propagation in a muffler for an internal combustion engine. The approach used here is generally applicable to analyzing the damping of propagating pressure waves as well as determining the transmission properties of a given system. The model uses the port boundary conditions to model the inlet and outlet of the muffler. The model shows how to analyze both inductive and resistive damping in pressure acoustics. The main output is the transmission loss for the frequency range 50 Hz–1500 Hz. It is represented both as a continuous curve and given in 1/3 octave bands.

### Model Definition

The muffler, schematically shown in the figure below, consists of a 24-liter resonator chamber with a section of the centered exhaust pipe included at each end. The model is first set up assuming that the chamber is empty. Secondly, it is lined with 15 mm of absorbing glass wool.

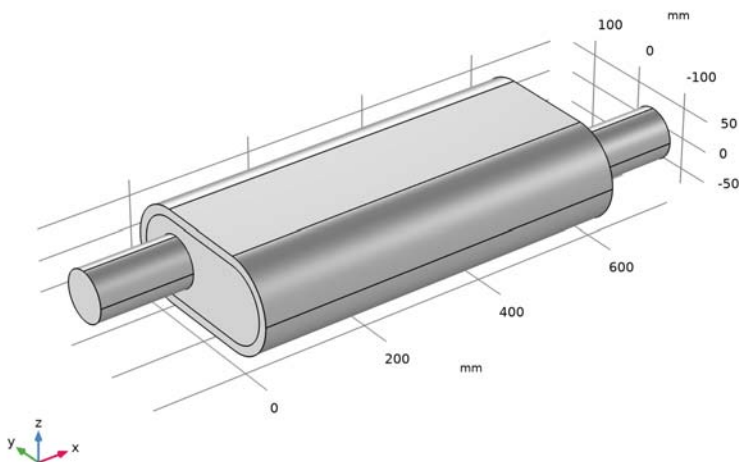


Figure 8: Geometry of the lined muffler; the liner is the outer layer in the main muffler volume. The exhaust fumes enter through the left pipe and exit through the right pipe.

### Domain Equations

This model solves the problem in the frequency domain using the Pressure Acoustics, Frequency Domain interface. The model equation is a slightly modified version of the Helmholtz equation for the acoustic pressure  $p$ :

$$\nabla \cdot \left( -\frac{\nabla p}{\rho} \right) - \frac{\omega^2 p}{c^2 \rho} = 0$$

where  $\rho$  is the density,  $c$  is the speed of sound, and  $\omega$  gives the angular frequency. The subscript  $c$  refers to that these can be complex valued.

In the absorbing glass wool, modeled as a Poroacoustics domain, the damping enters the equation as a complex speed of sound,  $c_c = \omega/k_c$ , and a complex density,  $\rho_c = k_c Z_c/\omega$ , where  $k_c$  is the complex wave number and  $Z_c$  equals the complex impedance. This is a so-called equivalent fluid model for the porous domain where the losses are modeled in a homogenized way.

For a highly porous material with a rigid skeleton, the classical empirical Delany and Bazley model estimates these parameters as functions of frequency and flow resistivity. Using the original coefficients of Delany and Bazley (Ref. 1), the expressions are

$$k_c = k_a \cdot \left( 1 + 0.098 \cdot \left( \frac{\rho_a f}{R_f} \right)^{-0.7} - i \cdot 0.189 \cdot \left( \frac{\rho_a f}{R_f} \right)^{-0.595} \right)$$

$$Z_c = Z_a \cdot \left( 1 + 0.057 \cdot \left( \frac{\rho_a f}{R_f} \right)^{0.734} - i \cdot 0.087 \cdot \left( \frac{\rho_a f}{R_f} \right)^{-0.732} \right)$$

where  $R_f$  is the flow resistivity, and where  $k_a = \omega/c_a$  and  $Z_a = \rho_a c_a$  are the free-space wave number and impedance of air, respectively. This model is the default selected for the Delany-Bazley-Miki model in the Poroacoustics domain feature. You can find flow resistivities in tables, see for example Ref. 3 or by measuring it. For glass-wool-like materials, Bies and Hansen (Ref. 2) give an empirical correlation

$$R_f = \frac{3.18 \cdot 10^{-9} \cdot \rho_{ap}^{1.53}}{d_{av}^2}$$

where  $\rho_{ap}$  is the material's apparent density and  $d_{av}$  is the mean fiber diameter. This model uses a lightweight glass wool with  $\rho_{ap} = 12 \text{ kg/m}^3$  and  $d_{av} = 10 \text{ }\mu\text{m}$ .

**Note:** The Delany-Bazley model is valid for values of  $(\rho_f)/R_f$  up to  $(\rho_f)/R_f \approx 1$ , so the upper frequency limit of 1500 Hz ensures that the poroacoustics model applies. Other variants of the Delany-Bazley model are built into the Acoustics Module; these have different validity regions or are used for other fibrous materials. For example, the Miki parameters can be selected; they extend the region of applicability of the Delany-Bazley constants.

## Boundary Conditions

- At the solid boundaries, which are the outer walls of the resonator chamber and the pipes, the model uses sound hard (wall) boundary conditions. The condition imposes that the normal velocity at the boundary is zero.
- The model uses port boundary conditions to model the inlet and outlet of the muffler. In waveguides, the port conditions are superior to radiation condition as they can capture complex wave fields that involve several propagating modes. In this model, only plane waves propagation is considered. This means that only one port condition needs to be added at each end. The port uses a plane wave (0,0) mode. If the analysis is carried out above the cutoff frequency of the first non-plane mode (above 2540 Hz), then simply add more port conditions at the inlet and outlet to capture these modes. Note that each port condition generates a post processing variable that defines the cutoff frequency of its mode, for example, for Port 1 the variable is `acpr.port1.fc`. The plane wave cutoff frequency is of course 0 Hz.

## Results and Discussion

The pressure distribution in the absorptive muffler without the lining material is shown in Figure 9 for the frequency  $f = 1500$  Hz. From the figure, it is seen that at this frequency not only longitudinal standing waves exist but also transverse modes are present.

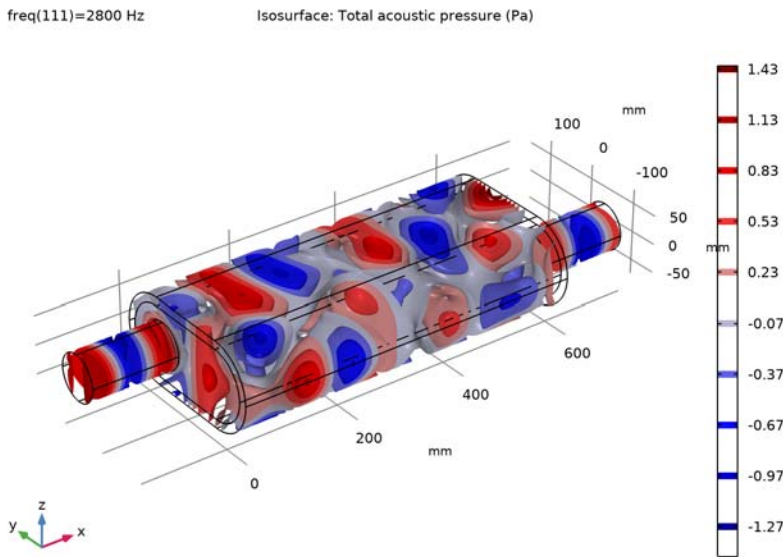


Figure 9: The pressure distribution in the absorptive muffler without the liner is shown for  $f = 1500$  Hz.

An important parameter for a muffler is the transmission loss or attenuation. It is defined as the ratio between the incoming and outgoing acoustic energy. The attenuation or transmission loss  $L$  (in dB) of the acoustic energy is defined by

$$L = 10 \log \left( \frac{P_{\text{in}}}{P_{\text{out}}} \right)$$

Here  $P_{\text{in}}$  and  $P_{\text{out}}$  denote the incoming power at the inlet and the outgoing power at the outlet, respectively. These values are readily defined by the port boundary conditions as `acpr.port1.P_in` and `acpr.port2.P_out` and can be directly used in postprocessing.

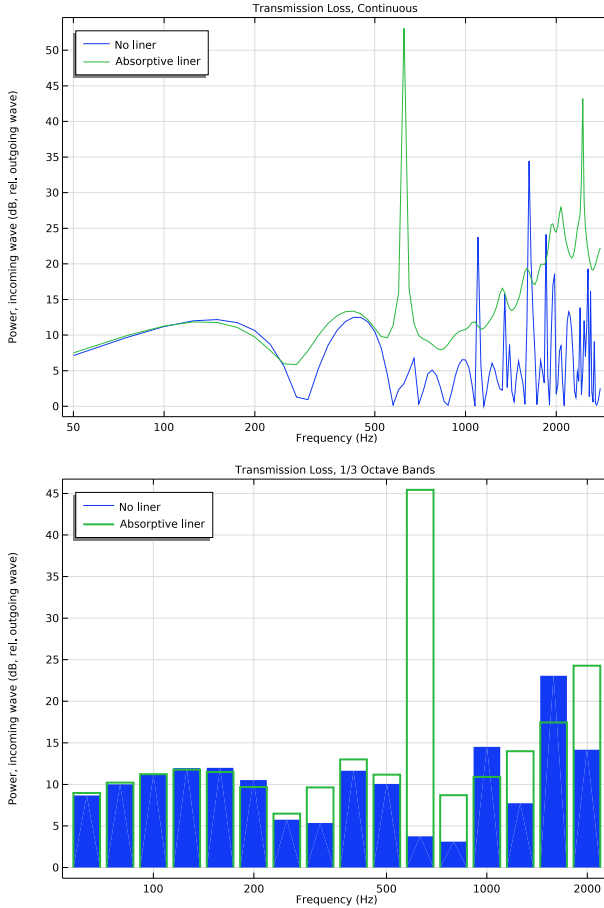


Figure 10: Comparison of the transmission loss as function of frequency for the empty muffler and the muffler with absorptive lining. (top) The transmission loss depicted as a continuous curve, and (bottom) The same data but depicted in 1/3 octave bands.

Figure 10 (top and bottom) shows the result of a parametric frequency study. The two graphs represent the case of an empty muffler without any absorbing lining material (blue lines) and the case with a layer of glass wool lining on the chamber's walls (green lines). The first four dips are due to longitudinal resonances. In the muffler with absorbing lining, the dips are still present, but the general trend is that the higher the frequency, the better the damping. In the top figure, the transmission loss is depicted as a continuous curve (pure tone sweep) while it is depicted in 1/3 octave bands in the bottom figure. Both graphs are created using the Octave Band Plot of the Acoustics Module.

The graph for the undamped muffler shows that damping works rather well for most low frequencies. At frequencies higher than approximately 1250 Hz, the plot's behavior is more complicated and there is generally less damping. This is because the tube supports not only longitudinal resonances but also cross-sectional propagating modes, for such frequencies. Not very far above this frequency a whole range of modes that are combinations of this propagating mode and the longitudinal modes participate, making the damping properties increasingly unpredictable. For an analysis of these modes, see the related model *Eigenmodes in a Muffler*. The glass-wool lining improves attenuation at the resonance frequencies as well as at higher frequencies.

The flow of energy in the muffler without the liner is shown in Figure 11 at 1500 Hz. The plot represents the intensity field depicted as streamlines. The intensity field is per definition the time average of the energy flux (instantaneous intensity) and thus represents the average energy flow in the system: here from the inlet to the outlet. Change between solutions and frequencies to study and visualize the sound-absorbing properties of the muffler.

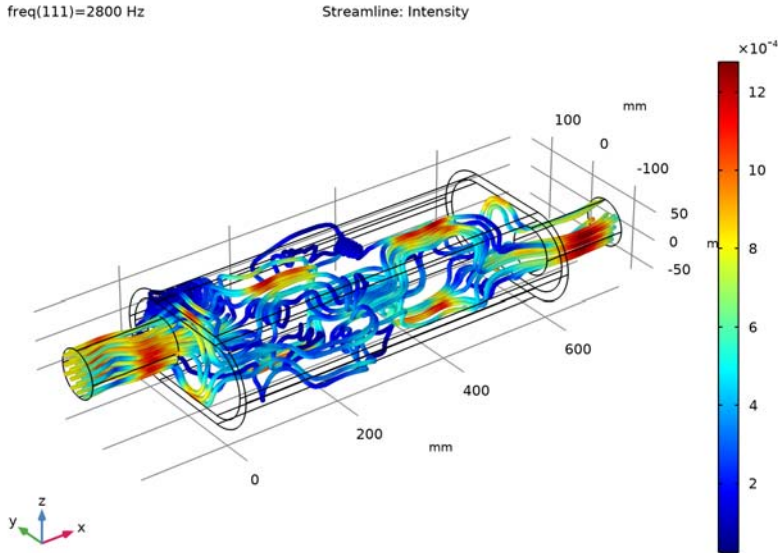


Figure 11: Intensity streamlines at 1500 Hz without the liner.

## References

1. M. A. Delany and E. N. Bazley, “Acoustic Properties of Fibrous Absorbent Materials,” *Appl. Acoust.*, vol. 3, pp. 105–116, 1970.
2. D. A. Bies and C. H. Hansen, “Flow Resistance Information for Acoustical Design,” *Appl. Acoust.*, vol. 13, pp. 357–391, 1980.
3. T. J. Cox and P. D’Antonio, *Acoustic Absorbers and Diffusers*, Second Edition, Taylor and Francis, 2009.

## Step-by-Step Instructions

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The first part of the model instructions (below) describe how to set up and postprocess the Absorptive Muffler model followed by the [Geometry Sequence Instructions](#) section where the geometry is set up; for simplicity, the geometry sequence is imported in the model instructions.



## Model Wizard

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The instructions take you through two versions of the model, first with a completely hollow chamber with rigid walls, then where the chamber is lined with glass wool.

**Note:** These instructions are for the user interface on Windows but apply, with minor differences, also to Linux and Mac.

- 1 To start the software, double-click the COMSOL icon on the desktop. When the software opens, you can choose to use the Model Wizard to create a new COMSOL model or Blank Model to create one manually. For this tutorial, click the Model Wizard button.

If COMSOL is already open, you can start the Model Wizard by selecting New  from the File menu and then click Model Wizard .

The Model Wizard guides you through the first steps of setting up a model. The next window lets you select the dimension of the modeling space.



- 2 In the Space Dimension window click the 3D button .
- 3 In the Select Physics tree under Acoustics>Pressure Acoustics, click Pressure Acoustics, Frequency Domain (acpr) . To add the physics interface, double-click it, click Add, or right-click and select  Add Physics.
- 4 Click Study .
- 5 On the Select Study window under General Studies, click Frequency Domain .
- 6 Click Done .

## Global Definitions


---

**Note:** The location of the text files used in this exercise vary based on the installation. For example, if the installation is on your hard drive, the file path might be similar to C:\Program Files\COMSOL56\applications\.

### Parameters

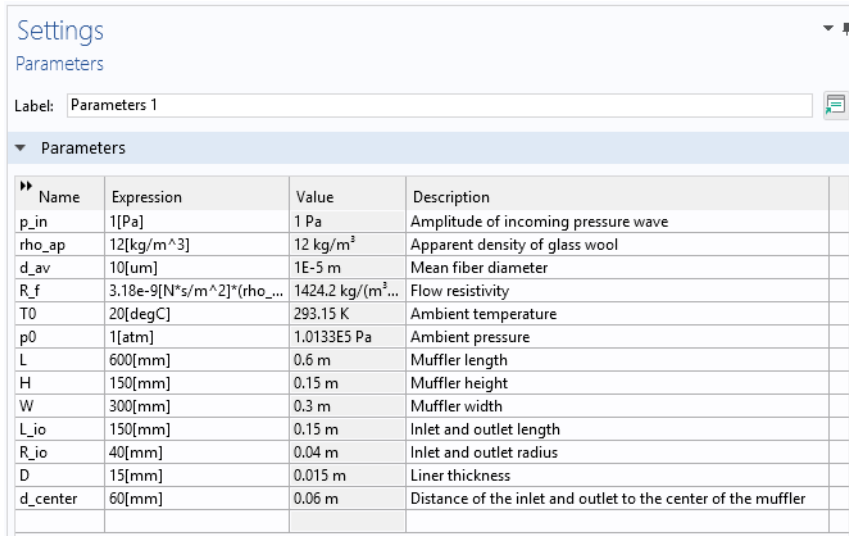
- 1 On the Home toolbar click Parameters  and select Parameter 1 .

**Note:** On Linux and Mac, the Home toolbar refers to the specific set of controls near the top of the Desktop.

- 2 Go to the Settings window for Parameters. Under Parameters click Load from File .

- 3 Browse to the application library folder (Acoustics\_Module\Automotive) and double-click the file `absorptive_muffler_parameters.txt`.

The parameters define the physical values of the system. The figure below shows the full list of parameters after the import of the geometry sequence. In this process the parameters that define the geometry are added to the list.



Name	Expression	Value	Description
p_in	1[Pa]	1 Pa	Amplitude of incoming pressure wave
rho_ap	12[kg/m^3]	12 kg/m <sup>3</sup>	Apparent density of glass wool
d_av	10[um]	1E-5 m	Mean fiber diameter
R_f	3.18e-9[N*s/m^2]*(rho_...	1424.2 kg/(m <sup>3</sup> ...	Flow resistivity
T0	20[degC]	293.15 K	Ambient temperature
p0	1[atm]	1.0133E5 Pa	Ambient pressure
L	600[mm]	0.6 m	Muffler length
H	150[mm]	0.15 m	Muffler height
W	300[mm]	0.3 m	Muffler width
L_io	150[mm]	0.15 m	Inlet and outlet length
R_io	40[mm]	0.04 m	Inlet and outlet radius
D	15[mm]	0.015 m	Liner thickness
d_center	60[mm]	0.06 m	Distance of the inlet and outlet to the center of the muffler

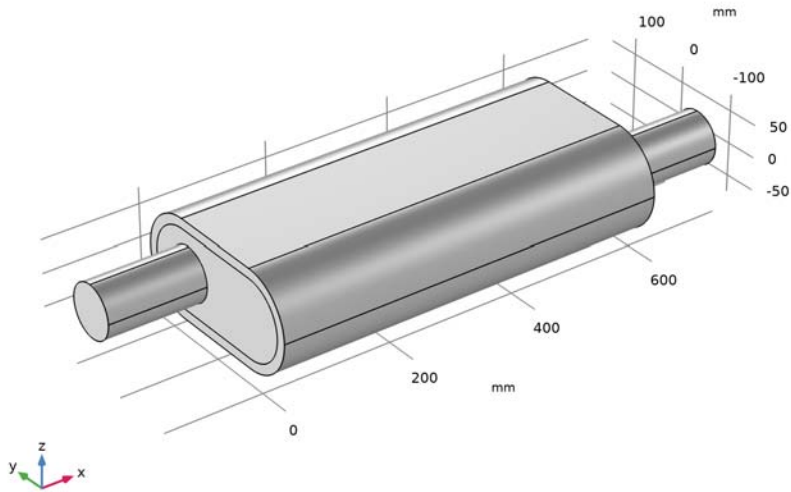
## Geometry I

- 1 In the Model Builder window, under Component 1 (comp1) click Geometry 1.
- 2 In the Settings window for Geometry, locate the Units section.
- 3 From the Length unit list, choose mm.

To save some time, import the geometry sequence from a file. The instructions for setting up the geometry can be found in the Geometry Sequence Instructions section at the bottom of this document.

- 1 In the Geometry toolbar, click Insert Sequence.
- 2 Browse to the model's Application Libraries folder and double-click the file `absorptive_muffler_geom_sequence.mph`.

3 In the Geometry toolbar, click Build All.




Having imported the geometry it can be easily modified as it is parameterized. Simply change the value of a dimension in the parameters list; this will update the geometry automatically. The imported geometry parameters are automatically added to the Parameters 1 node.

## Definitions


---

Create selections for the inlet and outlet of the muffler.

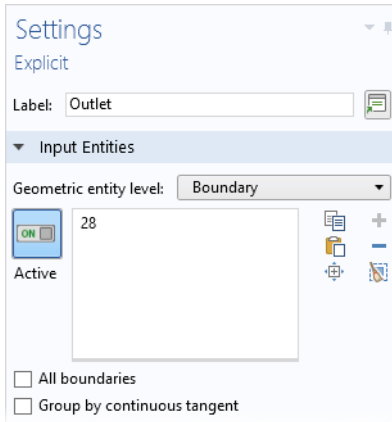
### *Explicit 1*

- 1 On the Definitions toolbar click Explicit .
- 2 Go to the Settings window for Explicit. Enter **Inlet** in the Label field (replace the default).
- 3 Under Input Entities from the Geometric entity level list, choose Boundary.
- 4 Select Boundary 1 only.





### *Explicit 2*

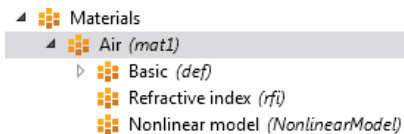
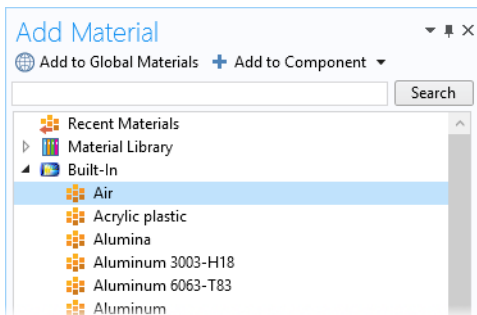
- 1 On the Definitions toolbar click Explicit .

- 2 Go to the Settings window for Explicit. Enter `Outlet` in the Label field (replace the default).
- 3 Under Input Entities from the Geometric entity level list, choose Boundary.
- 4 Select Boundary 28 only.



## Add Material

- 1 On the Home toolbar click Add Material .
- 2 Go to the Add Material window. In the tree under Built-In click Air .
- 3 In the Add material window, click  Add to Component.
- 4 Under Materials click Air  to look at the Material Contents in the Settings window.



The green check marks indicate which material parameters are necessary in the model.

Material Contents					
Property	Variable	Value	Unit	Property group	
<input checked="" type="checkbox"/> Density	rho	rho(pA,T)	kg/m <sup>3</sup>	Basic	
<input checked="" type="checkbox"/> Speed of sound	c	cs(T)	m/s	Basic	
Coefficient of thermal expansion	alpha_iso ; a...	alpha_p(pA,T)	1/K	Basic	
Mean molar mass	Mn	0.02897	kg/mol	Basic	
Bulk viscosity	muB	muB(T)	Pa·s	Basic	
Relative permeability	mur_iso ; m...	1	1	Basic	
Relative permittivity	epsilonIso ; m...	1	1	Basic	
Dynamic viscosity	mu	eta(T)	Pa·s	Basic	
Ratio of specific heats	gamma	1.4	1	Basic	

**Note:** By default the first material added applies to all domains so the geometric scope settings do not need to be changed.

In the second version of this model, a lining material is needed in Domain 2. For now, the muffler is completely hollow. The liner material is added here.

## Materials

### ABSORPTIVE LINER

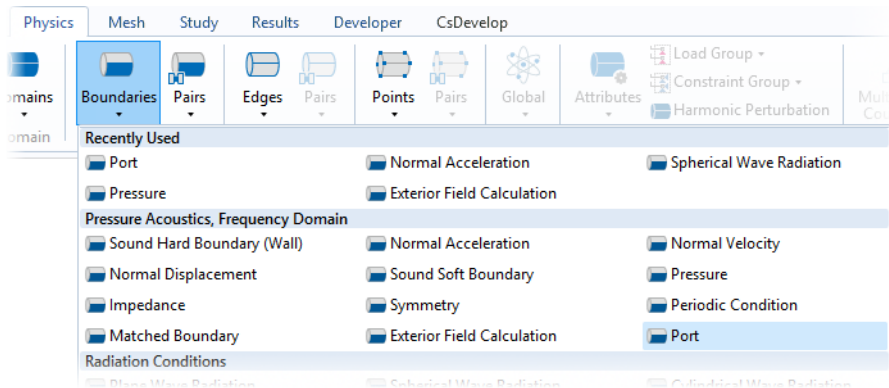
- 1 In the Model Builder window, under Component 1 (comp1) right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type Absorptive Liner in the Label text field.

## Pressure Acoustics, Frequency Domain

### Pressure Acoustics 1

- 1 In the Model Builder window, under Component 1 (comp1)>Pressure Acoustics, Frequency Domain (acpr) click Pressure Acoustics 1.
- 2 In the Settings window for Pressure Acoustics, locate the Model Input section.
- 3 In the  $T$  text field, type T0.
- 4 In the  $pA$  text field, type p0.

Use the Port boundary condition to define the inlet and outlet. The port condition is superior to the classical radiation condition in waveguide configurations. This is particularly the case when nonplane wave modes start to propagate. This happens above the first cutoff frequency. For the present model the cutoff frequency for the first nonplane mode ( $m = 1$  and  $n = 0$ ) is at 2514 Hz which is much higher than the frequencies studied here. The variable `acpr.port2.fc` gives the cutoff frequency of the modes (here for the mode defined on the Port 2 condition). Note that mode (1,0) is a so-called degenerate mode. It needs to be included twice, but with different orientations (rotated 90 deg.) as these are orthogonal. If the frequency analysis is extended above this frequency, then add even more port conditions to capture these modes.



## Port 1

- 1 In the Physics toolbar, click Boundaries and choose Port.
- 2 In the Settings window for Port, locate the Boundary Selection section.

- 3 From the Selection list, choose Inlet.
- 4 Locate the Port Properties section. From the Type of port list, choose Circular.
- 5 Locate the Incident Mode Settings section. In the  $A^{\text{in}}$  text field, type p\_in.

#### *Circular Port Reference Axis 1*

- 1 Right-click Port 1 and choose Circular Port Reference Axis.
- 2 In the Settings window for Circular Port Reference Axis, locate the Point Selection section.
- 3 Click Clear Selection.
- 4 Select Points 1 and 4 only.  
Select two points that define a reference axis for the azimuthal angle. The setting is in general necessary when higher order azimuthal modes are used and/or necessary.

▼ Port Properties

Port name:

Type of port:

▼ Port Mode Settings

Mode number, azimuthal:  
 $m$   1

Mode number, radial:  
 $n$   1

A circular port requires the Circular Port Reference Axis subfeatu

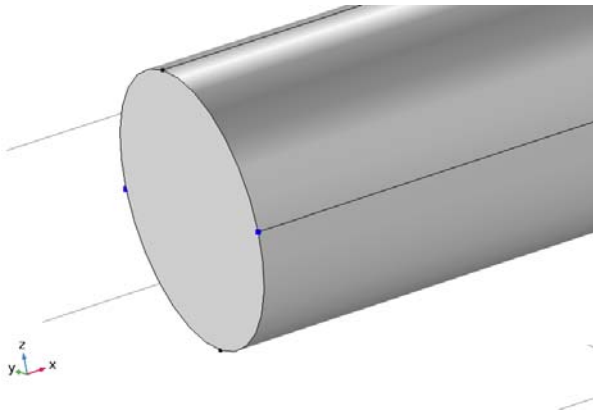
▼ Incident Mode Settings

Incident wave excitation at this port:

Define incident wave:

$A^{\text{in}}$   Pa

Phase:  
 $\phi^{\text{in}}$   rad



#### *Port 2*

- 1 In the Physics toolbar, click Boundaries and choose Port.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- 3 From the Selection list, choose Inlet.
- 4 Locate the Port Properties section. From the Type of port list, choose Circular.

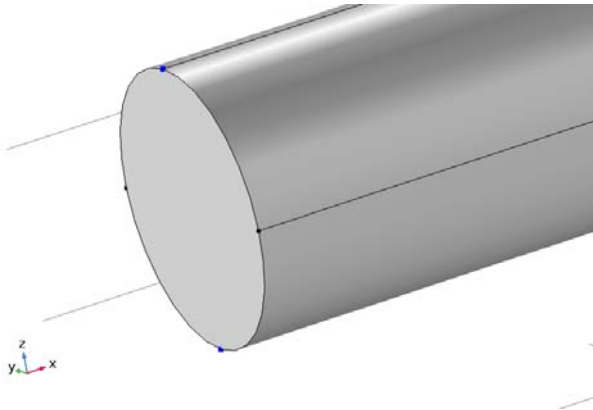
- 5 In the Port Mode Settings enter the Mode number, azimuthal as 1. Keep the Mode number, radial as the default 0.

#### *Circular Port Reference Axis 1*

- 1 Right-click Port 2 and choose Circular Port Reference Axis.
- 2 In the Settings window for Circular Port Reference Axis, locate the Point Selection section.
- 3 Click Clear Selection.  
Select two points at the outlet in the same way.
- 4 Select Points 1 and 4 only.
- 5 Duplicate the Port 2 boundary condition. Right-click and select Duplicate.

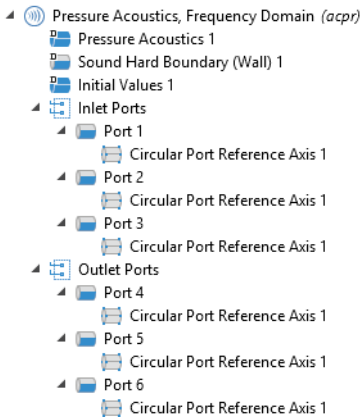
#### *Port 3*

- 1 Select to expand Port 3 and choose Circular Port Reference Axis.
- 2 Modify the Point Selection and select Points 2 and 3 only. This will give an orthogonal mode to the one described by Port 2.



Proceed to add three port conditions also on the Outlet boundary with the same properties as the inlet ports. One mode  $(0,0)$  and two mode  $(1,0)$  with different orientations. None of the ports on the outlet should have the incident wave



excitation turned on. Then group the ports by selecting the three Ports, right click and select Group. This step is only for organizing the user interface.



Now, add a poroacoustics model for the absorptive liner domain. You will deactivate this domain when configuring the first study step.

## Poroacoustics

---

- 1 On the Physics toolbar click Domains  and choose Poroacoustics .
- 2 Go to the Settings window for Poroacoustics. Select Domain 2 only.
- 3 In the Settings window for Poroacoustics, locate the Model Input section.
- 4 In the  $T$  text field, type  $T_0$ .
- 5 Locate the Porous Matrix Properties section. From the Porous elastic material list, choose Absorptive Liner (mat2).

The material data for the flow resistivity will now be picked up from the Absorptive Liner material. Enter the data in the material.

## Materials

---

### *Absorptive Liner (mat2)*

- 1 In the Model Builder window, under Component 1 (comp1)>Materials click Absorptive Liner (mat2).
- 2 In the Settings window for Material, locate the Material Contents section.

3 In the table, enter the following settings:


PROPERTY	VARIABLE	VALUE	UNIT	PROPERTY GROUP
Flow resistivity	Rf	R_f	Pa·s/m <sup>2</sup>	Poroacoustics model

## Mesh 1

### Free Triangular 1

- 1 In the Model Builder window, under Component 1 (comp1) click Mesh 1.
- 2 In the Settings window for Mesh, locate the Mesh Settings section.
- 3 From the Sequence type list, choose User-controlled mesh.

### Size

- 1 Under Mesh 1 click Size .
- 2 In the Settings window for Size, locate the Element Size section.
- 3 Click the Custom button.
- 4 Locate the Element Size Parameters section. In the Maximum element size text field, type  $343[\text{m/s}]/2800[\text{Hz}]/5$ .

The global maximum element size is set equal to the minimal wavelength divided by 5, that is,  $\lambda/5 = c_0/f_{\text{max}}/5$ , where  $c_0$  is the speed of sound.

Element Size

Calibrate for:  
General physics

☐ Predefined Normal
☒ Custom

Element Size Parameters

Maximum element size:  
 mm

Minimum element size:  
 mm

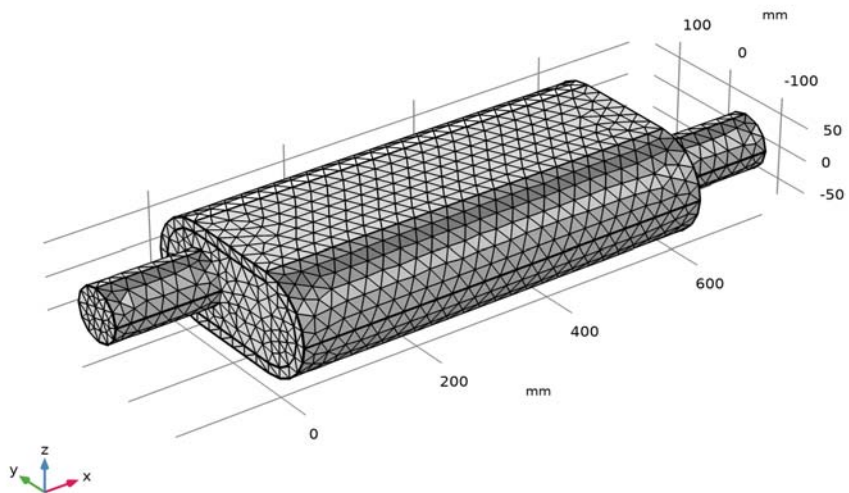
Maximum element growth rate:

Curvature factor:

Resolution of narrow regions:

- 5 Click the Build All button .


The mesh should look like the image below.





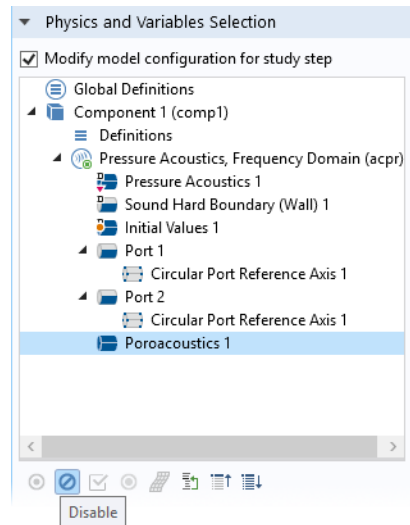
## Study I

---

### Step 1: Frequency Domain

- 1 In the Model Builder expand the Study 1 node then click Step 1: Frequency Domain .
- 2 Go to the Settings window for Frequency Domain. Under Study Settings in the Frequencies text field, enter range (50,25,2800).

- 3 Locate the Physics and Variables Selection section. Select the Modify physics tree and variables for study step check box.
- 4 In the tree, under Component 1>Pressure Acoustics, Frequency Domain, click Poroacoustics 1.
- 5 Click the Disable button  under the table.
- 6 On the Settings window or Home toolbar click Compute .



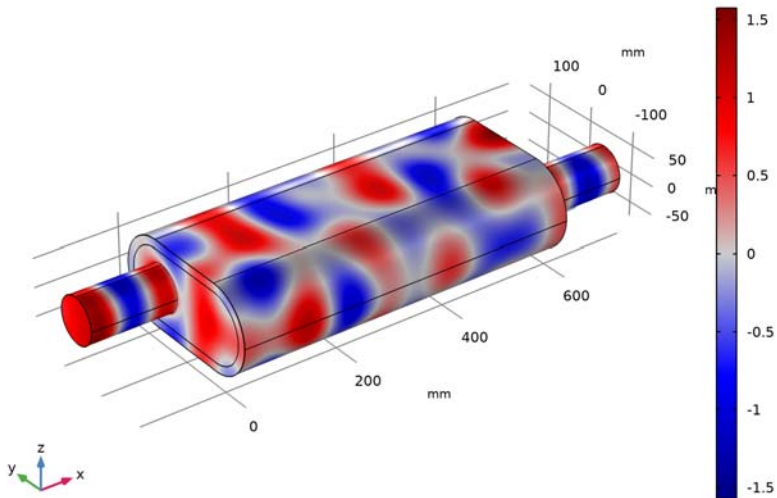
## Results

The first default plot shows the pressure distribution on the walls of the muffler at the highest frequency, 2800 Hz.



## Acoustic Pressure (*acpr*)

freq(111)=2800 Hz

Surface: Total acoustic pressure (Pa)




The pattern is very different at different frequencies. See for example what happens at 1250 Hz.

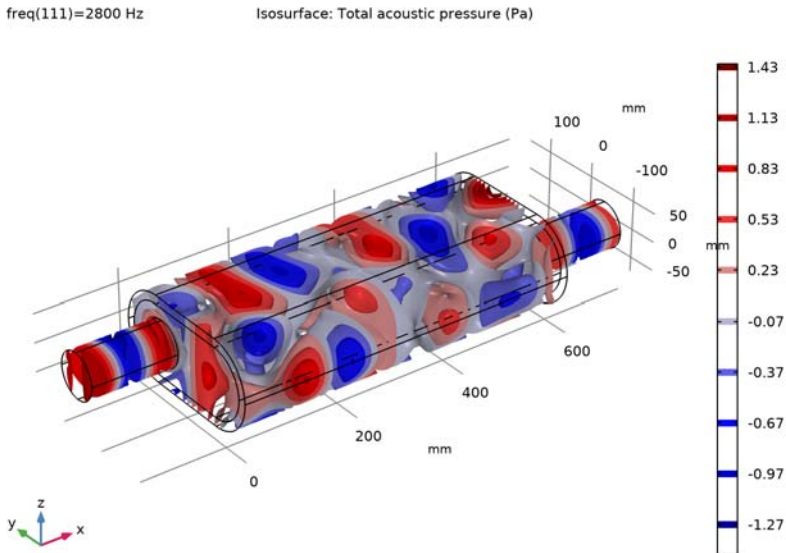
- 1 In the Model Builder under Results, click Acoustic Pressure (*acpr*) .
- 2 Go to the Settings window for 3D Plot Group. Under Data from the Parameter value (freq) list, choose 1250.0.
- 3 On the 3D Plot Group toolbar click the Plot button .

At 1250 Hz, the absolute value of the pressure does not vary much with the x-coordinate. The reason is that this is just higher than the cutoff frequency for the first symmetric propagating mode, which is excited by the incoming wave. For a separate analysis of the propagating modes in the chamber, see the description for the [Eigenmodes in a Muffler](#) model.

The two other default plot groups show the sound pressure level on the wall surface and the pressure inside the muffler as isosurfaces.


### Acoustic Pressure, Isosurfaces (acpr)

- 1 In the Model Builder under Acoustic Pressure, Isosurfaces (acpr), click the Isosurface node  to display the plot in the next figure.




Proceed to plot the transmission loss of the muffler system. Use the Octave Band Plot as it allow to plot any transfer function both as band plots and as continuous curves (sweeps).


### 1D Plot Group 4

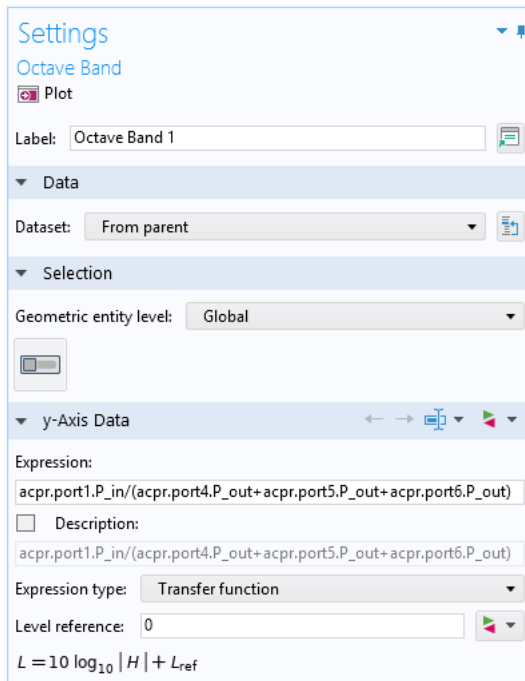
- 1 On the Home toolbar, click Add Plot Group and choose 1D Plot Group .
- 2 In the Settings window for 1D Plot Group, type Transmission Loss, Continuous in the Label text field.

### Transmission Loss, Continuous

- 1 On the Transmission Loss, Continuous toolbar, click Octave Band Plot .
- 2 In the Settings window for Octave Band Plot, locate the Selection section.
- 3 From the Geometric entity level list, choose Global.

Start by locating and inspecting the postprocessing variables available for the port boundary conditions. Add the variable for the power of the incident mode at Port 1. Then modify the expression manually to get the ratio to the power of all the outgoing modes at Port 4, 5, and 6. This will give the transmission loss.

- 4 In the upper-right corner of the y-axis data section, click Replace Expression  . From the menu, choose Component 1> Pressure Acoustics, Frequency Domain>Ports>Port 1> acpr.port1.P\_in - Power of incident mode - W.
- 5 Locate the y-Axis Data section. In the Expression text field, type acpr.port1.P\_in/(acpr.port4.P\_out+acpr.port5.P\_out+acpr.port6.P\_out).



- 6 From the Expression type list, choose Transfer function.
- 7 Locate the Plot section. From the Style list, choose Continuous.
- 8 Locate the Legends section. Select the Show legends check box.
- 9 From the Legends list, choose Manual.
- 10 In the table, enter the following settings:

LEGENDS
No liner




- 11 On the Transmission Loss, Continuous toolbar, click Plot  .

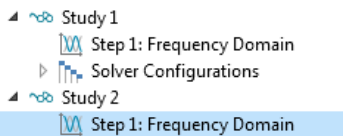
The plot should be a reproduction of the blue curve in [Figure 10](#).

## Model Wizard

---

Proceed to solve the model including a layer of absorptive glass wool on the muffler line. Continue working from where you left off with the model developed thus far and add a second study to keep your existing results intact. The first task is to add a second study to keep the existing results intact.


- 1 On the Home toolbar click Add Study .
- 2 Go to the Add Study window. Under Studies click Frequency Domain . Click Add Study . A Study 2 node is added to the Model Builder.

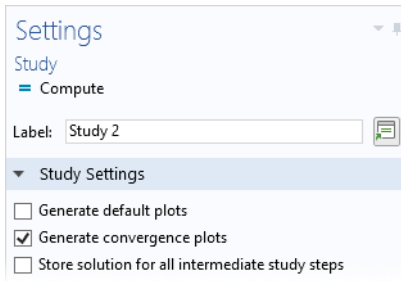


- 3 On the Home toolbar, click Add Study to close the Add Study window.


## Study 2

---

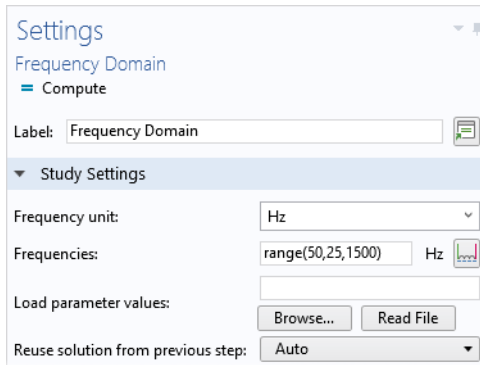
- 1 In the Model Builder click Study 2 .
- 2 In the Settings window for Study under the Study Settings section, click to clear the Generate default plots check box.



### *Step 1: Frequency Domain*

- 1 Under Study 2 click Step 1: Frequency Domain .
- 2 In the Settings window for Frequency Domain locate the Study Settings section.

- 3 In the Frequencies text field enter range(50,25,1500).




- 4 On the Settings window or Home toolbar click Compute .

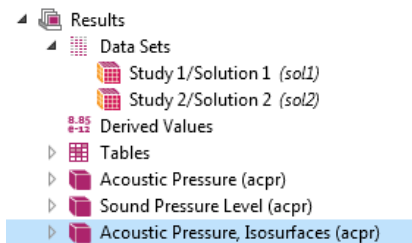
## Results

---

You chose not to have new default plots generated. Once the solution process is finished you can use the existing plot groups and just switch the dataset to see how the damping material affects the solution.

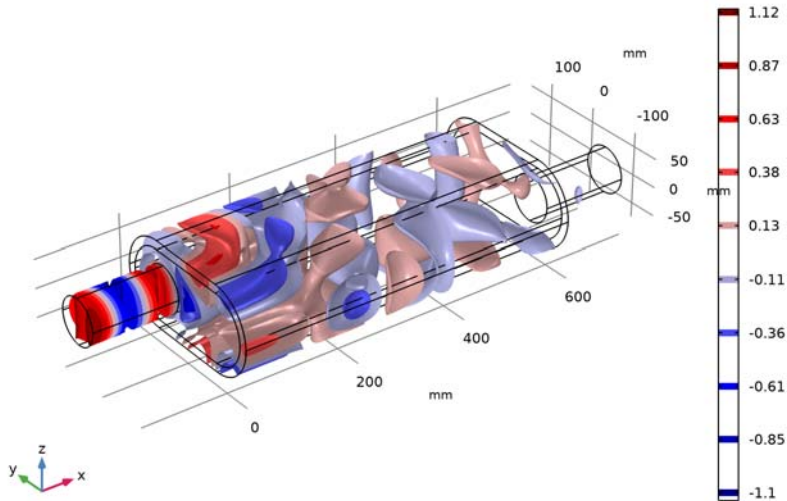
### *Acoustic Pressure, Isosurfaces (acpr)*

- 1 In the Model Builder under Results, click the Acoustic Pressure, Isosurfaces (acpr)  node.

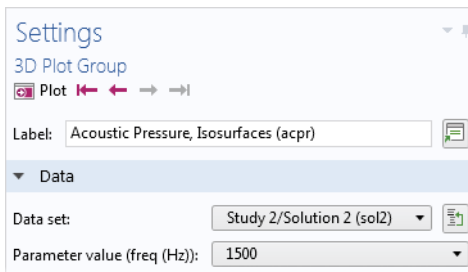



freq(111)=2800 Hz

Isosurface: Total acoustic pressure (Pa)



- 2 In the Settings window for 3D Plot Group under Data, from the Dataset list choose Study2/Solution 2.



- 3 On the Settings window click the Plot button .

At 1500 Hz, the pressure in the chamber is much lower than before.

Proceed to study how the transmission loss has changed with the addition of the lining. Duplicate the first plot and select the new dataset, first do a bit of formatting.

### *Transmission Loss, Continuous*

- 1 In the Model Builder window, under Results click Transmission Loss, Continuous.
- 2 In the Settings window for 1D Plot Group, click to expand the Title section.

- 3 From the Title type list, choose Manual.
- 4 In the Title text area, type Transmission Loss, Continuous.
- 5 Locate the Plot Settings section. Select the y-axis label check box.
- 6 In the associated text field, type Power, incoming wave (dB, rel. outgoing wave).
- 7 Click to expand the Legend section. From the Position list, choose Upper left.
- 8 In the Model Builder window, under Results>Transmission Loss, Continuous right-click Octave Band Plot 1 and choose Duplicate.
- 9 In the Settings window for Octave Band Plot, locate the Data section.
- 10 From the Dataset list, choose Study 2/Solution 2 (sol2).
- 11 Click to expand the Legends section. In the table, enter the following settings:

---

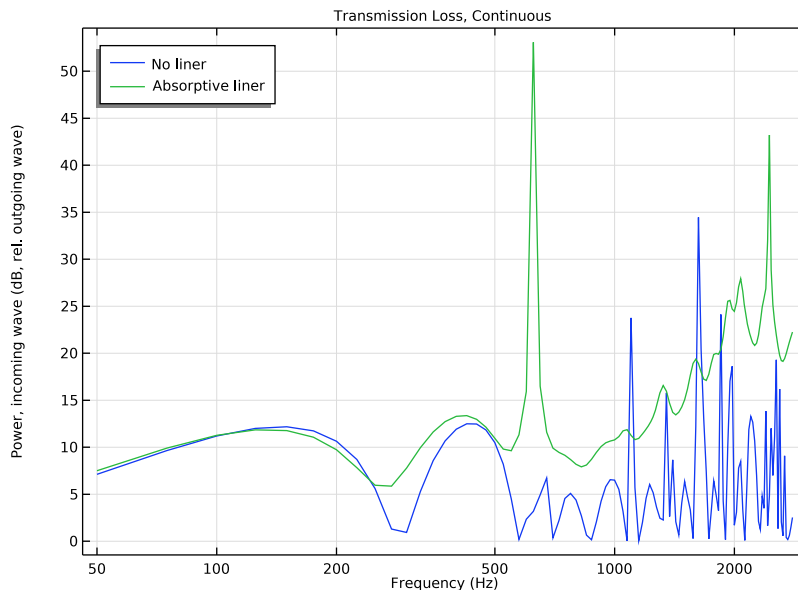
LEGENDS

---

Absorptive liner

---

- 12 On the Transmission Loss, Continuous toolbar, click Plot  .



The plot should look like that in [Figure 10](#) top.

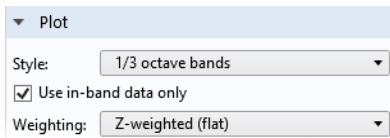
Duplicate the Transmission Loss plot and change the format to 1/3 octave bands.

### *Transmission Loss, Continuous I*


- 1 In the Model Builder window, right-click Transmission Loss, Continuous and choose Duplicate.
- 2 In the Settings window for 1D Plot Group, type Transmission Loss, 1/3 Octave Bands in the Label text field.
- 3 Locate the Title section. In the Title text area, type Transmission Loss, 1/3 Octave Bands.

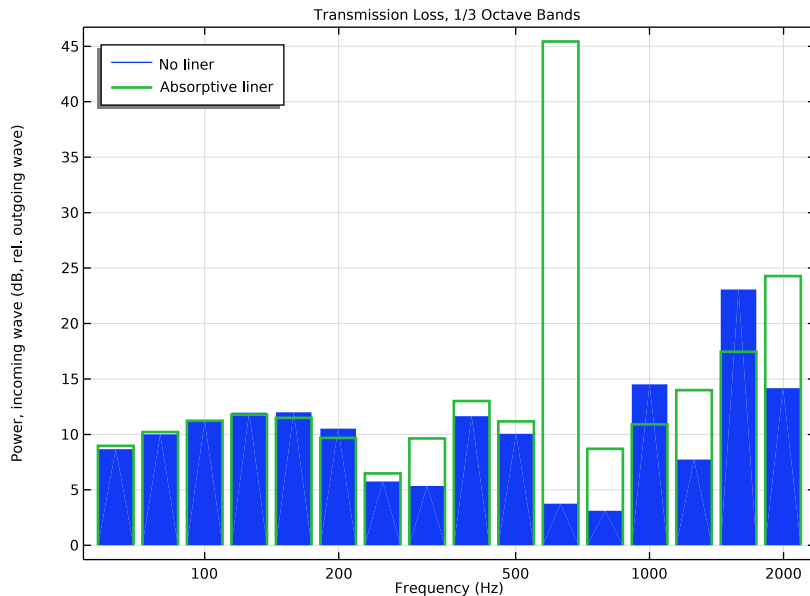
### *Transmission Loss, 1/3 Octave Bands*

- 1 In the Model Builder window, expand the Results>Transmission Loss, 1/3 Octave Bands node, then click Octave Band Plot 1.
- 2 In the Settings window for Octave Band Plot, locate the Plot section.
- 3 From the Style list, choose 1/3 octave bands.



- 4 In the Model Builder window, under Results>Transmission Loss, 1/3 Octave Bands click Octave Band Plot 2.
- 5 In the Settings window for Octave Band Plot, locate the Plot section.
- 6 From the Style list, choose 1/3 octave bands.
- 7 Click to expand the Coloring and style section. Locate the Coloring and Style section. From the Type list, choose Outline.
- 8 In the Width text field, type 2.

9 On the Transmission Loss, 1/3 Octave Bands toolbar, click Plot .






The plot should look like that in [Figure 10](#) bottom.

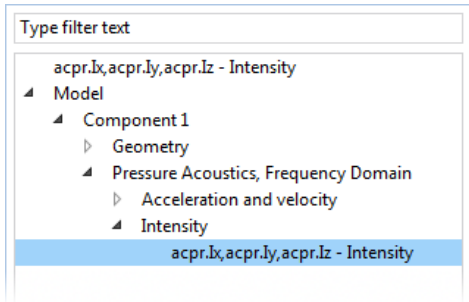
Now, create a plot that represents the intensity flux through the muffler system. Use streamlines that follow the intensity vector (flux of energy through the muffler). You can change between solutions and frequencies to study and visualize the muffler's sound-absorbing properties.

## 3D Plot Group 5

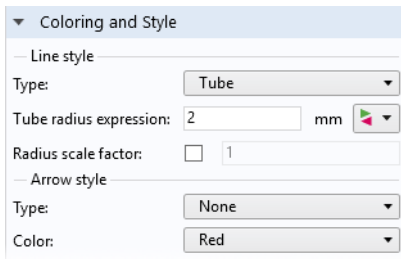
### Intensity



- 1 On the Results toolbar click 3D Plot Group .
- 2 In the Settings window for 3D Plot Group 5, enter Intensity in the Label text field.
- 3 On the Intensity toolbar click Streamline .
- 4 In the Settings window for Streamline click the Replace Expression  button.


- 5 From the menu, search for Intensity (RMS) or `acpr.Ix,acpr.Iy,acpr.Iz`. Double-click to add it to the Expression text field (or enter `acpr.Ix,acpr.Iy,acpr.Iz` in the field).

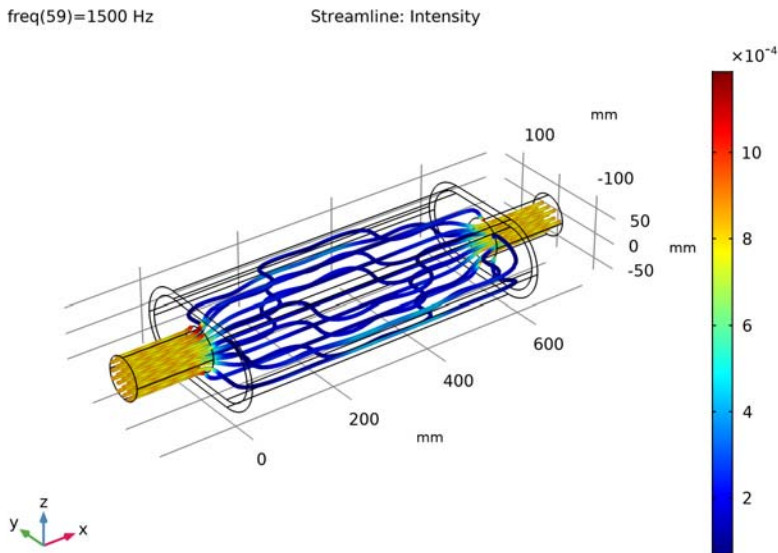


- 6 Under Selection select Boundary 1 only to add it to the selection list.
- 7 Under Coloring and Style:
- From the Line type list choose Tube.
  - In the Tube radius expression text field enter 2.




- 8 In the Model Builder under Intensity, right-click Streamline 1  and choose Color Expression .
- 9 In the Settings window for Color Expression enter `acpr.I_rms` in the Expression text field (replace the default).

10 On the Settings window click Plot .



This should reproduce [Figure 11](#).

As a final step, pick one of the plots to use as a model thumbnail.

1 In the Model Builder under Results, click Acoustic Pressure, Isosurfaces .

2 Click the Root node (the first node in the model tree). On the Settings window for Root under Model Thumbnail, click Set Model Thumbnail.

Make adjustments to the image in the Graphics window using the toolbar buttons until the image is one that is suitable to your purposes.

## Geometry Sequence Instructions


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Below you find the instructions on how to set up the geometry manually if the geometry has not been imported.

### PARAMETERS


1 On the Home toolbar click Parameters  and select Parameter 1 .

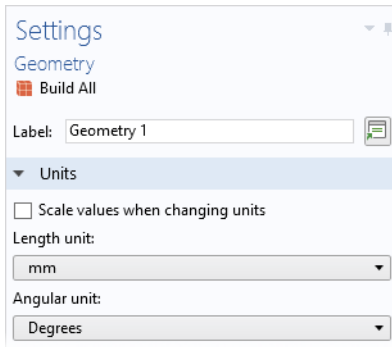
**Note:** On Linux and Mac, the Home toolbar refers to the specific set of controls near the top of the Desktop.

- 2 Go to the Settings window for Parameters. Under Parameters click Load from File .


Browse to the application library folder (Acoustics\_Module\Automotive) and double-click the file `absorptive_muffler_geom_sequence_parameters.txt`.

## GEOMETRY



- 1 In the Model Builder under Component 1, click Geometry 1 .
- 2 Go to the Settings window for Geometry. Under Units from the Length unit list, choose mm.

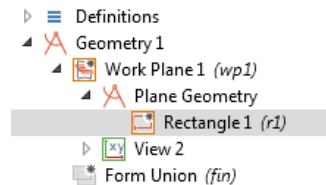


### Work Plane 1

- 1 On the Geometry toolbar click Work Plane .
- 2 Go to the Settings window for Work Plane. Under Plane Definition, from the Plane list choose yz-plane.


### Rectangle 1


- 1 Right-click Plane Geometry  and add a Rectangle .



- 2 Go to the Settings window for Rectangle. Under Size in the:
  - Width text field, enter W.
  - Height text field, enter H.
- 3 Locate the Position section. From the Base list, choose Center.

### Fillet 1

- 1 On the Work plane toolbar click Fillet .
- 2 On the object r1, select Points 1, 2, 3, 4 only.

**Note:** There are many ways to select geometric entities. When you know the points to add, such as in this exercise, you can click the Paste Selection button  and enter the information in the Selection text field. In this example for the Fillet 1 node, enter 1, 2, 3, 4 in the Paste Selection window. For more information about selecting geometric entities in the Graphics window, see the *COMSOL Multiphysics Reference Manual*.

- 3 Go to the Settings window for Fillet. Under Radius in the Radius text field, enter H/2.

Size and Shape

Width: W mm

Height: H mm

Position

Base: Center

xw: 0 mm

yw: 0 mm

Settings

Fillet

Build Selected

Build All

Label: Fillet 1

Points

Vertices to fillet:

ON

r1

1

2

3



4

Active

Radius

Radius: H/2 mm

### Rectangle 2

- 1 Right-click Plane Geometry  and choose Rectangle .
- 2 Go to the Settings window for Rectangle. Under Size in the:
  - Width text field, enter W-2\*D.
  - Height text field, enter H-2\*D.
- 3 Locate the Position section. From the Base list, choose Center.

Size and Shape

Width: W-2\*D mm

Height: H-2\*D mm



Position

Base: Center

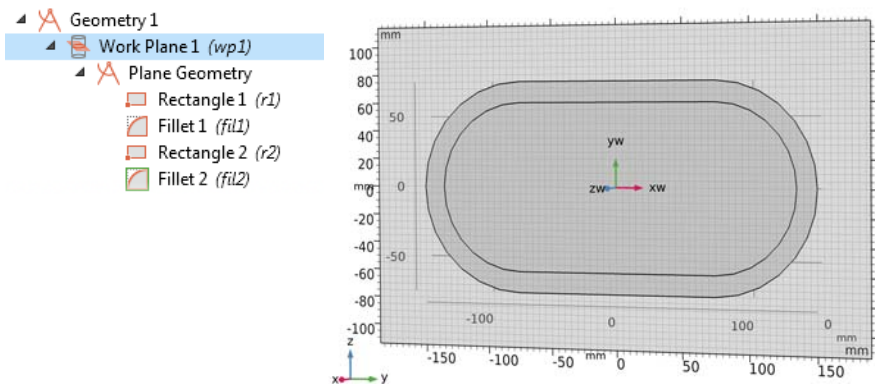
xw: 0 mm

yw: 0 mm



### Fillet 2

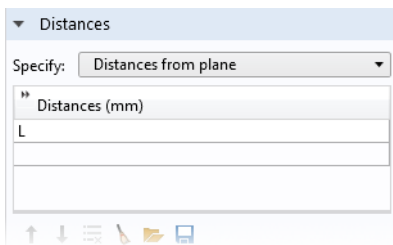
- 1 On the Work plane toolbar, click Fillet .
- 2 On the object r2, select Points 1, 2, 3, 4 only.
- 3 Go to the Settings window for Fillet. Under Radius in the Radius text field, enter  $(H - 2 \cdot D) / 2$ .
- 4 Click the Build All button  on the Settings window or Home toolbar.

The geometry in the Graphics window and the node sequence under Work Plane 1 should match these figures at this point:



### Extrude 1

- 1 On the Work plane toolbar, click Close .
- 2 On the Geometry toolbar click Extrude .
- 3 Go to the Settings window for Extrude. Under Distances from Plane in the table under Distances (mm), enter L in the column (replace the default).



### Cylinder 1

- 1 On the Geometry toolbar click Cylinder .

2 Go to the Settings window for Cylinder. Under Size and Shape in the:

- Radius text field, enter R\_io.
- Height text field, enter L\_io.

3 Under Position in the x text field, enter -L\_io.

4 Under Position in the y text field, enter d\_center.

5 Under Axis:

- From the Axis type list, choose Cartesian.
- In the x text field, enter 1.
- In the z text field, enter 0.

The screenshot shows the 'Cylinder' settings dialog box. It is divided into three main sections: 'Size and Shape', 'Position', and 'Axis'. In the 'Size and Shape' section, 'Radius' is set to 'R\_io' and 'Height' is set to 'L\_io', both with 'mm' units. In the 'Position' section, 'x' is 'L', 'y' is '-d\_center', and 'z' is '0', all with 'mm' units. In the 'Axis' section, 'Axis type' is set to 'Cartesian'. Below this, 'x' is '1', 'y' is '0', and 'z' is '0'.

Size and Shape	
Radius:	R_io mm
Height:	L_io mm

Position	
x:	L mm
y:	-d_center mm
z:	0 mm

Axis	
Axis type:	Cartesian
x:	1
y:	0
z:	0

### Cylinder 2

1 On the Geometry toolbar click Cylinder .

2 Go to the Settings window for Cylinder. Under Size and Shape in the:

- Radius text field, enter R\_io.
- Height text field, enter L\_io.

3 Under Position in the x text field, enter L.

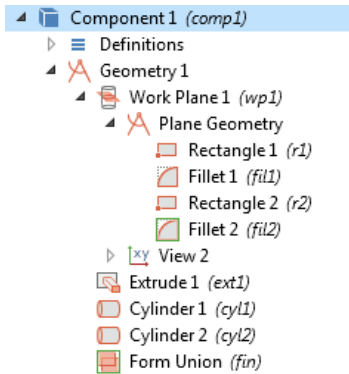
4 Under Position in the y text field, enter -d\_center.

5 Under Axis:

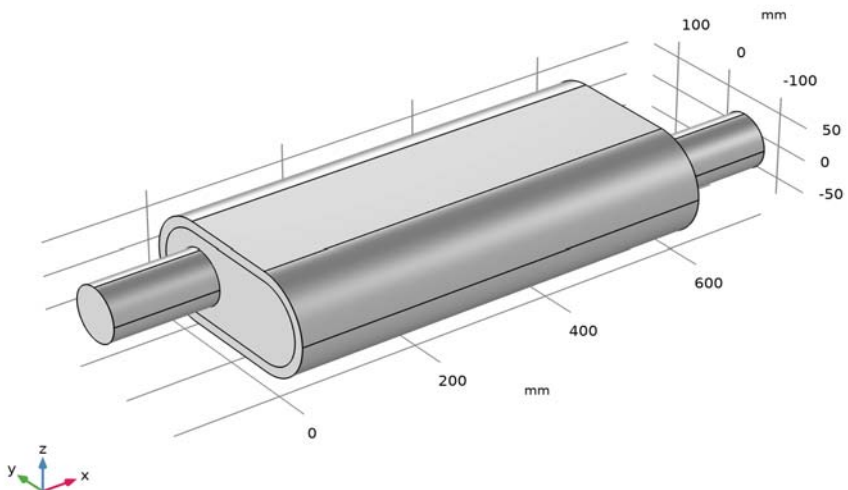
- From the Axis type list, choose Cartesian.
- In the x text field, enter 1.
- In the z text field, enter 0.

6 Click the Build All button  on the Home toolbar. Click the Zoom Extents button  on the Graphics toolbar.

The node sequence in the Model Builder should match the figure.



The finished geometry is shown in the figure below, the axis dimensions are in mm, as selected, and the system of coordinates is also shown.



## Additional Examples from the Application Libraries

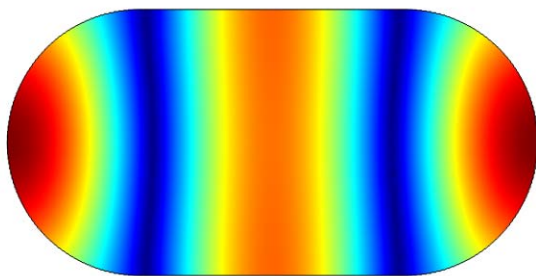
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The Acoustics Module application library has other tutorials available as well as advanced industrial and verification models. Short explanations and examples are given below for a cross-section of these models. Go to [The Application Libraries Window](#) to learn how to access these model files from COMSOL Multiphysics.

### *Eigenmodes in a Muffler*

In this model, the propagating modes in the chamber of an automotive muffler are computed. The geometry is a cross-section of the chamber as described in the Absorptive Muffler example in this guide.

The purpose of the model is to study the shape of the propagating modes and to find the cut-off frequencies. As discussed in the Absorptive Muffler tutorial, some of the modes significantly affect the damping of the muffler at frequencies above the cut-off. In the Eigenmodes in Muffler model, modes with cut-off frequencies up to 1500 Hz are studied.



*Figure 12: First fully symmetric propagation mode of the muffler chamber (with no absorbing liner). The plot shows the absolute value of the pressure.*

### *Piezoacoustic Transducer*

A piezoelectric transducer can be used either to transform an electric current to an acoustic pressure field or, the opposite, to produce an electric current from an acoustic field. These devices are generally useful for applications that require the generation of sound in air and liquids. Examples of such applications include phased array microphones, ultrasound equipment, inkjet droplet actuators, sonar transducers, and devices for drug discovery, bioimaging, and acousto-biotherapeutics.

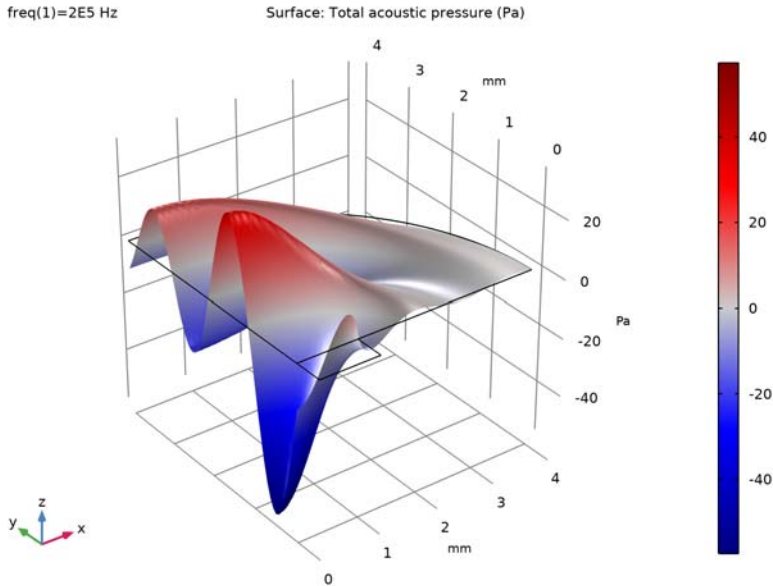


Figure 13: Surface and height plot of the pressure distribution created by the piezoactuator at  $f = 100 \text{ kHz}$ .

### ***Loudspeaker Driver in a Vented Enclosure***

An important class of acoustic models are transducers — that is, electromechanical acoustic transducers. Transducers are true multiphysics models that often in addition to acoustics necessitate a structural mechanics and an electromagnetic interface is added. One such class are loudspeakers (presented here), another are microphones presented below.

This model of a boxed loudspeaker lets you apply a nominal driving voltage and extract the resulting sound pressure level in the outside room as a function of the frequency. The electromagnetic properties of the driver are supplied from the Loudspeaker Driver model (available with the AC/DC Module). The model uses

the Acoustic-Shell Interaction interface and therefore requires the Structural Mechanics Module.

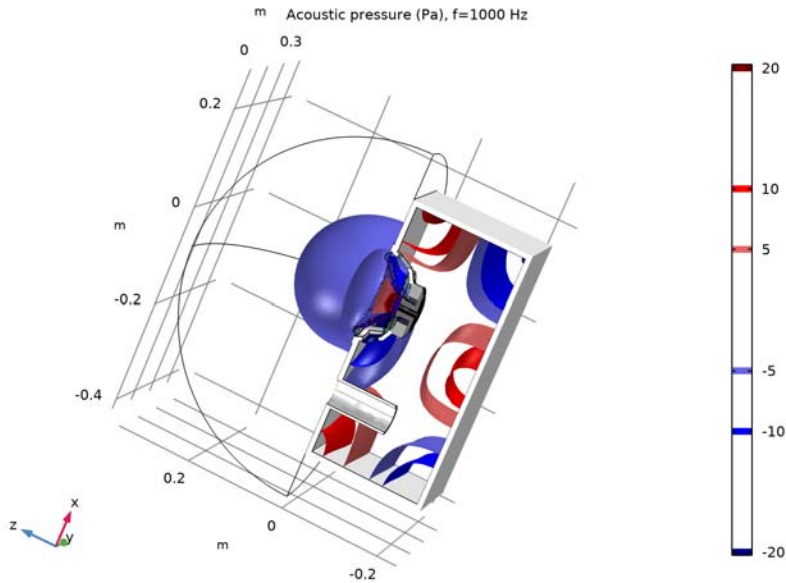


Figure 14: Iso-pressure contours (in gray scale) and deformation of the speaker cone (colors).

### ***The Brüel & Kjær 4134 Condenser Microphone***

Another type of transducer is the microphone. This is a model of the Brüel and Kjær 4134 condenser microphone. The geometry and material parameters are those of the microphone. The modeled sensitivity level is compared to measurements performed on an actual microphone and shows good agreement. The membrane deformation, pressure, velocity, and electric field are also

determined. The model requires the Acoustics Module, the AC/DC Module, and the Structural Mechanics Module.

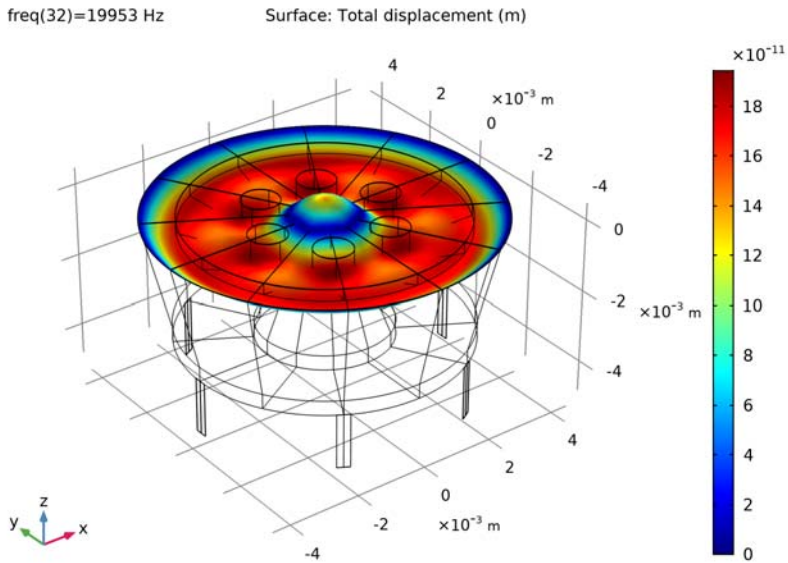


Figure 15: Deformation of the microphone membrane (diaphragm) at 20 kHz. The geometry is courtesy of Brüel & Kjær.

This concludes this introduction.

