

Duct with Right-Angled Bend

In this tutorial, the acoustic behavior of a duct or waveguide with a right-angled bend is analyzed. The model uses port boundary conditions at the inlet and outlet. The ports can capture and treat non-plane propagating modes in waveguides, extending the analysis above the first cutoff frequency. The transmission loss and the scattering coefficients of the system are determined.

Model Definition

The geometry of the waveguide system analyzed in this model is depicted in Figure 1. It consists of a duct with a right-angled bend in the middle. On the outlet branch there is also a small dent. The dent is present in order to excite modes that have components in the duct height (the z direction). The width of the duct is W and the height is H; these are parameters that can be changed. A 2D variant of this tutorial model that studied scattering in a 2D bend is described in Ref. 1.

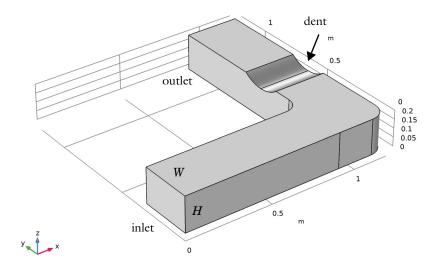


Figure 1: Waveguide geometry consisting of a two sections connected by a right-angled bend. A small dent is present on the outlet section.

The model is solved for frequencies in the range from 50 to 1300 Hz. In that range five modes exist: the plane (0,0), the first long edge (1,0), the first short edge (0,1), the first mixed mode (1,1), and the second long edge (2,0). Their cutoff frequencies are given in Table 1 below (these are derived in the postprocessing steps of the model using built-in variables). The mode shapes are depicted in the results section in Figure 5.

TABLE I: MODE CUTOFF FREQUENCIES.

MODE (M,N)	CUTOFF FREQUENCY	
(0,0)	0.0 Hz	
(1,0)	572.0 Hz	
(0,1)	858.0 Hz	
(1,1)	1031.2 Hz	
(2,0)	1144.0 Hz	

In order to capture these modes and ensure good non-reflecting behavior at the waveguide inlet and outlet, four Port boundary conditions are added at each end. Each port capturing a specific mode. When solving the model, a part of the solution are the scattering coefficients S_{i1} , where the subscript 1 refers to the fact that the system is excited at Port 1 (plane wave incidence at the inlet). This means that on the inlet or outlet boundaries, the combination of ports defines the total acoustic field (sum of incident and outgoing waves) as

$$p_{t} = \sum_{i \in bnd} (S_{i1} + A^{in} \delta_{i1}) p_{i}$$

where the summation "i" is over all ports on the given boundary "bnd" (for example 1, 2, 3, 4, and 5 on the inlet), Aⁱⁿ is the amplitude of the incident field (1 Pa in this model), and p_i is the mode shape of the i-th port. The mode shape p_i is normalized to have a unit maximum amplitude.

A benefit of using the Port boundary condition is that important postprocessing variables are readily defined on each port. This includes fields like the total pressure, intensity, and normal velocity, and also global (integrated) variables like the incoming or outgoing power or average pressure. These quantities can in general be difficult to compute when complex non-plane propagation occurs. In this model, the transmission loss TL of the system is calculated as

$$TL = 10\log_{10} \left(\frac{P_{in}}{\sum P_{out}} \right)$$

where the sum is over all the ports at the outlet. The incident power is simply given by the variable acpr.port1.P_in and the sum of the outgoing power as acpr.port5.P_out+ acpr.port6.P out+acpr.port7.P out+acpr.port8.P out.

Results and Discussion

The absolute value of the scattering coefficients $\left|S_{i1}\right|$ is depicted in Figure 2 below. The graph shows the cutoff of the different modes which is in accordance with the values given in Table 1. The transmission loss of the system is depicted in Figure 3. Isosurface plots of the pressure inside the duct is depicted in Figure 4 at four different frequencies, each representing values when one more mode is propagating in the system. The first image at the top left represents plane wave propagation and so forth. The five normalized mode shapes are depicted in Figure 5. Finally, the normalized outgoing power through the ports is presented in Figure 6.

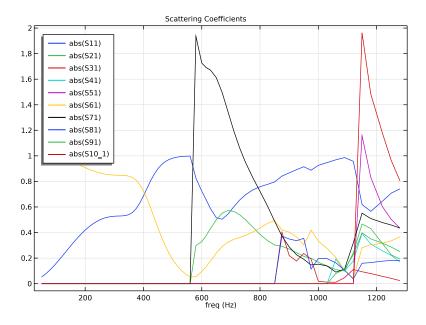


Figure 2: Absolute value of the scattering coefficients as function of frequency.

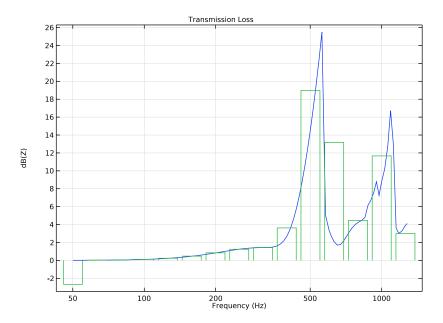


Figure 3: Transmission loss TL through the waveguide system.

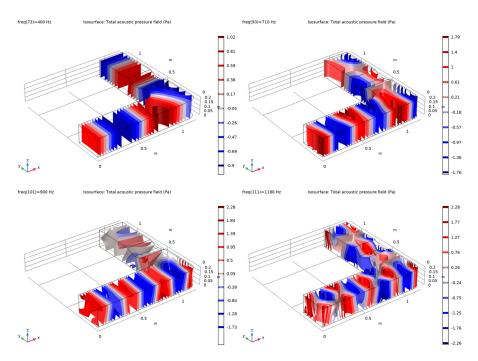


Figure 4: Pressure isosurfaces evaluated at four different frequencies.

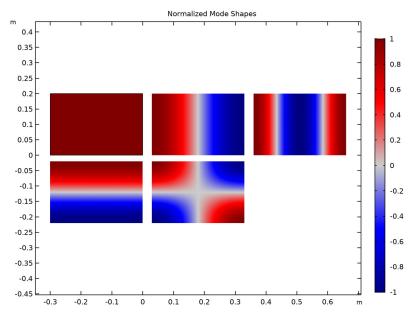


Figure 5: Normalized mode shapes for the five ports.

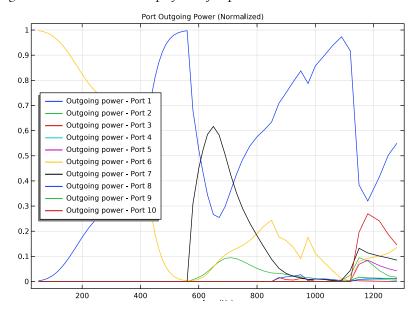


Figure 6: Normalized outgoing power for the five inlet and five outlet ports.

Reference

1. T. Graf and J. Pan, "Determination of the complex acoustic scattering matrix of a rightangled duct," J. Acoust. Soc. Am., vol 134, pp. 292-299, 2013.

Application Library path: Acoustics Module/Tutorials, Pressure Acoustics/ duct right angled bend

Modeling Instructions

This section contains the modeling instructions for the Absorptive Muffler model. They are followed by the Geometry Sequence Instructions section.

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click 3D.
- 2 In the Select Physics tree, select Acoustics>Pressure Acoustics, Frequency Domain (acpr).
- 3 Click Add.
- 4 Click Study.
- 5 In the Select Study tree, select General Studies>Frequency Domain.
- 6 Click Done.

GEOMETRY I

To save some time, import the geometry sequence from a file. The instructions for setting up the geometry can be found in the Geometry Sequence Instructions section at the bottom of this document.

- I In the Geometry toolbar, click Insert Sequence.
- **2** Browse to the model's Application Libraries folder and double-click the file duct_right_angled_bend_geom_sequence.mph.
- 3 In the Geometry toolbar, click Build All.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

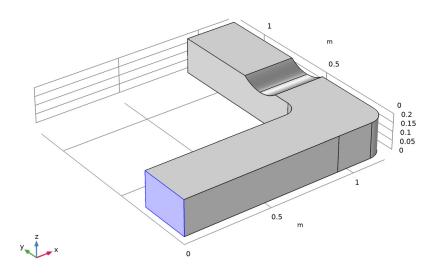
Name	Expression	Value	Description
f_max	1300[Hz]	1300 Hz	Maximum study frequency
lambda_min	343[m/s]/f_max	0.26385 m	Minimum wavelength

DEFINITIONS

Create selections for the inlet and outlet of the duct.

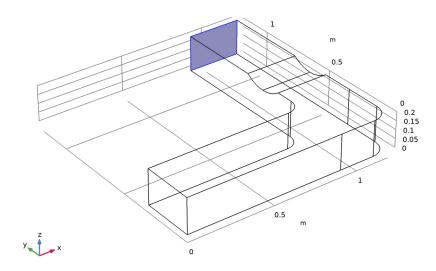
Explicit I

- I In the **Definitions** toolbar, click **Explicit**.
- 2 In the Settings window for Explicit, type Inlet in the Label text field.
- 3 Locate the Input Entities section. From the Geometric entity level list, choose Boundary.
- 4 Select Boundary 1 only.



Explicit 2

- I In the **Definitions** toolbar, click **Explicit**.
- 2 In the Settings window for Explicit, type Outlet in the Label text field.
- 3 Locate the Input Entities section. From the Geometric entity level list, choose Boundary.
- 4 Click the Wireframe Rendering button in the Graphics toolbar. This simplifies seeing and selecting the outlet boundary.
- **5** Select Boundary 12 only.



6 Click the Wireframe Rendering button in the Graphics toolbar.

ADD MATERIAL

- I In the Home toolbar, click Add Material to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Built-in>Air.
- 4 Click Add to Component in the window toolbar.
- 5 In the Home toolbar, click Add Material to close the Add Material window.

Proceed to setting up the physics by adding the Port boundary conditions to the inlet and the outlet. Use the Node Group feature to group the conditions at the inlet and outlet, respectively. This gives a better overview of the model setup.

Add five port conditions at each end of the duct (the waveguide structure). These will capture all propagating modes up to the studied frequency of 1200 Hz. In the postprocessing part of this model you will set up and see a list of the cutoff frequencies of the captured modes. It is always possible to use the Pressure Acoustics, Boundary Mode physics interface to study and analyze propagating and non-propagating modes in a waveguide cross section. See, for example, the eigenmodes_in_muffler model in the Automotive application library.

PRESSURE ACOUSTICS, FREQUENCY DOMAIN (ACPR)

Group 1

- I In the Model Builder window, under Component I (compl) right-click Pressure Acoustics, Frequency Domain (acpr) and choose Node Group.
- 2 In the Settings window for Group, type Inlet Ports in the Label text field.

Port 1

- I Right-click Inlet Ports and choose Port.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- 3 From the Selection list, choose Inlet.
- **4** Locate the **Port Properties** section. From the **Type of port** list, choose **Rectangular**.

Use the rectangular (analytical) option that applies to this geometry of a rectangular waveguide with sound hard boundaries. Note that the first port condition that you add has the incident mode option turned on per default, whereas the following are off per default.

5 Locate the **Incident Mode Settings** section. In the A^{in} text field, type 1.

Port 2

- I In the Physics toolbar, click Boundaries and choose Port.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- **3** From the **Selection** list, choose **Inlet**.
- 4 Locate the Port Properties section. From the Type of port list, choose Rectangular.
- **5** Locate the **Port Mode Settings** section. In the *m* text field, type 1.

Port 3

- I In the Physics toolbar, click Boundaries and choose Port.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- 3 From the Selection list, choose Inlet.

- 4 Locate the Port Properties section. From the Type of port list, choose Rectangular.
- **5** Locate the **Port Mode Settings** section. In the n text field, type 1.

Port 4

- I In the Physics toolbar, click Boundaries and choose Port.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- **3** From the **Selection** list, choose **Inlet**.
- 4 Locate the Port Properties section. From the Type of port list, choose Rectangular.
- **5** Locate the **Port Mode Settings** section. In the m text field, type 1.
- **6** In the *n* text field, type 1.

Port 5

- I In the Physics toolbar, click Boundaries and choose Port.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- **3** From the **Selection** list, choose **Inlet**.
- 4 Locate the Port Properties section. From the Type of port list, choose Rectangular.
- **5** Locate the **Port Mode Settings** section. In the *m* text field, type 2.
- **6** In the *n* text field, type 0.

Group 2

- I In the Model Builder window, right-click Pressure Acoustics, Frequency Domain (acpr) and choose **Node Group**.
- 2 In the Settings window for Group, type Outlet Ports in the Label text field.

Port 6

- I In the Physics toolbar, click Boundaries and choose Port.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- **3** From the **Selection** list, choose **Outlet**.
- 4 Locate the Port Properties section. From the Type of port list, choose Rectangular.

Port 7

- I In the Physics toolbar, click Boundaries and choose Port.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- **3** From the **Selection** list, choose **Outlet**.
- 4 Locate the Port Properties section. From the Type of port list, choose Rectangular.
- **5** Locate the **Port Mode Settings** section. In the m text field, type 1.

Port 8

- I In the Physics toolbar, click Boundaries and choose Port.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- 3 From the Selection list, choose Outlet.
- 4 Locate the Port Properties section. From the Type of port list, choose Rectangular.
- **5** Locate the **Port Mode Settings** section. In the n text field, type 1.

Port 9

- I In the Physics toolbar, click Boundaries and choose Port.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- **3** From the **Selection** list, choose **Outlet**.
- 4 Locate the Port Properties section. From the Type of port list, choose Rectangular.
- **5** Locate the **Port Mode Settings** section. In the m text field, type 1.
- **6** In the *n* text field, type 1.

Port 10

- I In the Physics toolbar, click Boundaries and choose Port.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- 3 From the Selection list, choose Outlet.
- 4 Locate the Port Properties section. From the Type of port list, choose Rectangular.
- **5** Locate the **Port Mode Settings** section. In the *m* text field, type 2.
- **6** In the n text field, type 0.

MESH I

Free Tetrahedral I

In the Model Builder window, under Component I (compl) right-click Mesh I and choose Free Tetrahedral.

Size

- I In the Settings window for Size, locate the Element Size section.
- 2 Click the **Custom** button.
- **3** Locate the **Element Size Parameters** section. In the **Maximum element size** text field, type lambda min/6.
- 4 Click Build All.

STUDY I

Step 1: Frequency Domain

- I In the Model Builder window, under Study I click Step I: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- 3 Click Range.
- 4 In the Range dialog box, choose ISO preferred frequencies from the Entry method list.
- 5 In the Start frequency text field, type 50.
- **6** In the **Stop frequency** text field, type f max.
- 7 From the Interval list, choose 1/24 octave.
- 8 Click Replace.
- **9** In the **Home** toolbar, click **Compute**.

Note that a solver warning is given: New constraint force nodes detected: These are not stored. This warning can be disregarded. It is due to the changing number of constraints when more ports become active as the frequency increases.

RESULTS

Take a look at the first three default plots that are generated automatically. They represent the acoustic pressure, the sound pressure level, and isocontours of the pressure, respectively. Change the Parameter value (freq (Hz)) in the plots to change the evaluation frequency, for example, to 400 Hz.

The isosurface plots of the pressure at four different frequencies is also depicted in Figure 4.

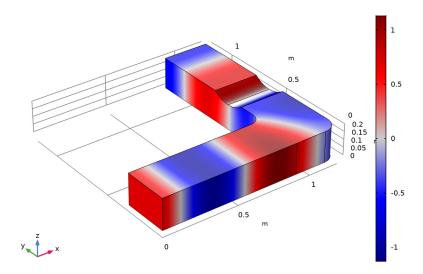
Acoustic Pressure (acpr)

- I In the Model Builder window, under Results click Acoustic Pressure (acpr).
- 2 In the Settings window for 3D Plot Group, locate the Data section.

3 From the Parameter value (freq (Hz)) list, choose 400.

freq(73)=400 Hz

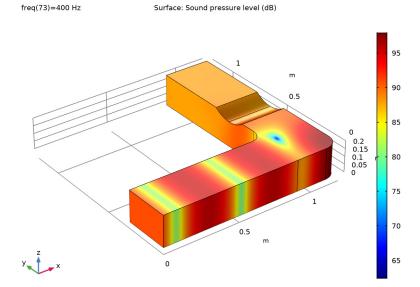
Surface: Total acoustic pressure field (Pa)



Sound Pressure Level (acpr)

- I In the Model Builder window, click Sound Pressure Level (acpr).
- 2 In the Settings window for 3D Plot Group, locate the Data section.

3 From the Parameter value (freq (Hz)) list, choose 400.



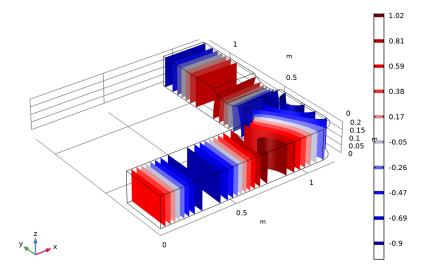
Acoustic Pressure, Isosurfaces (acpr)

- I In the Model Builder window, click Acoustic Pressure, Isosurfaces (acpr).
- 2 In the Settings window for 3D Plot Group, locate the Data section.

3 From the Parameter value (freq (Hz)) list, choose 400.

freq(73)=400 Hz

Isosurface: Total acoustic pressure field (Pa)



ID Plot Group 4

Now proceed and plot the scattering coefficent to reproduce Figure 2.

- I In the Home toolbar, click Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Scattering Coefficents in the Label text field.
- 3 Click to expand the Title section. From the Title type list, choose Manual.
- 4 In the Title text area, type Scattering Coefficients.
- 5 Locate the Legend section. From the Position list, choose Upper left.

Global I

- I Right-click Scattering Coefficents and choose Global.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
abs(acpr.S11)	1	abs(S11)
abs(acpr.S21)	1	abs(S21)
abs(acpr.S31)	1	abs(S31)

Expression	Unit	Description	
abs(acpr.S41)	1	abs(S41)	
abs(acpr.S51)	1	abs(S51)	
abs(acpr.S61)	1	abs(S61)	
abs(acpr.S71)	1	abs(S71)	
abs(acpr.S81)	1	abs(S81)	
abs(acpr.S91)	1	abs(S91)	
abs(acpr.S10_1)	1	abs(S10_1)	

4 In the Scattering Coefficients toolbar, click Plot.

ID Plot Group 5

Now plot the transmission loss to reproduce Figure 3.

- I In the Home toolbar, click Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Transmission Loss in the Label text field.
- 3 Locate the Title section. From the Title type list, choose Manual.
- 4 In the **Title** text area, type Transmission Loss.

Octave Band I

- I In the Transmission Loss toolbar, click More Plots and choose Octave Band.
- 2 In the Settings window for Octave Band, locate the Selection section.
- 3 From the Geometric entity level list, choose Global.
- 4 Locate the y-Axis Data section. In the Expression text field, type acpr.port1.P in/ (acpr.port6.P_out+acpr.port7.P_out+acpr.port8.P_out+ acpr.port9.P out+acpr.port10.P out).

This expression gives the ratio of the incoming power (the source at Port 1) and the total outgoing power at the outlet (the sum of the outgoing power of all modes). Note that in general this is not a straightforward quantity to compute for the non-plane modes. Thus, using the built-in variables for the power (acpr.port4.P out etc.) greatly simplifies postprocessing.

- 5 From the Expression type list, choose Transfer function.
- 6 Locate the Plot section. From the Style list, choose Continuous.
- 7 In the Transmission Loss toolbar, click Plot.

Octave Band 2

I Right-click Octave Band I and choose Duplicate.

- 2 In the Settings window for Octave Band, locate the Plot section.
- 3 From the Style list, choose 1/3 octave bands.
- 4 Click to expand the Coloring and Style section. From the Type list, choose Curve.
- 5 In the Transmission Loss toolbar, click Plot.

Datasets

Now, plot the normalized propagation modes to reproduce Figure 5.

Surface 1

- I In the Results toolbar, click More Datasets and choose Surface.
- 2 Select Boundary 1 only.

2D Plot Group 6

- I In the Results toolbar, click 2D Plot Group.
- 2 In the Settings window for 2D Plot Group, type Normalized Mode Shapes in the Label text field.
- 3 Click to expand the **Title** section. From the **Title type** list, choose **Manual**.
- 4 In the Title text area, type Normalized Mode Shapes.
- 5 Clear the Parameter indicator text field.

Surface 1

- I Right-click Normalized Mode Shapes and choose Surface.
- 2 In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I>Pressure Acoustics, Frequency Domain>Ports>Port I>acpr.portI.pn - Normalized mode pressure - Pa.
- 3 In the Normalized Mode Shapes toolbar, click Plot.
- 4 Locate the Coloring and Style section. From the Color table list, choose Wave.
- 5 Select the Symmetrize color range check box.

Surface 2

- I Right-click Surface I and choose Duplicate.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type acpr.port2.pn.
- 4 Click to expand the Inherit Style section. From the Plot list, choose Surface 1.

Deformation I

I Right-click Surface 2 and choose Deformation.

- 2 In the Settings window for Deformation, locate the Expression section.
- 3 In the x component text field, type 1.1*W.
- **4** In the **y component** text field, type **0**.
- **5** Locate the **Scale** section. Select the **Scale factor** check box.
- 6 In the associated text field, type 1.
- 7 In the Normalized Mode Shapes toolbar, click Plot.
- 8 Click the **Zoom Extents** button in the **Graphics** toolbar.

Surface 3

- I In the Model Builder window, under Results>Normalized Mode Shapes right-click Surface 2 and choose Duplicate.
- 2 In the Settings window for Surface, locate the Expression section.
- **3** In the **Expression** text field, type acpr.port3.pn.

Deformation I

- I In the Model Builder window, expand the Surface 3 node, then click Deformation 1.
- 2 In the Settings window for Deformation, locate the Expression section.
- 3 In the x component text field, type 0.
- **4** In the **y** component text field, type -1.1*H.
- 5 In the Normalized Mode Shapes toolbar, click Plot.
- 6 Click the **Zoom Extents** button in the **Graphics** toolbar.

Surface 4

- I In the Model Builder window, under Results>Normalized Mode Shapes right-click Surface 3 and choose Duplicate.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type acpr.port4.pn.

Deformation I

- I In the Model Builder window, expand the Surface 4 node, then click Deformation I.
- 2 In the Settings window for Deformation, locate the Expression section.
- 3 In the x component text field, type 1.1*W.
- 4 In the Normalized Mode Shapes toolbar, click Plot.
- 5 Click the **Zoom Extents** button in the **Graphics** toolbar.

Surface 5

- I In the Model Builder window, under Results>Normalized Mode Shapes right-click **Surface 4** and choose **Duplicate**.
- 2 In the Settings window for Surface, locate the Expression section.
- **3** In the **Expression** text field, type acpr.port5.pn.

Deformation I

- I In the Model Builder window, expand the Surface 5 node, then click Deformation I.
- 2 In the Settings window for Deformation, locate the Expression section.
- 3 In the x component text field, type 2.2*W.
- **4** In the **y component** text field, type **0**.
- 5 In the Normalized Mode Shapes toolbar, click Plot.
- **6** Click the **Zoom Extents** button in the **Graphics** toolbar.

Evaluation Group 1

- I In the Results toolbar, click Evaluation Group.
- 2 In the Settings window for Evaluation Group, type Cutoff Frequencies in the Label text field.
- 3 Locate the Data section. From the Parameter selection (freq) list, choose First.

Global Evaluation 1

- I Right-click Cutoff Frequencies and choose Global Evaluation.
- 2 In the Settings window for Global Evaluation, click Replace Expression in the upper-right corner of the Expressions section. From the menu, choose Component 1>

Pressure Acoustics, Frequency Domain>Ports>Port I>acpr.port1.fc -Mode cutoff frequency - Hz.

Modify the first description to reflect which mode it refers to and then add the other cutoff frequency variables. These values are also discussed in the results section of the model description.

3 Locate the **Expressions** section. In the table, enter the following settings:

Expression	Unit	Description
acpr.port1.fc	Hz	Mode (0,0) cutoff frequency
acpr.port2.fc	Hz	Mode (1,0) cutoff frequency
acpr.port3.fc	Hz	Mode (0,1) cutoff frequency
acpr.port4.fc	Hz	Mode (1,1) cutoff frequency
acpr.port5.fc	Hz	Mode (2,0) cutoff frequency

4 In the Cutoff Frequencies toolbar, click Evaluate.

ID Plot Group 7

Now, plot the port outgoing power to reproduce Figure 6.

- I In the Home toolbar, click Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Port Outgoing Power (Normalized) in the Label text field.
- 3 Click to expand the Title section. From the Title type list, choose Manual.
- 4 In the Title text area, type Port Outgoing Power (Normalized).
- 5 Locate the Legend section. From the Position list, choose Middle left.

Global I

- I Right-click Port Outgoing Power (Normalized) and choose Global.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
acpr.port1.P_out/ acpr.port1.P_in	1	Outgoing power - Port 1
<pre>acpr.port2.P_out/ acpr.port1.P_in</pre>	1	Outgoing power - Port 2
<pre>acpr.port3.P_out/ acpr.port1.P_in</pre>	1	Outgoing power - Port 3
acpr.port4.P_out/ acpr.port1.P_in	1	Outgoing power - Port 4
acpr.port5.P_out/ acpr.port1.P_in	1	Outgoing power - Port 5
acpr.port6.P_out/ acpr.port1.P_in	1	Outgoing power - Port 6
acpr.port7.P_out/ acpr.port1.P_in	1	Outgoing power - Port 7
acpr.port8.P_out/ acpr.port1.P_in	1	Outgoing power - Port 8
<pre>acpr.port9.P_out/ acpr.port1.P_in</pre>	1	Outgoing power - Port 9
acpr.port10.P_out/ acpr.port1.P_in	1	Outgoing power - Port 10

4 In the Port Outgoing Power (Normalized) toolbar, click Plot.

From the File menu, choose New.

NEW

In the New window, click Blank Model.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
L	120[cm]	1.2 m	Waveguide length
W	30[cm]	0.3 m	Waveguide width
Н	20[cm]	0.2 m	Waveguide height
Rcurv	8[cm]	0.08 m	Bend curvature radius
Rcyl	20[cm]	0.2 m	Cylinder radius (for dent)

ADD COMPONENT

In the **Home** toolbar, click **Add Component** and choose **3D**.

GEOMETRY I

Work Plane I (wpl)

In the Geometry toolbar, click Work Plane.

Work Plane I (wp I)>Rectangle I (r I)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type L.
- 4 In the Height text field, type W.

Work Plane I (wp I)>Rectangle 2 (r2)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type W.

- 4 In the Height text field, type L.
- **5** Locate the **Position** section. In the **xw** text field, type L-W.

Work Plane I (wbl)>Union I (unil)

- I In the Work Plane toolbar, click Booleans and Partitions and choose Union.
- 2 Click in the **Graphics** window and then press Ctrl+A to select both objects.
- 3 In the Settings window for Union, locate the Union section.
- 4 Clear the Keep interior boundaries check box.
- 5 Click Build Selected.

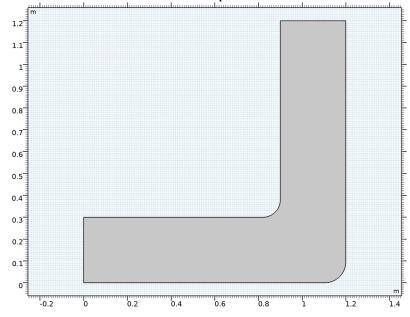
Work Plane I (wbl)>Fillet I (fill)

- I In the Work Plane toolbar, click Fillet.
- **2** On the object unil, select Point 4 only.
- 3 In the Settings window for Fillet, locate the Radius section.
- 4 In the Radius text field, type Rcurv.

Work Plane I (wp I)>Fillet 2 (fil2)

- I In the Work Plane toolbar, click Fillet.
- 2 On the object fill, select Point 7 only.
- 3 In the Settings window for Fillet, locate the Radius section.
- 4 In the Radius text field, type 1.2*Rcurv.
- 5 Click Build Selected.

6 Click the Zoom Extents button in the Graphics toolbar.



Work Plane I (wbl)

In the Model Builder window, click Work Plane I (wpl).

Extrude I (ext I)

- I In the Geometry toolbar, click Extrude.
- 2 In the Settings window for Extrude, locate the Distances section.
- **3** In the table, enter the following settings:

Distances (m) Н

4 Click Build Selected.

Cylinder I (cyl1)

- I In the Geometry toolbar, click Cylinder.
- 2 In the Settings window for Cylinder, locate the Size and Shape section.
- 3 In the Radius text field, type Rcyl.
- 4 Locate the **Position** section. In the x text field, type L/2.
- 5 In the y text field, type L/2.

- 6 In the z text field, type H+0.8*Rcyl.
- 7 Locate the Axis section. From the Axis type list, choose x-axis.

Difference I (dif1)

- I In the Geometry toolbar, click Booleans and Partitions and choose Difference.
- **2** Select the object **ext1** only.
- 3 In the Settings window for Difference, locate the Difference section.
- **4** Find the **Objects to subtract** subsection. Select the **Activate selection** toggle button.
- **5** Select the object **cyll** only.
- 6 Click Build All Objects.
- 7 Click the **Zoom Extents** button in the **Graphics** toolbar.

